

## TABLES

## VENUS,

PREPARED FOR THE USE OF

THE AMERICAN EPHEMERIS AND NAUTICAL ALIIANAG.

BY

GEORGE W. HILL.


PUBLISHED BY AUTHORITY OF THE SECRETARY OF THE NAVY.

> BUREAU OF NAVIGATION, WASHINGTON.
> 1873.


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## PREFACE.

The following tables of Venus have been prepared to take the place of the unsatisfactory elements and tables heretofore used in the preparation of the American Ephemeris and Nautical Almanac.

The elements given in Le Verrier's Annales de l'Observatoire Imperial de Paris, Tome VI., have been corrected by the discussion of an extended series of observations; Le Verrier's expressions for the perturbations have been modified by changes in the adopted values of the planetary masses; and the tables have been carefully arranged so as to facilitate the computation either of particular places, or of an Ephemeris, of the planet.

The work has been performed by Mr. George W. Hill, who has long been one of the most efficient Assistants in the preparation of the works published by this office.

J. H. C. COFFIN,<br>Prof. Math. U. S. N., Superintendent of Nautical Almanac.

Washington, May, 1872.

## CONTENTS.

Istrodectios. Construction and use of the Tables
Page
Elements of the orbit of Venus 1850.01
Precession of the equinoxes ..... 2
Masses of the planets ..... 2
Varying elements of the orbit of Venus ..... 2
Perturbations of the orbit longitude ..... 3
u u a logarithm of the radius vector ..... 4
" * u latitude. ..... 5
Arguments of the tables ..... 6
Obliquity of the ecliptic and nutation ..... 6
Formula for rectangular coördinates ..... 7
" " the effect of nutation. ..... 7
" " aberration, parallax and semi-diameter ..... 7,8

* $\quad$ " rectangular coördinates referred to the ecliptic and equinox of a fixed date ..... 8
Explanation of Tables 1 to XV ..... 9
« 4 « XVI to XXV ..... 10
u $\quad$ u $\quad$ ( XXVI to XXXV ..... 11
a 4 « XXXVI to XL. ..... 12 ..... 13
Dirctions for the wee of the ToWles
Dirctions for the wee of the ToWles
Directions for the wse of the Tables ..... 14
Example ..... 16
Transit of Venus in 1761 ..... 21
« * * 1769 ..... *2
Corrections of the elements of the orbit of Venms ..... 23
Leverrier's elements of the orbnt of Venus ..... 23
Position of Venus at the transits of 1761 and 1769 ..... 23
Normal places in the inferior part of the orbit ..... 24
* $\quad$ a $\quad$ a $=$ superior part of the orbit ..... 25
Equations of condition derived from the longitudes ..... 27
u $\quad$ u $\quad$ u $\quad$ u latitudes ..... 31
Normal equations ..... 34
Corrections of Leverrier's elements ..... 36
Required correction of the mass of Venus ..... 36
Occultation of Mercury by Venus in 1737 ..... 36
TABLES.
Table I. Longitudes of the principal observatories ..... 2
II. Julian date of the beginning of each year ..... 3
III. Number of days from the beginuing of the year ..... 4
IV Equivalents of hours, minutes and seconds in decimals of a day ..... 5
V. Periods of the Arguments ..... 5
VI. Mean longitade, Argaments, $\mathbb{N} e$, for the beginning of each year ..... 6
VII. Motion of mean longitade, \&ic.: Fraction of a year ..... 14
VIII. $\quad$ * $\quad$ * for hours, $d i c$. ..... 17
IX. Factor of a small correction of the longitude ..... 17
X. Equation of the centre ..... 18
XI. to XXV. Perturbations of the longitode ..... 26
Page.
Table . . XXVI. Logarithm of the elliptic radius vector ..... 46
XXVII, to XXXVI. Perturbations of $\log r$ ..... 51
XXXVII., XXXVIII. Perturbations of the latitude ..... 66
XXXIX. Values of $K_{\mathrm{x}}, K_{y}$, \&c., and Args. XV. and XVI for the beginning of each year ..... 72
XL. Corrections of $K_{\mathrm{x}}, K_{\mathrm{y}}, \& c$., due to lunar Nutation ..... 76
XLI. " " " " " due to solar Nutation ..... 77
XLII. Factors for finding corrections of $x, y, z$, due to perturbations of the latitude ..... 78
XLIII. Parallax and semidiameters ..... 78
XLIV. Motions of the Arguments for centuries ..... 79
XLV. A term of long period in the perturbation of the longitude ..... 80
XLVI. Reduction to the Eeliptic ..... 80


# INTRODUCTION. 

## CONSTRUCTION AND USE OF THE TABLES.

The Tables are based on the following elements :-
Epoch, 1850, Jan. 0.0, Washington Mean Time.

$$
\begin{array}{rl}
L^{\prime} & =244 \AA^{\prime} 18 \\
18 & 18.32 \\
\pi^{\prime} & =129 \\
127 & 42.86 \\
\delta^{\prime} & =7519 \\
\hline 53.10 \\
i^{\prime} & =323 \\
e^{\prime} & =0.006843113 \\
n^{\prime} & =2106641^{\prime \prime} .35447
\end{array}
$$

These elements have been derived from a discussion of the data furnished by the transits of Venus in 1761 and 1769, and by observations made at Greenwich in the interval 1836-1870, at Paris in the interval 1838-1866, and at Washington in the interval 1863-1867. In this discussion the Solar Theory of Hansen and Olufsen was used.* Consequently these Tables should be used in conjunction with the Tables du Soleil of these authors.t

The value of the Precession of the Equinoxes, according to Peters, $\ddagger$ is

$$
\cdot 50^{\prime \prime} .2411 t+0^{\prime \prime} .0001134 t^{2}
$$

where the unit of $t$ is the tropical year, and it is counted from 1800. If we make the unit the Julian year, and count $t$ from 1850, the formula will be

$$
50^{\prime \prime} .25351 t+0^{\prime \prime} .0001134 t^{2}
$$

The formulæ which define the motion of the plane of the ecliptic are, according to Hansen and Olufsen, $\$$

$$
\begin{aligned}
& \sin i^{\prime \prime} \sin \Omega^{\prime \prime}=+0^{\prime \prime} .053916 t+0^{\prime \prime} .00001887 t^{2} \\
& \sin i^{\prime \prime} \cos \Omega^{\prime \prime}=-0^{\prime \prime} .467839 t+0^{\prime \prime} .00000562 t^{2}
\end{aligned}
$$

In order to obtain the tropical motion of the planet, it is necessary to add, to the sidereal motion, the precession, and the small term,

$$
-\frac{1}{2} \sin i^{\prime} \sin i^{\prime \prime} \sin \left(\delta^{\prime}-\delta^{\prime \prime}\right)
$$

the numerical value of which is $+0^{\prime \prime} .01382 t$. This it is also necessary to add to the longitude of the perihelion.

[^0]
## INTRODUCTION.

The values of the planetary masses, adopted, are

| Mercury | $m=\frac{1}{4865751}$, | Mars | $m^{\prime \prime \prime}=\frac{1}{3200900}$, |
| :--- | :--- | :--- | :--- |
| Venus | $m^{\prime}=\frac{1}{408134}$, | Jupiter | $m^{\mathrm{iv}}=\frac{1}{1050}$, |
| The Earth and Moon $m^{\prime \prime}=\frac{1}{322800}$, | Saturn | $m^{\mathrm{v}}=\frac{1}{3560}$. |  |

The mass of Mercury is that of Encke, ${ }^{*}$ the mass of the Earth and Moon is that found by Prof. S. Newcomb, $\dagger$ and which corresponds to the value $8^{\prime \prime} .848$ of the mean horizontal parallax of the Sun; the values of the other masses are those adopted by Hansen and Olufsen. On these values of the disturbing masses depend the expressions of the secular and periodic perturbations used, with the single exception, that, since the discussion of the "cobservations indicated $32^{\prime \prime} .515$ as the value of the annual tropical motion of the node, this value has been preferred to the value $32^{\prime \prime} .2931$, given by theory. If we suppose that the modification of the values of the masses, necessary $\therefore$ 啹 produce the first number, should be applied to Venus alone, the mass of this planet would be reduced to 1 $\overline{427240}$.

Thus the following are the expressions of the varying elements, the longitudes being referred to the mean equinox and ecliptic of date, and $t$ reckoned from 1850, Jan. 0.0, Washington Mean Time :-

$$
\begin{aligned}
L^{\prime} & =24 \AA^{\prime} 1^{\prime} 18.32+2106691.62180 t+0^{\prime \prime} .0001134 t^{2} \\
\pi^{\prime} & =1292742.86+\quad 50.0494 t-0.000592 t^{2}, \\
\delta^{\prime} & =751953.10+32.5150 t+0.000151 t^{2} \\
i^{\prime} & =32335.01+00.03814 t-0.0000016 t^{2}, \\
e^{\prime} & =0.006843113-0.00000050009 t+0.0000000000128 t^{2}, \\
& =1411^{\prime \prime} .494-0^{\prime \prime} .10315 t+0^{\prime \prime} .00000265 t^{2} .
\end{aligned}
$$

The value of the semi-axis major of the planet's orbit is given by the equation

$$
a^{\prime}=\left[\frac{1+m^{\prime}}{1+m^{\prime \prime}} \cdot \frac{n^{\prime \prime 2}}{n^{\prime 2}}\right]^{\frac{1}{3}} a^{\prime \prime}
$$

To be consistent, we must employ the same linear unit for the radius vector of Venus as that which Hansen and Olufsen have used for the radius vector of the Earth. From an examination of their formulæ, it appears that they have taken as unity, not $a^{\prime \prime}$, but, in the notation of Laplace, the quantity

$$
a^{\prime \prime}+\frac{1}{6} \sum m a^{\prime / 3} \frac{d A^{(0)}}{d a^{\prime \prime}}
$$

$\Sigma$ denoting summation with respect to all the masses which produce sensible perturbations in the motion of the Earth. Hence their value of $a^{\prime \prime}$ is

$$
1-\frac{1}{6} \Sigma m a^{\prime / 2} \frac{d A^{(0)}}{d a^{\prime \prime}}
$$

And, the numerical values being substituted, we obtain

$$
\log a^{\prime \prime}=9.9999998786
$$

The tropical motion of the Sun, in a Julian year, is, according to the Tables $d u$ Soleil, equal to

$$
360^{\circ}-22^{\prime \prime} .56009-0^{\prime \prime} .380853 \times 0.01677+50^{\prime \prime} .23414
$$

If from this is subtracted $50^{\prime \prime} .25351$, our value of the precession, the value of $n^{\prime \prime}$, we adopt, is obtained,

$$
n^{\prime \prime}=1295977^{\prime \prime} .41415
$$

And consequently,
$\log a^{\prime}=9.8593376699$.

* Astronomische Nachrichten, No. 443.
$\dagger$ Astronomical and Metcorologrcal Olservations made at the United States Naval Observatory during the year 1865. Appendix II., p. 29.


## INTRODUCTION.

The expression of the equation of the centre, for the epoch 1850.0 , is

$$
+2822^{\prime \prime} .971 \sin M+12^{\prime \prime} .074 \sin 2 M+0^{\prime \prime} .072 \sin 3 M
$$

The expression of the logarithm of the elliptic radius vector for the same time is

$$
9.859342748-0.002971874 \cos M-0.000015253 \cos 2 M-0.000000099 \cos 3 M
$$

The elliptic heliocentric latitude referred to the ecliptic of date may be found from the formula

$$
\log \sin \text { lat. }=8.7722149+13.54 t+\log \sin \left[\text { orb. long. }+\left(360^{\circ}-\delta^{\prime}\right)\right]
$$

The secular perturbation of the orbit longitude is given by the formula,

$$
\left(-0^{\prime \prime} .12691 \sin M-0^{\prime \prime} .00108 \sin 2 M\right) \mathrm{m} .
$$

m denoting the number of anomalistic revolutions of the planet from the epoch.
The secular perturbation of the logarithm of the radius vector is given by the formula, (in units of the eighth decimal),

$$
(-0.046+13.360 \cos M+0.137 \cos 2 M) \mathrm{m}
$$

The following are the expressions for the periodic perturbations of Venus; $l, l^{\prime} \& c$. denoting the mean longitudes of the several planets in their order, referred to the mean equinox of 1850.0 . They have been obtained by multiplying the expressions given in Le Verrier's "Annales de l' Observatoire lmperial de Paris," Tome VI, by the proper factors.

## Perturbations of the Orbit Longitude.

- 

Action of Mercury.

$$
\begin{array}{ll}
+0.014 \sin \left(l-l^{\prime}\right) & +0.328 \sin \left(l-2 l^{\prime}+254^{\circ} .8\right) \\
-0.010 \sin 2\left(l-l^{\prime}\right) & +0.015 \sin \left(2 l-3 l^{\prime}+74^{\circ}\right) \\
-0.005 \sin 3\left(l-l^{\prime}\right) & +0.047 \sin \left(3 l^{\prime}-l+35^{\circ}\right) \\
+0.021 \sin \left(2 l-l^{\prime}+284^{\circ}\right) & \\
& +0.139 \sin \left(2 l-4 l^{\prime}+328^{\circ} .3\right) \\
& \\
& +0.453 \sin \left(2 l-5 l^{\prime}+35^{\circ} .1\right) .
\end{array}
$$

Action of the Earth.

```
- ".984 sin}(\mp@subsup{l}{}{\prime}-\mp@subsup{l}{}{\prime\prime}
-11.489 \operatorname{sin}2(\mp@subsup{l}{}{\prime}-\mp@subsup{l}{}{\prime\prime})
+7.260 sin (3\mp@subsup{l}{}{\prime\prime}-3\mp@subsup{l}{}{\prime\prime}+\mp@subsup{0}{}{\circ}\mp@subsup{7}{}{\prime}.6)
+ 1.050 \operatorname{sin}(4\mp@subsup{l}{}{\prime}-4\mp@subsup{l}{}{\prime\prime}+\mp@subsup{0}{}{\circ}1\mp@subsup{0}{}{\prime})
+0.335 sin (5 l' - 5 l'\prime}+\mp@subsup{1}{}{\circ}.5
+0.143 sin 6 (l' - l'\prime}
+}0.013\operatorname{sin}10(\mp@subsup{l}{}{\prime}-\mp@subsup{l}{}{\prime\prime}
+ 0.007 sin 11 (l' - l'\prime}
+0.004 sin 12(l\prime}-\mp@subsup{l}{}{\prime\prime}
+0.003 sin 13(\mp@subsup{l}{}{\prime}-\mp@subsup{l}{}{\prime\prime})
+0.059\operatorname{sin}(4\mp@subsup{i}{}{\prime}-3\mp@subsup{l}{}{\prime\prime}+22\mp@subsup{7}{}{\circ}.7)
+0.099\operatorname{sin}(3\mp@subsup{l}{}{\prime}-2\mp@subsup{l}{}{\prime\prime}+5\mp@subsup{3}{}{\circ}.2)
+0.049\operatorname{sin}(2\mp@subsup{l}{}{\prime\prime}-\mp@subsup{l}{}{\prime\prime}+5\mp@subsup{1}{}{\circ})
+0.070 sin (l\prime\prime}+10\mp@subsup{9}{}{\circ}.2
+0.093 sin (2 ll'}-\mp@subsup{l}{}{\prime}+1\mp@subsup{8}{}{\circ}.2
+3.515 sin (2\mp@subsup{l}{}{\prime}-3\mp@subsup{l}{}{\prime\prime}+26\mp@subsup{8}{}{\circ}\mp@subsup{7}{}{\prime}.5)
```

$+0.067 \sin 7\left(l^{\prime \prime}-l^{\prime \prime}\right) \quad+0.022 \sin \left(2 l^{\prime \prime \prime}+210^{\circ}\right)$
$+0.035 \sin 8\left(l^{\prime \prime}-l^{\prime \prime}\right) \quad+0.044 \sin \left(3 l^{\prime \prime}-l^{\prime}+53^{\circ}\right)$
$+0.019 \sin 9\left(l^{\prime \prime}-l^{\prime \prime}\right) \quad+1.495 \sin \left(5 l^{\prime \prime \prime}-3 l^{\prime \prime}+198^{\circ} 24\right)$

$$
\begin{aligned}
& +0.687 \sin \left(3 l^{\prime \prime}-4 l^{\prime \prime \prime}+268^{\circ} .1\right) \\
& +1.620 \sin \left(4 l^{\prime \prime}-5 l^{\prime \prime}+268^{\circ} 24^{\prime} .5\right) \\
& +0.210 \sin \left(5 l^{\prime \prime}-6 l^{\prime \prime \prime}+89^{\circ} .5\right) \\
& +0.055 \sin \left(6 l^{\prime \prime}-7 l^{\prime \prime}+89^{\circ}\right) \\
& +0.024 \sin \left(7 l^{\prime \prime}-8 l^{\prime \prime \prime}+88^{\circ}\right) \\
& +0.013 \sin \left(8 l^{\prime \prime}-9 l^{\prime \prime \prime}+90^{\circ}\right) \\
& +0.022 \sin \left(2 l^{\prime \prime \prime}+210^{\circ}\right) \\
& +0.044 \sin \left(3 l^{\prime \prime}-l^{\prime \prime}+53^{\circ}\right) \\
& +1.495 \sin \left(5 l^{\prime \prime \prime}-3 l^{\prime \prime}+198^{\circ} 24\right) \\
& +0.188 \sin \left(4 l^{\prime \prime}-6 l^{\prime \prime}+340^{\circ} .7\right) \\
& +0.096 \sin \left(5 l^{\prime \prime}-7 l^{\prime \prime}+337^{\circ} .5\right) \\
& +0.155 \sin \left(6 l^{\prime}-8 l^{\prime \prime}+163^{\circ} .1\right) \\
& +0.015 \sin \left(7 l^{\prime}-9 l^{\prime \prime}+160^{\circ}\right) \\
& +0.013 \sin \left(5 l^{\prime \prime}-2 l^{\prime \prime}+77^{\circ}\right) \\
& +0.218 \sin \left(5 l^{\prime \prime}-8 l^{\prime \prime}+66^{\circ} .5\right) \\
& +0.013 \sin \left(7 l^{\prime \prime}-10 l^{\prime \prime \prime}+67^{\circ}\right) \\
& +0.067 \sin \left(9 l^{\prime \prime}-13 l^{\prime \prime}+346^{\circ} .2\right) \\
& +2.820 \sin \left(8 l^{\prime \prime}-13 l^{\prime \prime}+227^{\circ} 58^{\prime}\right) \\
& +0.026 \sin \left(13 l^{\prime \prime \prime}-7 l^{\prime}+198^{\circ}\right) .
\end{aligned}
$$

## INTRODUCTION.

## Action of Mars.

$$
\begin{aligned}
& -0.048 \sin \left(l^{\prime}-l^{\prime \prime \prime}\right) \\
& +0.059 \sin 2\left(l^{\prime}-l^{\prime \prime \prime}\right) \\
& +0.019 \sin \left(l^{\prime}-2 l^{\prime \prime \prime}+155^{\circ}\right) \\
& +0.657 \sin \left(2 l^{\prime}-3 l^{\prime \prime \prime}+332^{\circ} 44^{\prime}\right)
\end{aligned}
$$

$$
\begin{aligned}
& +\frac{\prime \prime}{\prime \prime} .009 \sin \left(3 l^{\prime}-4 l^{\prime \prime \prime}+333^{\circ}\right) \\
& +1.168 \sin \left(l^{\prime \prime}-3 l^{\prime \prime \prime}+117^{\circ} 56^{\prime}\right) \\
& +0.019 \sin \left(2 l^{\prime}-4 l^{\prime \prime \prime}+126^{\circ}\right) \\
& +0.021 \sin \left(3 l^{\prime}-6 l^{\prime \prime \prime}+281^{\circ}\right) \\
& +0.082 \sin \left(2 l^{\prime \prime}-6 l^{\prime \prime \prime}+74^{\circ} .8\right)
\end{aligned}
$$

Action of Jupiter.

$$
\begin{aligned}
& -\ddot{\prime \prime} .959 \sin \left(l^{\prime}-l^{\mathrm{iv}}+0^{\circ} 31^{\prime}\right) \\
& +0.880 \sin 2\left(l^{\prime}-l^{\mathrm{iv}}\right) \\
& +0.041 \sin 3\left(l^{\prime}-l^{\mathrm{iv}}\right) \\
& +0.007 \sin 4\left(l^{\prime}-l^{\mathrm{iv}}\right) \\
& +0.026 \sin \left(2 l^{\prime}-l^{\mathrm{iv}}+113^{\circ}\right) \\
& +1.557 \sin \left(l^{\mathrm{iv}}+169^{\circ} 50^{\prime}\right)
\end{aligned}
$$

$$
\begin{aligned}
& +{ }^{\prime \prime} .477 \sin \left(l^{\prime \prime}-2 l^{\mathrm{iv}}+155^{\circ} .6\right) \\
& +0.167 \sin \left(2 l^{\prime}-3 l^{\mathrm{iv}}+12^{\circ} .1\right) \\
& +0.019 \sin \left(3 l^{\prime}-4 l^{\mathrm{iv}}+12^{\circ}\right) \\
& +0.094 \sin \left(l^{\prime}+l^{\mathrm{iv}}+2^{\circ} .3\right) \\
& +0.055 \sin \left(2 l^{\mathrm{iv}}+143^{\circ}\right) \\
& +0.046 \sin \left(l^{\prime \prime}-3 l^{\mathrm{iv}}+164^{\circ}\right) \\
& +0.027 \sin \left(2 l^{\prime}-4 l^{\mathrm{iv}}+24^{\circ}\right)
\end{aligned}
$$

Action of Saturn.

$$
\begin{aligned}
& -0.178 \sin \left(l^{\prime \prime}-l^{v}\right) \\
& +0.050 \sin 2\left(l^{\prime \prime}-l^{v}\right)
\end{aligned}
$$

$$
\begin{aligned}
& +{ }^{\prime \prime} .205 \sin \left(l^{\mathrm{v}}+190^{\circ}\right) \\
& +0.025 \sin \left(l^{\prime}-2 l^{\mathrm{v}}+.151^{\circ}\right) \\
& +0.010 \sin \left(2 l^{\prime}-3 l^{\mathrm{v}}+90^{\circ}\right)
\end{aligned}
$$

Perturbation of the second order, depending on the product of the masses of the Earth and Mars.

$$
+0^{\prime \prime} .282 \sin \left(4 l^{\prime \prime \prime}+3 l^{\prime \prime}-7 l^{\prime \prime}+147^{\circ} .1\right)
$$

Perturbations of the Common Logarithm of the Radius Vector, in units of the eighth decimal.
Action of Mercury.

```
+4.3
+8.1 cos(l-l')
+ 1.1 cos 2(l-l')
+6.1\operatorname{cos}(2l-l}+28\mp@subsup{5}{}{\circ}
+4.3 cos (l'}+10\mp@subsup{5}{}{\circ}
```

$$
\begin{aligned}
& +15.3 \cos \left(2 l-4 l^{\prime}+150^{\circ} .7\right) \\
& +22.2 \cos \left(l-2 l^{\prime}+75^{\circ} .1\right) \\
& +1.9 \cos \left(2 l-3 l^{\prime}+75^{\circ}\right) \\
& +3.5 \cos \left(3 l^{\prime}-l+207^{\circ}\right) \\
& +7.5 \cos \left(2 l-5 l^{\prime}+226^{\circ}\right) .
\end{aligned}
$$

Action of the Earth.
$-18.6$
$+228.2 \cos \left(l^{\prime \prime}-l^{\prime \prime}\right)$
大 $998.6 \cos 2\left(l^{\prime \prime}-l^{\prime \prime}\right)$
$-841.8 \cos \left(3 l^{\prime}-3 l^{\prime \prime}+0^{\circ} 8^{\prime}\right)$
$-145.2 \cos 4\left(l^{\prime \prime}-l^{\prime \prime}\right)$
$-52.2 \cos \left(5 l^{\prime}-5 l^{\prime \prime}+0^{\circ} 20^{\prime}\right)$
$-23.0 \cos 6\left(l^{\prime \prime}-l^{\prime \prime}\right)$
$-11.5 \cos 7\left(l^{\prime \prime}-l^{\prime \prime}\right)$

- $6.4 \cos 8\left(l^{\prime \prime}-l^{\prime \prime}\right)$
- $3.5 \cos 9\left(l^{\prime \prime}-i^{\prime \prime}\right)$
- $2.6 \cos 10\left(l^{\prime}-l^{\prime \prime}\right)$
$+7.2 \cos \left(4 l^{\prime \prime}-3 l^{\prime \prime}+45^{\circ}\right)$
$+11.7 \cos \left(3 l^{\prime}-2 l^{\prime \prime}+230^{\circ} .5\right)$
$+6.6 \cos \left(2 l^{\prime}-l^{\prime \prime}+230^{\circ}\right)$
$+3.1 \cos \left(l^{\prime}+105^{\circ}\right)$

$$
\begin{aligned}
& +\quad 4.7 \cos \left(l^{\prime \prime}+286^{\circ}\right) \\
& +\quad 3.2 \cos \left(2 l^{\prime \prime}-l^{\prime \prime}+114^{\circ}\right) \\
& +\quad 76.8 \cos \left(2 l^{\prime \prime}-3 l^{\prime \prime \prime}+89^{\circ} .8\right) \\
& +\quad 46.1 \cos \left(3 l^{\prime \prime}-4 l^{\prime \prime}+88^{\circ} .9\right) \\
& +162.2 \cos \left(4 l^{\prime \prime}-5 l^{\prime \prime \prime}+88^{\circ} 52^{\prime}\right) \\
& +\quad 25.6 \cos \left(5 l^{\prime \prime}-6 l^{\prime \prime \prime}+268^{\circ} .7\right) \\
& +\quad 7.7 \cos \left(6 l^{\prime \prime}-7 l^{\prime \prime \prime}+268^{\circ}\right) \\
& +\quad 4.2 \cos \left(7 l^{\prime \prime}-8 l^{\prime \prime \prime}+270^{\circ}\right) \\
& +\quad 3.7 \cos \left(2 l^{\prime \prime}+30^{\circ}\right) \\
& +\quad 4.5 \cos \left(3 l^{\prime \prime \prime}-l^{\prime}+249^{\circ}\right) \\
& +\quad 17.2 \cos \left(5 l^{\prime \prime}-3 l^{\prime \prime}+21^{\circ} .8\right) \\
& +\quad 7.2 \cos \left(4 l^{\prime \prime}-6 l^{\prime \prime}+159^{\circ}\right) \\
& +\quad 7.1 \cos \left(5 l^{\prime \prime}-7 l^{\prime \prime}+172^{\circ}\right) \\
& +\quad 17.2 \cos \left(6 l^{\prime \prime}-8 l^{\prime \prime}+338^{\circ} .2\right) \\
& +\quad 6.9 \cos \left(9 l^{\prime \prime}-13 l^{\prime \prime \prime}+158^{\circ}\right) \\
& +\quad 2.4 \cos \left(13 l^{\prime \prime}-7 l^{\prime \prime}+25^{\circ}\right) .
\end{aligned}
$$

## INTRODUCTION.

## Action of Mars.

$$
+68.1 \cos \left(2 l^{\prime}-3 l^{\prime \prime \prime}+152^{\circ} .6\right) .
$$

## Action of Jupiter.

- 19.2
$+299.2 \cos \left(l^{\prime}-l^{\text {iv }}+0^{\circ} 20^{\prime}\right)$
$-133.0 \cos 2\left(l^{\prime}-l^{\text {iv }}\right)$
- $7.0 \cos 3\left(l^{\prime}-l^{\text {iv }}\right)$
$+\quad 1.1 \cos \left(2 l^{\prime}-l^{\mathrm{iv}}+237^{\circ}\right)$

$$
\begin{aligned}
& +8.8 \cos \left(l^{\mathrm{iv}}+352^{\circ}\right) \\
& +46.9 \cos \left(l^{\prime}-2 l^{\mathrm{iv}}+335^{\circ} .0\right) \\
& +24.8 \cos \left(2 l^{\prime}-3 l^{\mathrm{iv}}+192^{\circ} .1\right) \\
& +9.6 \cos \left(l^{\prime}+l^{\mathrm{iv}}+182^{\circ}\right) \\
& +4.4 \cos \left(l^{\prime}-3 l^{\mathrm{iv}}+340^{\circ}\right)
\end{aligned}
$$

Action of Saturn.

$$
\begin{array}{ll}
+18.7 \cos \left(l^{\prime}-l^{v}\right) & +2.5 \cos \left(l^{\prime}-2 l^{v}+334^{\circ}\right) \\
-4.3 \cos 2\left(l^{\prime}-l^{v}\right) &
\end{array}
$$

## Perturbations of the Latitude.

Action of the Earth.

$$
\begin{aligned}
& +0.012 \sin \left(2 l^{\prime \prime}-2 l^{\prime \prime}+175^{\circ}\right) \\
& +0.016 \sin \left(3 l^{\prime}-3 l^{\prime \prime}+356^{\circ}\right) \\
& +0.013 \sin \left(4 l^{\prime \prime}-3 l^{\prime \prime}+284^{\circ}\right) \\
& +0.026 \sin \left(3 l^{\prime}-2 l^{\prime \prime}+286^{\circ}\right) \\
& +0.078 \sin \left(2 l^{\prime \prime}-l^{\prime \prime}+285^{\circ}\right) \\
& +0.124 \sin \left(l^{\prime}+104^{\circ} .5\right) \\
& +0.092 \sin \left(2 l^{\prime \prime}-l^{\prime}+104^{\circ} .5\right)
\end{aligned}
$$

$$
\begin{aligned}
& +0.075 \sin \left(2 l^{\prime \prime}-3 l^{\prime \prime}+75^{\circ} .5\right) \\
& +0.081 \sin \left(3 l^{\prime}-4 l^{\prime \prime}+75^{\circ} .5\right) \\
& +0.308 \sin \left(4 l^{\prime}-5 l^{\prime \prime}+75^{\circ} .3\right) \\
& +0.050 \sin \left(5 l^{\prime \prime}-6 l^{\prime \prime}+256^{\circ}\right) \\
& +0.014 \sin \left(6 l^{\prime \prime}-7 l^{\prime \prime}+258^{\circ}\right) \\
& +0.020 \sin \left(3 l^{\prime \prime}-l^{\prime}+20^{\circ}\right) \\
& +0028 \sin \left(6 l^{\prime}-8 l^{\prime \prime}+343^{\circ}\right) \\
& +0.015 \sin \left(9 l^{\prime}-13 l^{\prime \prime}+143^{\circ}\right)
\end{aligned}
$$

Action of Jupiter.

$$
\begin{aligned}
& \left.+{ }^{\prime \prime} .020 \sin l^{\prime}-l^{\mathrm{iv}}+153^{\circ}\right) \\
& +0.159 \sin \left(l^{\prime}-2 l^{\mathrm{iv}}+61^{\circ} .8\right)
\end{aligned}
$$

Action of Saturn.

$$
+0^{\prime \prime} .017 \sin \left(l^{\prime}-2 l^{v}+28^{\circ}\right)
$$

The tropical motion of Venus in different intervals of time, for the epoch 1850.0 , is,


Denoting by $d$ the number of days elapsed from the epoch (1850, Jan. 0.0, Washington mean time), the values of $l, l^{\prime}, \& c$., are-

$$
\begin{gathered}
l^{\prime}=324.0656+4.0923387467 \mathrm{~d}, \\
l^{\prime}=244.3050+1.6021304695 \mathrm{~d}, \\
l^{\prime \prime}=100.0159+0.9856091228 \mathrm{~d}, \\
l^{\prime \prime \prime}=83.2669+0.5240328545 \mathrm{~d}, \\
l^{\mathrm{iv}}=159.9594+0.0830912762 \mathrm{~d}, \\
l^{\mathrm{v}}=14.8203+0.0334596753 \mathrm{~d} . \\
5
\end{gathered}
$$

## INTRODUCTION.

The Arguments employed in these tables have severally the following meanings:-
The Argument rat is an integer, which denotes the number of times Venus has passed through its perihelion since the beginning of 1850 ; it is negative before this epoch, and remains constant during an amomistic revolution of tho planet.

Argument $I$ is the number of mean solar days siuce $M=0^{\circ}$.
" II is the number of Julian yeurs since $8 l^{\prime}-13 l^{\prime \prime \prime}+318^{\circ} 47^{\prime}=0^{\circ}$.
" III is the number of mean solar days sinec $l^{\prime}-.3 t^{\prime \prime \prime}=0^{\circ}$.
" IV is the number of mean solar days since 5$)^{\prime \prime \prime}-3 "^{\prime \prime}+288^{\circ} 27^{\prime}=0^{\circ}$.
" V is the number of mean solar days since $2 l^{\prime}-3 l^{\prime \prime}=0^{\circ}$.
" VI is the number of mean solar days since $l^{\prime}-l^{\prime \prime}=0^{\circ}$.
" VII is the number of mean solar days since $4 l^{\prime \prime}-57^{\prime \prime}+1^{\circ} 59^{\prime}=0^{\circ}$.
" VIII is the number of mean solar days sinee $\left.27^{\prime}-3\right]^{\prime \prime \prime \prime}+65^{\circ} 32^{\prime}=0^{\circ}$.
" IX is the number of mean solar days since $7^{\prime \prime} 7^{\mathrm{iv}}=0^{\circ}$.
" X is the value of $l$, when last $l^{\prime}=129^{\circ} 2714^{\prime \prime} .5,^{*}$ in parts of 60 to a circumference.
" XI is the value of $\ell^{\prime \prime}$, when last $\gamma^{\prime}=129^{\circ} 27^{\prime} 14^{\prime \prime} .5$, in parts of 240 to a circumference.
" XII is the value of $l^{\prime \prime \prime}$ when last $7^{\prime}=129^{\circ} 27^{\prime} 11^{\prime \prime} .5$, in parts of 60 to a circumferenee.
" XIII is the value of $7^{\prime \prime}$, when last $l^{\prime}=129^{\circ} 27^{\prime} 14^{\prime \prime} .5$, in parts of 60 to a circumference.
" XIV is the value of $T^{v}$, when last $\eta^{\prime}=129^{\circ} 27^{\prime} 11^{\prime \prime} .5$, in parts of 36 to a circumference.
". XV is $\operatorname{Arg} . \mathrm{XI}+\mathrm{Arg} . \mathrm{XIII}+0.22+$ day of the year, of Hansen and Olufsen.
" XVI is Arg. I $+022052+0.01791+$ day of the year, of Hansen and Olufsen.
Arguments X-XIV remain constant during a period of Argument I, and are atgmented, in each ease, by a certain fixed quantity, when Vonus passes through its perihelion and mis inereased by a unit.

From the data previously given, are readily obtained the following expressions for the value of the different arguments; $i$ denoting an integer, in general so taken that the Argument may be less thau its period:

$$
\begin{aligned}
& \mathrm{I}=71^{4} .6815355^{2}+d+0^{4} .0000001224 t^{2}-224^{4} .700777861 \mathrm{~mm}, \uparrow \\
& \mathrm{II}=167 \% .9+t-238.92 i, \\
& \mathrm{III}=11804^{2} .26 \quad+d-11987^{2} .25 i, \\
& \text { IV }=457^{d} .137 \quad+d-2959^{d} .209 i, \\
& \mathrm{~V}=762^{2} .072+d-1454^{4} .9358 i, \\
& \mathrm{VI}=231^{1.0375}+d-583^{\mathrm{n}} .92137 \mathrm{i} \text {, } \\
& \mathrm{VII}=80^{4} .466+d-243^{d} .16487 i, \\
& \mathrm{VIII}=186^{\mathrm{d}} .467+d-220^{4} .56628 i, \\
& \mathrm{IX}=55^{4} .526+d-236^{2} .99191 i, \\
& \mathrm{X}=5.167+33.25863 \mathrm{pn2}-60 i \text {, } \\
& \mathrm{XI}=19.5741+147.64477 \mathrm{~m}-240 i \\
& \mathrm{XII}=\quad 7.6168+19.62509 \mathrm{~m}-60 i, \\
& \text { XIII }=25.6671+3.11178 \text { m }-60 i \text {, } \\
& \mathrm{XIV}=1.2422+0.75181 \mathrm{~m}-36 i, \\
& \mathrm{XV}=4037^{2} .4+d-6798^{d} .262 i, \\
& \mathrm{XVI}=\quad 1^{3} .64+d-365^{\mathrm{d}} .21219 i .
\end{aligned}
$$

'The values of the obliquity of the celiptic and of the nutation, employed in these 'lables, are those given in the Tubles du Soleil,

$$
\begin{aligned}
\varepsilon & =23^{\circ} 27^{\prime} 31^{\prime \prime} .42-0^{\prime \prime} .46784 t-0^{\prime \prime} .000001405 t^{2} \\
\Delta \zeta^{\prime \prime} & =-17^{\prime \prime} .332 \sin \delta+0^{\prime \prime} .208 \sin 2 \Omega-1^{\prime \prime} .254 \sin 2 \odot \\
\Delta \varepsilon & =+9^{\prime \prime} .271 \cos \Omega-0^{\prime \prime} .089 \cos 2 \Omega
\end{aligned}
$$

$\Omega_{0}$ being the longitude of the Moon's ascending node, and © the Sun's true longitude.

[^1]
## INTRODUCTION.

The rectangular coördinates of a planet, referred to the equinox and equator, are most readily computed by means of the formulæ-

$$
\begin{aligned}
& x=k_{\mathrm{x}} r \sin \left(\lambda+K_{\mathrm{x}}\right)+p_{\mathrm{x}} \delta \beta, \\
& y=k_{\mathrm{y}} r \sin \left(\lambda+K_{\mathrm{y}}\right)+p_{y} \delta \beta, \\
& z=k_{\mathrm{z}} r \sin \left(\lambda+K_{z}\right)+p_{\mathrm{z}} \delta \beta,
\end{aligned}
$$

where $\lambda$ is the orbit longitude, and $\delta \beta$ the perturbation of the latitude, expressed in parts of the radius
The quantities $k_{\mathrm{x}}, K_{\mathrm{x}}, \& c \mathrm{c}$., are obtained from the following formulæ:-
Find $h, H, g, G$ from the equations

$$
\begin{array}{ll}
h \sin H=\sin ^{2} \frac{i}{2} \sin 2 \Omega, & g \sin G=\sin i \cos \Omega \\
h \cos H=\sin i \sin \Omega, & g \cos G=1-2 \sin ^{2} \frac{i}{2} \cos ^{2} \Omega
\end{array}
$$

then

$$
\begin{array}{cc}
k_{\mathrm{x}} \sin K_{\mathrm{x}}=1-2 \sin ^{2} \frac{i}{2} \sin ^{2} \Omega, & k_{\mathrm{y}} \sin K_{\mathrm{y}}=h \sin (H+\varepsilon), \\
k_{\mathrm{x}} \cos K_{\mathrm{x}}=h \sin H, & k_{\mathrm{y}} \cos K_{\mathrm{y}}=g \cos (G+\varepsilon), \\
k_{\mathrm{z}} \sin K_{\mathrm{z}}=-h \cos (H+\varepsilon), \\
k_{\mathrm{z}} \cos K_{\mathrm{z}}=\quad g \sin (G+\varepsilon) .
\end{array}
$$

The values of $p_{\mathrm{x}}, p_{\mathrm{y}}$ and $p_{\mathrm{z}}$ are, $\lambda^{\prime}$ denoting the longitude reduced to the ecliptic,

$$
\begin{aligned}
& p_{\mathrm{x}}=-r \sin \beta \cos \lambda^{\prime} \\
& p_{\mathrm{y}}=-r \sin \beta \cos \varepsilon \sin \lambda^{\prime}-r \cos \beta \sin \varepsilon \\
& p_{\mathrm{z}}=-r \sin \beta \sin \varepsilon \sin \lambda^{\prime}+r \cos \beta \cos \varepsilon
\end{aligned}
$$

These formulæ avail for obtaining $x, y$, and $z$ referred to any equinox and equator, provided that the longitudes $\lambda, \Omega$ are referred to the same equinox, and the proper values are assigned to the inclinations $i$ and $\varepsilon$.

But when the values of $k_{\mathrm{x}}, K_{\mathrm{x}}, \& c$., have been computed for mean equinox of date, the effect of nutation on these quantities will be most easily computed by the aid of these differential coefficients,

$$
\begin{aligned}
& \frac{d \cdot \log k_{\mathrm{x}}}{d \varepsilon}=0, \\
& \frac{d . \log k_{y}}{d \varepsilon_{1}}=-\frac{M k_{z}}{k_{y}} \cos \left(K_{y}-K_{z}\right), \quad \frac{d K_{y}}{d \varepsilon}=\frac{k_{z}}{k_{y}} \sin \left(K_{\mathrm{y}}-K_{z}\right), \\
& \frac{d \cdot \log k_{\mathrm{z}}}{d \varepsilon}=\frac{\mathrm{K}_{\mathrm{z}} k_{y}}{k_{\mathrm{z}}} \cos \left(K_{\mathrm{y}}-K_{z}\right), \quad \frac{d K_{\mathrm{z}}}{d \varepsilon}=\frac{k_{\mathrm{y}}}{k_{z}} \sin \left(K_{\mathrm{y}}-K_{z}\right), \\
& \frac{d . \log k_{\mathrm{x}}}{d \delta}=\frac{2 M}{k_{\mathrm{x}}} \sin ^{2} \frac{i}{2} \cos \left(K_{\mathrm{x}}+2 \Omega\right) \text {, } \\
& \frac{d K_{\mathrm{x}}}{d \Omega}=-\frac{2}{k_{\mathrm{x}}} \sin ^{2} \frac{i}{2} \sin \left(K_{\mathrm{x}}+2 \Omega\right) \text {, } \\
& \frac{d \cdot \log k_{y}}{d \Omega}=\frac{M}{k_{y}}\left[2 \sin ^{2} \frac{i}{2} \cos \varepsilon \sin \left(K_{y}+2 \Omega\right)+\sin i \sin \varepsilon \sin \left(K_{y}+\Omega\right)\right] \text {, } \\
& \frac{d K_{\mathrm{y}}}{d \Omega}=\frac{1}{k_{\mathrm{y}}}\left[2 \sin ^{2} \frac{i}{2} \cos \varepsilon \cos \left(K_{y}+2 \Omega\right)+\sin i \sin \varepsilon \cos \left(K_{y}+\Omega\right)\right] \text {, } \\
& \frac{d \cdot \log k_{\mathrm{z}}}{d \Omega}=\frac{M}{k_{\mathrm{z}}}\left[2 \sin ^{2} \frac{i}{2} \sin \varepsilon \sin \left(K_{\mathrm{z}}+2 \Omega\right)-\sin i \cos \varepsilon \sin \left(K_{\mathrm{z}}+\Omega\right)\right] \text {, } \\
& \frac{d K_{z}}{d \Omega}=\frac{1}{k_{z}}\left[2 \sin ^{2} \frac{i}{2} \sin \varepsilon \cos \left(K_{z}+2 \Omega\right)-\sin i \cos \varepsilon \cos \left(K_{z}+\Omega\right)\right],
\end{aligned}
$$

where $M$ denotes the modulus of common logarithms. In computing the variations of $\log k_{\mathrm{x}}, \log k_{\mathrm{y}}$, and $\log k_{z}$, $\Delta \varepsilon$ and $\Delta \Omega$ or $\Delta \psi$ must be expressed in parts of the radius.

In computing the aberration, the constant of Struve should be used. The aberration time is then given by the formula, $\Delta$ being the distance of the planet from the Earth.
$\log$. aberration time in days $=7.76052+\log . \Delta$.

## INTRODUCTION.

The parallax is given by the formula

$$
\text { parallax }=\frac{8^{\prime \prime} .848}{\Delta}
$$

and the semi-diameter by the formula

$$
\text { semi-diameter }=\frac{8^{\prime \prime} .546}{\triangle}
$$

In the computation of the perturbations produced by Venus on other planetary bodies, the values of the inclination of the orbit and the longitude of the ascending node referred to the ecliptic and equinox of some fixed date are needed; also the reduction of the longitude to this ecliptic and equinox is wanted. If the current time be $1850+t$, and the fixed date $1850+t_{0}$, and $\psi$ denote the general precession from 1850 to $1850+t$, and $\lambda$ denote the orbit longitude, and $\psi_{0}$ denote the general precession from 1850 to $1850+t_{0}$, the formulæ, we are in quest of, are

$$
\begin{aligned}
i_{\mathrm{o}} & =i-0^{\prime \prime} .06634\left(t-t_{\mathrm{o}}\right) \\
\delta_{\mathrm{o}} & =\delta-\left(\psi-\psi_{\mathrm{o}}\right)+7^{\prime \prime} .8616\left(t-t_{\mathrm{o}}\right) \\
\lambda_{\mathrm{o}} & =\lambda-\left(\psi-\psi_{\mathrm{o}}\right)-0^{\prime \prime} .01382\left(t-t_{\mathrm{o}}\right)
\end{aligned}
$$

Or, with sufficient accuracy for our purpose,

$$
\begin{aligned}
i_{0} & =3^{\circ} 23^{\prime} 35^{\prime \prime}+0^{\prime \prime} .03814 t_{\mathrm{o}}-0^{\prime \prime} .02820\left(t-t_{0}\right) \\
\delta_{0} & =75^{\circ} 19^{\prime} 53^{\prime \prime}+32^{\prime \prime} .515 t_{\mathrm{o}}-9^{\prime \prime} .882\left(t-t_{\mathrm{o}}\right) \\
\lambda_{\mathrm{o}} & =\lambda-50^{\prime \prime} .273\left(t-t_{\mathrm{o}}\right)
\end{aligned}
$$

In the American Ephemeris the heliocentric coördinates of the planets are given, for the purpose of the computation of special perturbations, referred to the ecliptic and equinox of the $2400000^{\text {th }}$ day of the Julian period, and of every $5000^{\text {th }}$ day thereafter. If $d$ denote the number of days between the epoch and the current time, (it will be negative when the current time is before the epoch,) the formulæ for the computation of these coördinates, for Venus, are ;-

Epoch $=2400000^{\text {th }}$ day of the Julian Period $=1858$, Nov. 16.
$\lambda_{0}=\lambda-0^{\prime \prime} .13763 d$,
$x_{0}=[9.99929] r \sin \left(\lambda_{0}+89^{\circ} 58^{\prime} 32^{\prime \prime}\right)$,
$y_{\circ}=[9.99995] r \sin \left(\lambda_{\circ}+0^{\circ} 1^{\prime} 29^{\prime \prime}\right)$
$z_{\circ}=[8.7722] r \sin \left(\lambda_{0}+284^{\circ} 35^{\prime} 18^{\prime \prime}+0^{\prime \prime} .027 d\right)$.
Kpoch $=2405000^{\text {th }}$ day of the Julian Period $=1872$, July 25.
$\lambda_{0}=\lambda-0^{\prime \prime} .13764 d$,
$x_{0}=[9.99929] r \sin \left(\lambda_{0}+89^{\circ} 58^{\prime} 32^{\prime \prime}\right)$,
$y_{\circ}=[9.99995] r \sin \left(\lambda_{0}+0^{\circ} 1^{\prime} 28^{\prime \prime}\right)$,
$z_{\circ}=[8.7722] r \sin \left(\lambda_{0}+284^{\circ} 27^{\prime} 53^{\prime \prime}+0^{\prime \prime} .027 d\right)$.
Epoch $=2410000^{\text {th }}$ day of the Julian Period $=1886$, Apr. 3.
$\lambda_{0}=\lambda-0^{\prime \prime} .13765 d$,
$x_{0}=[9.99928] r \sin \left(\lambda_{0}+89^{\circ} 58^{\prime} 33^{\prime \prime}\right)$,
$y_{0}=[9.99995] r \sin \left(\lambda_{0}+0^{\circ} 1^{\prime} 27^{\prime \prime \prime}\right)$
$z_{0}=[8.7723] r \sin \left(\lambda_{0}+284^{\circ} 20^{\prime} 28^{\prime \prime}+0^{\prime \prime} .027 d\right)$.
Epoch $=2415000^{\text {th }}$ day of the Julian Period $=1899$, Dec. 11.
$\lambda_{0}=\lambda-0^{\prime \prime} .13766 d$,
$x_{\circ}=[9.99928] r \sin \left(\lambda_{\circ}+89^{\circ} 58^{\prime} 34^{\prime \prime}\right)$,
$y_{0}=[9.99995] r \sin \left(\lambda_{0}+0^{\circ} 1^{\prime} 26^{\prime \prime}\right)$
$z_{\circ}=[8.7723] r \sin \left(\lambda_{0}+284^{\circ} 13^{\prime} 3^{\prime \prime}+0^{\prime \prime} .027 d\right)$.
Epoch $=2420000^{\text {th }}$ day of the Julian Period $=1913$, Aug. 20.
$\lambda_{0}=\lambda-0^{\prime \prime} .13766 d$,
$x_{\circ}=[9.99928] r \sin \left(\lambda_{0}+89^{\circ} 58^{\prime} 34^{\prime \prime}\right)$,
$y_{0}=[9.99995] r \sin \left(\lambda_{0}+0^{\circ} 1^{\prime} 24^{\prime \prime}\right)$,
$z_{0}=[8.7723] r \sin \left(3^{\circ}+284^{\circ} 5^{\prime} 37^{\prime \prime}+0^{\prime \prime} .027 d\right)$.

## INTRODUCTION.

In the above expressions of the rectangular coordinates, the logarithms of the constant factors, inclosed in $\rfloor$, have been given, instead of the constants themselves; and the perturbations of the latitude have been negleeted.

Table I. contains the longitudes of the prineipal Ohservatories from Washington, as given by Dr. Gould in the American Lphemeris for 1870. West longitudes are considered as positue.

Tables II., III., and IV. are tables of $\Lambda$ stronomical Dites in mean solar days, from which any date, given in the usual form of reference to the Christian era, may be reduced to its value in days and decimals of a day of the Iulian period. They are taken from Pemes's Lamar 'Tables. By adding the days given for the current century to the days of the previons centemial date, we obtain the number of days elapsed of the Julian Period for Jun. $0^{1}$ Mean Noon in common years and for lan. $1^{\text {d }}$ in lissextile years. 'To this should be added the days and decimals of a day for fractional parts of a year given in Tables III, and IV.

Table V. contains the periods of the various arguments, and multiplies of them, which it is sometimes necessary to subtract, to render the arguments less than their periods.

Table VI. contains for Washington Mam Noon of Jan. $0^{d}$ in common years, Jan. $1^{11}$ in bissextite years, of each year from 1750 to $\mathbf{1 9 5 0}$, the following quantities:

$$
\begin{aligned}
L= & 214^{\circ} 18^{\prime} 18^{\prime \prime} .32-0^{\circ} 47^{\prime} 40^{\prime \prime} .00+2106691^{\prime \prime} .6218 t \\
& +0^{\prime \prime} .0001131 t^{2}+0^{\prime \prime} .282 \sin \left(1 l^{\prime \prime \prime}+3 l^{\prime}-7 l^{\prime \prime \prime}+147^{\circ} .1\right)
\end{aligned}
$$

the integer res, the Argunents I.-XIV., the logarithm of the sine of the inelination, and the supplement to $360^{\circ}$ of the moan longitude of the ascending node. The term $0^{\circ} 47^{\prime} 40^{\prime \prime} .00$ in $L$ is equivalent to the sum of all the constants which have been added to the quantities in the tables of the equation of the eentre, and of the periodic perturbations of the orbit longitude, in order to render them always positive.

Table VII. contains for every day of the year, the motion of the mean longitude, and the motion of the sup. plement of the node, and the fraction of the year from the begiming of the year.

Table VIII. contains the motion of $L$ for hours. minutes and seconds; also for tenths, hundredths and thousandths of a day.

Table 1X. contains the factor of a small correction to be applied to $L$, on account of the inequality of its motion. The quantity taken from this table must be multiplied by the fraction of the year obtained from the preceding table, and the product added to $L$.

Table X. contains the Lquation of the Centre for every tenth of a day of Argument I. Its secular variation, corresponding to the fractional part of the anomalistic period, is included in the numbers of the table. The constant alded, to render all the numbers positive, is $47^{\prime} 3^{\prime \prime} .50$.

Tables Xl,-XXV. contain the perturbations of the Orbit Longitude. They are given in units of hundredths of a sccond of arc.

And particularly,-Table XI. contains the factor of the secular perturbation for cach day of Argument I. The quantity taken from this table must be multiplied by the integer m. The logarithm of the factor is also given, as some may prefer making the multiplication by the aid of logarithms.
'Table XII. contains the factor of that part of the secular perturbation which varies as the square of the time. It is given nt intervals of 4 days of the Argument I. The quantity taken from this table, must be multiplied by $\left(\frac{1 \mathrm{Im}}{100}\right)^{2}$. The logarithm of the factor is also given. The formula for the numbers of this table is

$$
+2.01 \sin M
$$

Table XIII. contains the long period term, due to the aetion of the Earth,

$$
+2^{\prime \prime} .820 \sin \left(8 l^{\prime}-13 l^{\prime \prime}+227^{\circ} 58^{\prime}\right)
$$

It is given at intervals of 2 years of the Argument II. The constant added to render all the numbers positive is $\mathfrak{2}^{\prime \prime} .82$.
Table XIV. contains the terms

$$
\begin{aligned}
& +\mathbf{1}^{\prime \prime} .168 \sin \left(l^{\prime \prime}-3 l^{\prime \prime \prime}+117^{\circ} 56^{\prime}\right) \\
& +0^{\prime \prime} .082 \sin \left(2 l^{\prime}-6 l^{\prime \prime \prime}+74^{\circ} .8\right)
\end{aligned}
$$

due to the action of Mars. They are given at intervals of 200 days of the Argument III. The constant added is $\mathbf{1}^{\prime \prime} . \mathbf{1 5}$.
Table XV, contains the term

$$
+1^{\prime \prime} \cdot 495 \sin \left(5 l^{\prime \prime}-3 l^{\prime}+198^{\circ} 24^{\prime}\right)
$$

due to the action of the Earth. It is given at intervals of 40 days of the Argument IV. 'The constant added is $\mathbf{l}^{\prime \prime} .50$

## INTRODUCTION.

Fable XVI. contains the terms

$$
\begin{aligned}
& +3^{\prime \prime} .515 \sin \left(9 l^{\prime}-3 l^{\prime \prime}+268^{\circ} 7^{\prime} .5\right) \\
& +0^{\prime \prime} .188 \sin \left(4 l^{\prime}-6 l^{\prime \prime}+340^{\circ} .7\right)
\end{aligned}
$$

due to the action of the Earth. They are given at intervals of 16 days in the Argument $V$. The constant added is $3^{\prime \prime} .60$.

Table XVII. contains the terms

$$
\begin{array}{ll}
-{ }^{\prime \prime} .981 \sin \left(l^{\prime}-l^{\prime \prime}\right) & +0.067 \sin \left(7 l^{\prime \prime}-7 l^{\prime \prime}\right) \\
-11.489 \sin \left(2 l^{\prime}-2 l^{\prime \prime}\right) & +0.035 \sin \left(8 l^{\prime \prime}-8 i^{\prime \prime}\right) \\
+7.260 \sin \left(3 l^{\prime}-3 l^{\prime \prime}+0^{\circ} 7^{\prime} .6\right) & +0.019 \sin \left(9 l^{\prime}-9 l^{\prime \prime}\right) \\
+1.050 \sin \left(4 l^{\prime}-4 l^{\prime \prime \prime}+0^{\circ} .10^{\prime}\right) & +0.013 \sin \left(10 l^{\prime}-10 l^{\prime \prime}\right) \\
+0.335 \sin \left(5 l^{\prime}-5 l^{\prime \prime}+1^{\circ} .5\right) & +0.007 \sin \left(11 l^{\prime}-11 l^{\prime \prime}\right) \\
+0.143 \sin \left(6 l^{\prime}-6 l^{\prime \prime \prime}\right) & +0.004 \sin \left(12 l^{\prime}-12 l^{\prime \prime}\right) \\
& \\
& +0.003 \sin \left(13 l^{\prime}-13 l^{\prime \prime}\right)
\end{array}
$$

due to the action of the Earth. They are given at intervals of 2 days in the Argument Vl. The constant added is $16^{\prime \prime}$. 65 .

Table XVIII contains the term

$$
+1^{\prime \prime} .620 \sin \left(4 l^{\prime}-5 l^{\prime \prime}+268^{\circ} 24^{\prime} .5\right)
$$

due to the action of the Earth. It is given at intervals of 4 days in the Argument VII. The constant added is $\mathbf{1}^{\prime \prime} .62$.
Table XIX. contains the term

$$
+0^{\prime \prime} .657 \sin \left(2 l^{\prime}-3 l^{\prime \prime \prime}+339^{\circ} 44^{\prime}\right)
$$

due to the action of Mars. It is given at intervals of 4 days in the Argument VIII. The constant added is $0^{\prime \prime} .66$.
Table XX. contains the terms

$$
\begin{array}{ll}
-2^{\prime \prime} .959 \sin \left(l^{\prime}-l^{\text {iv }}+0^{\circ} 31^{\prime}\right) & +0^{\prime \prime} .041 \sin \left(3 l^{\prime}-3 l^{\text {iv }}\right) \\
+0^{\prime \prime} .880 \sin \left(2 l^{\prime}-2 l^{\text {iv }}\right) & +0^{\prime \prime} .007 \sin \left(4 l^{\prime}-4 l^{\text {iv }}\right)
\end{array}
$$

due to the action of Jupiter. They are given at intervals of 2 days in the Argument IX. The constant added is $3^{\prime \prime} .35$.
Table XXI. contains the perturbations due to the action of Mercury. The formula has already been given at page 3. The tabulation is to double entry, the horizontal argument being l., and the vertical argument X., which remains constant during a period of Argument I. When Argument I. surpasses the limit of the table, $224^{4} .7$ should be subtracted from it, and 33.26 should be added to Argument X .; and if this last surpasses 60,60 may be subtracted from it. The constant added to the numbers, to render them positive, is $0^{\prime \prime} .85$.

Table XXII. contains the residnal perturbations due to the action of the Earth. The analytical expression is that given on page 3 with the omission of the terms which have been tabulated in Tables XIII., XV., XV1., XVIl., and XVIII. The tabulation is to double entry, the horizontal argument being I., and the vertical argument XI., which remains constant during a period of Argument I. When 224.7 is subtracted from Argument 1., 147.64 should be added to Argument XI.; and if this last exceeds 240,240 may be subtracted from it. The constant added to the numbers of this table is $1^{\prime \prime} .40$.

Table XXIII. contains the residual perturbations due to the action of Mars. The analytical expression is that given at page 4, with the omission of the terms which have been tabulated in Tables XIV. and XIX. The tabulation is to double entry, the horizontal argument being I., and the vertical argument XII., which remains constant during a period of Argument I. When $224^{d} .7$ is subtracted from Argument I., 19.6 must be added to Argument X11.; and if this last exeeeds 60,60 may be subtracted from it. The constant added to the numbers of this table is $0^{\prime \prime} .15$.

Table XXIV. contains the residual perturbations due to the action of Jupiter. The analytical expression is that given at page 4, with the omission of the terms which have been tabulated in Table XX. The tabulation is to double entry, the horizontal argument being I., and the vertical argument XIII., which remains constant during a period of Argument I. When $224^{4.7}$ is subtracted from Argument 1., 3.11 must be ạdded to Argument XIII.; aud if this last exceeds 60,60 may be subtracted from it. The constant added to the numbers of this table is $2^{\prime \prime} .35$.
'Iable XXV. contains the perturbations due to the action of Saturn. The analytical expression is given on page 4. 'The tabulation is to donble entry, the horizontal argunent being I., and the vertical argument XIV., which

## INTRODUCTION.

remains constant during a period of Argument 1. When $224^{4} .7$ is subtracted from Argument I., 0.8 must be added to Argument XIV., and if this last exceeds 36, 36 may be subtracted from it. The oonstant added to the numbers of this table is $0^{\prime \prime} .40$.

The preceding tables give tho Orbit Longitude of Venus referred to the mean equinox of date.
Table XXVI. contains the common logarithm of the Elliptic Radius Vector, for every tenth of a day of Arganent I. Its secular variation, corresponding to the fractional part of the anomalistic period is included. The formula tabulated is

$$
\begin{aligned}
& 9.85934275-0.0000257-0.00297187 \cos M \\
& -0.00001525 \cos 2 M-0.00000010 \cos 3 M \\
& +\frac{\text { Arg. I }-71^{\mathrm{d}} .7}{224^{\mathrm{d}} .7} \text { (quantity from Tab. XXVII). }
\end{aligned}
$$

The term 0.0000257 is equivalent to the sum of all the constants, which have been added in the tables of the periodic perturbations, in order to render the numbers always positive.

Tables XXVII.-XXXV. contain the perturbations of log. $r$; they are given uniformly in units of the eighth decimal ; and specially :-

Table XXVII. contains the factor of the secular perturbations for each day of Argument I. The quantity taken from this table must be multiplied by the integer $\mathbf{m}$. The logarithm of the factor is also given.

Table XXVIII contains the factor of that part of the secular perturbation which varies as the square of the time. It is given for intervals of 4 days in the Argument I. The quantity taken from this table must be multiplied by $\left(\frac{\mathrm{m}}{100}\right)^{2}$. The formula for the numbers of this table is $-2.1 \cos M$.

Table XXIX. contains the terms

$$
\begin{array}{ll}
-18.6 & -23.0 \cos \left(6 l^{\prime}-6 l^{\prime \prime}\right) \\
+228.2 \cos \left(l^{\prime}-l^{\prime \prime}\right) & -11.5 \cos \left(7 l^{\prime}-7 l^{\prime \prime}\right) \\
+998.6 \cos \left(2 l^{\prime}-2 l^{\prime \prime \prime}\right) & -6.4 \cos \left(8 l^{\prime}-8 l^{\prime \prime}\right) \\
-841.8 \cos \left(3 l^{\prime \prime}-3 l^{\prime \prime}+0^{\circ} 8^{\prime}\right) & -3.5 \cos \left(9 l^{\prime}-9 l^{\prime \prime}\right) \\
-145.2 \cos \left(4 l^{\prime \prime}-4 l^{\prime \prime}\right) & -2.6 \cos \left(10 l^{\prime}-10 l^{\prime \prime}\right. \\
-52.2 \cos \left(5 l^{\prime}-5 l^{\prime \prime}+0^{\circ} 20^{\prime}\right) &
\end{array}
$$

due to the action of the Earth. The constant added is 1594.
Table XXX. contains the term

$$
+162.2 \cos \left(4 l^{\prime \prime}-5 l^{\prime \prime}+88^{\circ} 52^{\prime}\right)
$$

due to the action of the Earth. The constant added is $\mathbf{1 6 2}$.
Table XXXI. contains the terms

$$
\begin{array}{ll}
-19.2 & -133.0 \cos \left(2 l^{\prime}-2 l^{\mathrm{iv}}\right) \\
+299.2 \cos \left(l^{\prime}-l^{\mathrm{iv}}+0^{\circ} 20^{\prime}\right) & -7.0 \cos \left(3 l^{\prime}-3 l^{\mathrm{iv}}\right)
\end{array}
$$

due to the action of Jupiter. The constant added is 445.
Table XXXII. contains the perturbations due to the action of Mercury. The formula has already been given on page 4. The constant added is 34 . The tabulation is to double entry, and the remarks which have been made with regard to Table XXI. also apply here.

Table XXXIII. contains the residual perturbations due to the action of the Earth. The formula is that given at page 4 with the omission of the terms which have been tabulated in Tables XXIX. and XXX. The constant added is 150 . The tabulation is to double entry, and the remarks made with regard to Table XXII. apply here.

Table XXXIV. contains the perturbations due to the action of Mars. The formula has been given at page 5 . The constant added is 80 . The tabulation is to double entry, and the remarks made with regard to Table XXIII apply here.

Table XXXV. contains the residual perturbations due to the action of Jupiter. The formula is that given on page 5, when the terms tabulated in Table XXXI. are omitted. The constant added is 80 . The tabulation is to double entry, and the remarks made with regard to Table XXIV. apply here.

Table XXXVI. contains the perturbations due to the action of Saturn. The formula has been given at page 5 .

## INTRODUCTION.

The constant added is $\mathbf{2 5}$. Tho tabulation is to double entry, and the remarks made with regard to Table XXV apply here.

These tables (XXVI.-XXXVI.) suflice for finding the lugarithm of the radius vector.
Tables XXXVII. and XXXVIII. contain the perturbations of the latitude expressed in units of hundredths of a second of are.

Table XXXVIl. contains the perturbations due to the action of the Larth. The formula has been given at page 5. The constant added is $0^{\prime \prime}$.62. The tabulation is to double entry, and the remarks made with regard to Table XXIl. apply here.

Table XXXVIII. contains the perturbations due to the action of Jupiter. The formula has been given at page 6. The constant added is $0^{\prime \prime} .21$. The tabulation is to double entry, and the remarks made with regard to Table XXIV. apply here.

The latitude of Venus is then obtained in the following way. The elliptic latitude is obtained from the formula $\log \sin ($ clliptic lat. $)=\log \sin i+\log \sin \left[\right.$ orbit long. $\left.+\left(360^{\circ}-\Omega\right)\right]$, is which the orbit longitude is corrected for perturbations. Then the true latitude is given by the formula
True Latitude $=$ Elliptic Latitude + the sum of the quantities derived from Tables XXXVII. and XXXVIII. $-0^{\prime \prime} 83$.*
Table XXXIX. contains, for the beginning of each year between $1750-1950$, the valucs of the quantitics $K_{x}$, $K_{y}, K_{z}, \log k_{x}, \log k_{y}, \log k_{z}$ and the Arguments XV. and XVI. on which depend respectively the lunar and solar nutation.

The beginning of the ycar for Arguments XV. and XVI. nust be understood as being the Washington mean noon of Jan. 0, (Jan. 1 in bissextile years, ). But the other six quantities of this Table are given for this time of the beginning ol' the year only for 1850 , and backwards and forwards from this epoch they proceed by intervals of a tropical year. This modification has been made, in order that the mution of these quantities for the fractional part of the year inight be included in 'Fable XL1. From each of the quantities $K_{x}, K_{y}$, and $K_{z}$, there has been subtracted the constant $20^{\prime \prime} .00$, and from $\log k_{y}$ the constant 0.0000089 , and from $\log k_{z}$ the constant 0.0000560 . These constants are equivalent, in each ease, to the sum of the constants which have been added to the quantities in Tables XL. and XLI. to render them positive. Moreover to $K_{x}$ laas been added the small correction, due to lunar nutation, over and above the lunar nutation itself; and to $\log k_{x}$ has been added the small correction due to lunar nutation.

Table XL. contains the variations of the quantities $K_{x}, K_{y}, K_{z}, \log k_{y}$, and $\log k_{z}$ which are produced by lunar nutation. The two last are expressed in units of the seventh decimal place. These quantities have all been conputed for the epoch 1850 , and are subject to small secular changes, which, except in the case of the correction of $K_{z}$, are barely sensible in the course of a century. The variation of $J K_{z}^{r}$ in a century has therefore been given in the adjacent column.

The constants which have been added to render the numbers positive, are $18^{\prime \prime} .00$ to $\Delta K_{x}, 18^{\prime \prime} .00$ to $\Delta K_{y}^{r}$, $17^{\prime \prime} .00$ to $\Delta K_{z}, 88$ units to $\Delta \log k_{y}, 430$ units to $\Delta \log k_{z}$. The lunar nutation of the equinox can be obtained from the value of $\Delta K_{x}$ by subtracting $18^{\prime \prime} .00$. The formulæ for the quantities tabulated are

$$
\begin{aligned}
& \Delta K_{x}=18^{\prime \prime} .00+\Delta \xi^{\prime} \\
& \Delta K_{y}=18^{\prime \prime} .00+1.0044 \Delta \psi^{\prime}+0.0690 \Delta \varepsilon \\
& \Delta K_{z}=17^{\prime \prime} .00+0.9498 \Delta \psi^{\prime \prime}+0.3323 \Delta \varepsilon
\end{aligned}
$$

sec. var. of $\Delta K_{z}=+0.0030 \Delta 3$, $\Delta \log k_{y}=88+0.5469 \Delta \psi-9.480 \Delta \varepsilon$, $\left.\Delta \log k_{x}=430-2.534 \Delta \psi+45.71\right\lrcorner \varepsilon$,
when for $\Delta \psi$ and $\Delta \varepsilon$ are substituted those parts of the values of these quantities given on page 6 which depend in $\delta \mathbb{C}$. The part of $\Delta K_{x}$ which has been applied to $K_{x}$ in Tibble XXX1X is

$$
+0.0015 \perp
$$

und the value of $\Delta \log k_{x}$ which has been added to $k_{x}$ in the sume Table is

$$
-0.0181\lrcorner \psi
$$

[^2]
## INTRODUCTION.

Table $\mathcal{N 1} 1$. contains the variations of the quantities $K_{x}, K_{y}, K_{z}, \log k_{y}$, and $\log _{g}{k_{z}}_{z}$ which are produced by solar nutation, angmented by the motion of the quatities in the fractional prort of the tropical year. $\perp \log k_{y}$, and $J$ log $l_{i}$, are expressed in units of the seventh decimal phace. The yuantities have been computed for the epoch 1850. The sceular variation $\lrcorner K_{z}$, becoming sensible in the course of a eentury, is given in the atjacent columu. The last column contains the solar mutation of the equinox. 'The constants which have been added are $\mathbf{Q}^{\prime \prime} .00$ to $\lrcorner K_{x}, 2^{\prime \prime} .00$ to $\lrcorner K_{y}, 3^{\prime \prime} .00$ to $\lrcorner K_{z}, 1$ unit to $\lrcorner \log k_{y}$, and 130 units to $\lrcorner \log k_{z}$. The formule for the quantities tabulated are,

$$
\begin{aligned}
& د K_{x}=2^{\prime \prime} .00+0^{\prime \prime} .05=+\perp \psi^{\prime}, \\
& \lrcorner K_{y}=2^{\prime \prime} .00+0^{\prime \prime} .126 \div+\right\rfloor 4^{\prime}+0^{\prime \prime} .038 \sin \left(2 \odot+98^{\circ} .2\right) \text {, } \\
& \left.\Delta K_{2}=3^{\prime \prime} .00-1^{\prime \prime} .864 \div+\right\rfloor \psi^{\prime}+0^{\prime \prime} .194 \sin \left(2 \odot+71^{\circ} .0\right) \text {, } \\
& \text { sec. var. } \perp K_{z}^{\prime}=+0^{\prime \prime} .019-\text {, } \\
& \lrcorner \log k_{y}=1+22.145 \div+5.3 \sin \left(2 \odot+263^{\circ} .5\right) \text {, } \\
& 4 \log k_{z}=130-103.110 t+25.4 \sin \left(2 \odot+83^{\circ} .8\right) \text {, }
\end{aligned}
$$

$\tau$ denoting the fraction of the year, and the value of $\lrcorner \xi^{\text {b }}$ being

$$
-1^{\prime \prime} .251 \sin 2 \odot
$$

The proper values of $K_{x}, K_{y}^{r}$ \&c., needed for computing the values of $x, y$, und $z$ referred to the true equinox and equator of date, are therefore obtained, by adding the quantities obtained from 'rables XL. and XLI. to the quantities given in Table XXXIX. for the beginning of the year. And there is no need of interpotation in this last Tible, except for $\log . k_{x}$, which however is nearly constant.

Table XLLII. contains the values of the factors by which the perturbation of the latitude, obtained from Tables XXXVII. and XXXVIII. by subtracting $0^{\prime \prime} .83$, and expressed in hundredths of a second of are, must be multiphed, in order to ubtain the corresponding corrections of the coürdinates $x, y$, and $z$ expressed in units of the seventh lecimal place. 'The Argument is the Orbit Longitude.

Table XLILI. contains the Parallax and Semidiameter. The Argument is the logarithm of the planet's distance from the Earth. The formula have already been given at page 8. The value of the semidiameter here given has still need to be increased by a constant quantity for the effect of irradiation, but varying for different observers and instruments, when the reduction of observations is in question.

Tables XLIV. and XLV. give the means of obtaining the mean longitude and arguments for a time not con. tained between the limits $1750-1950$.

Table XLIV. contains the quantities which must be added to the quantities of the $19^{u_{1}}$ century contained in Tables VI. and XXXIX., to obtain the mean longitude and arguments for the beginning of the corresponding year of any other century between 300 B . C. and 2300 A . D. The numbers in the columns headed $t^{\prime}-50$, must be multiplied by $\left(t^{\prime}-50\right), t^{\prime}$ denoting the number of years from the beginning of the century, and the products added to the numbers of the preceding column. In the case of $\log \sin i$, the numbers of the column headed $t^{\prime}-50$ must be understood as being in units of the last decimal place of $\log \sin i$. In using this Table for dates which are B. C. the given year must be conceived as increased algebraically by a unit. It will be noticed that two lines occur for the argument 1500: the first is for dates which are according to the Julian calendar (Old Style), and the sccond for those which are according to the Gregorian ealendar (New Style). The Julian calendar ends with Oct. 4, 1582 ; and the Gregorian begins with Oct. 15, 1582.
'Table XLV. contains the values of the inequality of the longitude to long period,

$$
+0^{\prime \prime} .282 \sin \left(4 l^{\prime \prime \prime}-7 l^{\prime \prime}+3 l^{\prime}+147^{\circ} .1\right)
$$

and of certain multiples of the period of the argument in years. As this inequality has been added to the numbers of the column headed $L$ in Table VI., we must enter the Table first with the argument equal to the corresponding year of the $19^{\text {th }}$ century and take the equation with the opposite sign; and next with the argument equal to the year of the given date, and take the corresponding equation: then both these quantities must be added to the $L$ resulting from the previous 'rables. If the year of the given date is not found in the limits of this Table, that multiple of the period of the argument, which is requisite, must be added to it or subtracted from it.

Table NLVI. contains the Reduction of the Orbit Longitude to the ecliptic. The Argument is the "Orbit Longitude $+360^{\circ}-\Omega "$, or this angle diminished by $180^{\circ}$ when it exceeds $180^{\circ}$. It is given for every $10^{\prime}$ of the

## INTRODUCTION.

Argument. The arraugement of the Table will be easily understoed. The Table is constructed for the epoch 1850.0, and the variation in a century, of the numbers tabulaterl, is given in the last column but one, for every degree. The formula for the reduction to the ecliptic is

$$
-180^{\prime \prime} .94 \sin 2\left(2+360^{\circ}-8\right)+0^{\prime \prime} .079 \sin 4\left(2+360^{\circ}-\delta\right)
$$

and for its secular variation

$$
-0^{\prime \prime} .113 \sin 2\left(\lambda+360^{\circ}-8\right)
$$

## DIRECTIONS FOR THE USE OF TIIE TABLES.

The given time must be reduced to Washington Mean Time lyy the aid of Table I. The hours, minutes and seconds cin then be redueed to the equivalent decimal part of a day by Table IV.; and the whole number of days which have elapsed since the begiming of the year can be found from Table III.

The values of the mean longitude $L$, mand the fourteen arguments of the perturbations are taken from Table VI. for the given year, if it lies between 1750 and 1949. If we do not want the heliocentric longitude and latitude of the planet, but intend to compute the geocentric coürdinates by the Gaussian process, the quantities, in the columns of this Table, headed Log. $\sin i$ and $360^{\circ}-\Omega$, will not be needed.

From Table VII. will be obtained the motion of $L$ from the beginning of the year to the given day; and also the fraction of the year; from 'lable IX. the factor which must be multiplied by the fraction of the year and the product added to $L$; and from Table VIII, the motion of $L$ for hours, minutes and seconds, or for decimal parts of a day. The quantities obtained from Tables VII.-IX. being added to the $L$ from Table VI., we obtain the tabular mean longitude of the planet for the given date.

To Arguments I.-IX., II. excepted, we add the number of days and decimal part of a day which have elapsed since the beginning of the year; to Argument II. we add the fractional part of the year. If any argument thus obtained, exceed its period given in Table V., we subtract as many multiples of the period as may be necessary to reduce it below its period. To the Argument an, we add as many units, as we have subtracted multiples of its period from Argument I., and to Arguments X.-XIV, we add severally the same number of multiples of the numbers $33.26,147.64,19.6,3.11$, and 0.8 . The values of these multiples are given in Table V. If any Argument X.-XIV, exceed its period given in Table V., we may subtract from it the largest contained multiple of its period.

The Equation of the Centre is obtained from Table $\boldsymbol{X}$. with the Argument I. The perturbations of the longitude in hundredths of a second of are will be obtained with the proper arguments from Tables XI.-XXV. Tho number obtained from Table XI. must be multiplied by the integer m, and the number from Table XII. by the factor $\binom{\mathrm{m}}{\mathrm{t} 00}^{2}$; the logarithms of the numbers in these two tables have also been given in the adjacent column, in order that, if preferred, the multiplication may bo performed by their aid. The Equation of the Centre and these perturbations being added to the mean longitude, we obtain the orbit longitude referred to the mean equinox of date.

The Logarithm of the Elliptic Radius Vector is obtained from Table XXVI, with the Argument I; and its perturbations, in units of the eighth decimal, with the proper arguments from Tables XXVII.- XXXVI. The number obtained from Table XXVII. must be multiplied by the integer rat, and the number from Table XXVIII. by the factor $\binom{\text { nin }}{100}^{2}$; the logarithm of the number is also given in Table XXVII., in order that, if preferred, the multiplication may be performed by its aid. If the sum of the numbers thus obtained from Tables XXVII.-XXXVI. be divided by 10, and the quotient be added to the last figures of the quantity obtained from Table XXVI., we shall have the common logarithm of the radius vector of the planet.

If we diminish by 83 the sum of the numbers, obtained from Tables XXXVII. and XXXVIII, with the proper arguments, we shatl have, in hundredths of a second of are, the perturbations of the latitude.

The values of $K_{x}, K_{y}$, \&cc, and Arguments XV. and XVl. are to be taken from Table XXXIX, for the given year. And to Arguments XV. and XVI. should be added the number of days and the decimal part of a day elapsed since the beginning of the year; and if Argument XV. exceed its period, given in Table V., the period

## INTRODUCTION.

should be subtracted from it. The corrections of $K_{x}, K_{y}, \& c$. , are obtained from Tables XL. and XLI., with the respective Arguments XV. and XVI. In the case of $K_{\mathrm{z}}$ in each Table, the variation in 100 years, given in the adjacent column, must be taken into account; we multiply it by the fractional part of the century elapsed since 1850 , and add the product to the quantity obtained from the preceding column. These corrections being added to the values of $K_{x}, K_{y}$, \&c., obtained without interpolation from Table XXXIX., we have the proper values of these quantities for computing the rectangular coördinates of the planet referred to the true equinox and equator of date.

If $r$ denote the radius vector, and $\lambda$ the orbit longitude of the planet, these coördinates are obtained by the formulæ

$$
\begin{aligned}
& x=k_{\mathrm{x}} r \sin \left(\lambda+K_{\mathrm{x}}\right), \\
& y=k_{\mathrm{y}} r \sin \left(\lambda+K_{y}\right), \\
& z=k_{\mathrm{z}} r \sin \left(\lambda+K_{z}\right) .
\end{aligned}
$$

The values of the coördinates thus found need correction for the effect of perturbations in latitude. To obtain these corrections we multiply the perturbations of the latitude, expressed in hundredths of a second of arc, respectively by the three factors obtained from Table XLII. with the argument $\lambda$, and the products are the respective corrections of the coördinates expressed in units of the seventh decimal.

If $X, Y$ and $Z$ denote the coördinates of the Sun referred to the same system of planes as $x, y$ and $z$, the geocentric right ascension $\alpha$, declination $\delta$, and distance from the Earth $\Delta$, of the planet, are obtained from the equations,

$$
\begin{aligned}
& \Delta \cos \alpha \cos \delta=x+X \\
& \Delta \sin \alpha \cos \delta=y+Y \\
& \Delta \sin \delta \quad=z+Z
\end{aligned}
$$

The $\alpha$ and $\delta$ thus obtained have still to be corrected for aberration, if we desire the apparent position of the planet. The aberration time $T$ in days is given by the equation

$$
\log T=7.76052+\log \Delta ; \text { or, } T=.005761 \Delta
$$

If $\frac{d \alpha}{d t}$ and $\frac{d \delta}{d t}$ denote the daily variation of $\alpha$ and $\delta$ at the given date, the corrections for aberration are

$$
\begin{aligned}
& \Delta \alpha=-T \frac{d \alpha}{d t} \\
& \Delta \delta=-T \frac{d \delta}{d t}
\end{aligned}
$$

Finally, from Table XLIII., we can obtain, with the argument $\log \Delta$, the parallax and semidiameter of the planet.

If we desire to have the heliocentric longitude and latitude, we take from Table VI. the values of $\log$. $\sin i$ and $360^{\circ}-\Omega$ for the given year. The motion of $360^{\circ}-\Omega$ for the fraction of the year is given in Table VII.; that of $\log \sin i$ can readily be inferred from Table VI. Then if the latitude be computed from the equation,

$$
\log \sin \text { lat. }=\log \sin i+\log \sin \left(\lambda+360^{\circ}-8\right)
$$

and the perturbations of the latitude, which have already been obtained, be added to it, we shall have the heliocentric latitude required. The ecliptic heliocentric longitude, referred to the mean equinox of date, will be got by adding to $\lambda$ the reduction to the ecliptic, from Table XLVI. As the value of the reduction, given in the body of the Table, is for the epoch 1850, we must apply to it the variation in 100 years multiplied by the fraction of a century elapsed since 1850. The heliocentric longitude referred to the true equinox of date will be found by adding the nutation of the equinoxes in longitude. The lunar nutation will be obtained by subtracting $18^{\prime \prime}$ from $\Delta K_{\mathrm{x}}$ in Table XL.; the solar nutation is given in the last column of Table XLI.
$x, y$, and $z$ may then be obtained by the formulæ

$$
\begin{aligned}
& x=r \cos l \cos \lambda^{\prime} \\
& y=r \cos l \sin \lambda^{\prime} \cos \varepsilon^{\prime}-r \sin l \sin \varepsilon^{\prime} \\
& z=r \cos l \sin \lambda^{\prime} \sin s^{\prime}+r \sin l \cos \varepsilon^{\prime}
\end{aligned}
$$

in which $\lambda^{\prime}$ and $l$ are the heliocentric longitude and latitude, and $\varepsilon^{\prime}=\varepsilon+\Delta \varepsilon$, the apparent obliquity of the ecliptic.

## INTRODUCTION.

If the given year is not between the limits $\mathbf{1 7 5 0 - 1 9 4 9}$, we take from Tables VI. and XXXIX, the values of $L$, nm , the Arguments I.- XVI., $\log \sin i$ and $360^{\circ}-\delta$, for the corresponding year of the $19^{\text {th }}$ century, (remembering to add algebraically a unit to the year if the given date is before the Christian era.)

We add to these the quantitics obtained from Table XLIV., with the given century as the Argument. Moreover we add to $L, I, \log \sin i$ and $360^{\circ}-\delta$ respectively the quantities given in the adjacent columns, headed $t^{\prime}-50$, multiplied by this factor, ( $t^{\prime}$ denotiug the number of years of the given century,) noticing that in the case of $\log \sin i$, the quantities in the column headed $t^{\prime}-50$ are in units of the last decimal of this quantity. It will be observed that the argument 1500 occurs twice in Table XLIV.; the first line is to be employed for dates in old style, the second for dates in new style.

After this, we proceed precisely as before, except that Table VIII. not being available, we employ in its stead Table XLV., which we enter twice, first with the corresponding year of the $19^{\text {th }}$ century as the argument, and subtractiug from $L$ the equation obtained; next with the given year, as the argument, or this augmented or diminished by the requisite number of multiples of the period, which will be found at the bottom of the Table; and adding to $L$ the equation thus obtained.

In this case, we must necessarily deduce the heliocentric longitude and latitude of the planet, since the tables for finding $K_{x}, K_{y}$, \&c., are restricted to the years 1750 - 1919. The method of computing by rectangular courdinates is only to be preferred when we have the coördinates of the sun ready at hand.

In eomputing an ephemeris we shall avoid the horizontal interpolation in the tables to double entry, if, instead of computing the perturbations, for the Washington Mean Noon of some particular day, and for equal intervals thereafter, we compute the value of the perturbations, for the times, when Arg. I. is an exact multiple of 8 clays, and then the interpolation, with reference to Arg. I., can be performed on the sums. It will be found that the interval of 8 days is not too long for the secure interpolation of intermediate values. However, if en should be quite large, that is, if the given time is quite distant from 1850, the terms of the perturbations, which iavolve this factor, may be computed separately, for the times, for which, the ephemeris is wanted. In all eases, the interpolation of the sums of the perturbations, to the times of the ephemeris, will be easier, if these sums are first interpolated into the middle, that is, for every 4 days. In the computation of an isolated position even, this method of obtaining the perturbations, first for the times when Arg. I. is a multiple of 8 days, can be followed with advantage, at least as far as regards the tables to double entry.

The following examples will sufficiently illustrate the foregoing precepts:-

1. Required in ephemeris of the heliocentric position of Venus, for Washington Mean Noon, at intervals of 2 days, and covering the time of the Transit on Dec. $8^{\text {th }}, 1874$.

We will commence the calculation of the perturbations at $310^{2} .3195$ from the beginning of the year $=$ Nov. $6^{4} .3195$, when the value of Argument $I$ is $160^{4}$.

Preparation of the Arguments.


## INTRODUCTION.

|  | X. | XI. | XII. | XII | XIV. | XV. | XVI. |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Table VI., 1874, | 42.20 | 17.72 | 53.0 | 27.03 | 30.6 | 6005.2 | 1.8 |
| Table V., Incr. of $\mathbf{m}=1$, | 33.26 | 147.64 | 19.6 | 3.11 | 0.7 | 310.0 | 310.0 |
| Periods, | -60.00 |  | -60.0 |  |  |  |  |
| Arguments for Date, | 15.46 | 165.36 | 12.6 | 301.4 | 31.3 | 6315.2 | 311.8 |

Perturbations of the Longitude, in hundredths of a second.


Note.-The inequality from Table XII. is insensible at this epoch, as is also the corresponding one of Log. $r$ in Table XXVIII

Perturbations of Log $r$, in units of the eighth decimal.

| Arg. I. | 160 | 168 | 176 | 184 | 192 | 200 | 208 | 216 | 224 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Table XXVII | $-133$ | $-15$ | +104 | +219 | $+323$ | $+411$ | $+478$ | $+522$ | +538 |
| Table XXIX | 2146 | 1989 | 1850 | 1753 | 1716 | 1748 | 1841 | 1978 | 2136 |
| Table XXX | 292 | 309 | 320 | 324 | 321 | 311 | 295 | 274 | 248 |
| Table XXXI | 17 | 66 | 141 | 236 | 339 | 440 | 528 | 594 | 636 |
| Table XXXII . | 50 | 46 | 36 | 24 | 13 | 9 | 9 | 12 | 11 |
| Table XXXIII | 231 | 221 | 214 | 210 | 211 | 216 | 224 | 235 | 245 |
| Table XXXIV | 85 | 70 | 57 | 46 | 36 | 29 | 23 | 20 | 19 |
| Table XXXV . | 140 | 134 | 125 | 112 | 99 | 85 | 73 | 65 | 60 |
| Table XXXVI | 36 | 32 | 27 | 22 | 17 | 11 | 6 | 3 | 0 |
| Sums | 2864 | 2852 | 2874 | 2946 | 3075 | 3260 | 3477 | 3703 | 3893 |

Perturbations of the Latitude, in hundredths of a second.


## INTRODUOTION.

Interpolating the perturbations of the longitude and $\log r$ to intervals of 4 days, we have,

| Arg. I. | Pert. of the Long. | Diff. | Pert of $\log r$. | Diff. | Arg. | Pert. of the Long. | Diff. | Pert. of $\log r$. | Diff. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 160 | 42.65 |  | 2864 |  | 192 | 41.13 |  | 3075 |  |
| 161 | 42.47 | - 18 | 2855 |  | 196 | 40.72 | - 41 | 3162 | + |
| 168 | 42.31 | 16 | 2852 | - 3 | 200 | 40.19 | 53 | 3260 |  |
| 17: | 42.18 | 13 | 2858 | +6 | 201 | 39.54 | 65 | 3365 | 105 |
| 176 | 42.01 | 14 | 2874 | 16 | 208 | 38.75 | 79 | 3477 | 112 |
| 180 | 41.89 | 15 | 2903 | 29 | 212 | 37.80 | 95 | 3592 | 11 |
| 181 | 41.70 | 19 | 2946 | 43 | 216 | 36.72 | 108 | 3703 | 11 |
| 188 | 41.45 |  | 3003 | 57 | 2:0 | $3 \overline{5} .50$ | 122 | 3804 | 10 |
| 19: | 41.13 | - 32 | 3075 | +72 | 221 | 34.17 | -133 | 3893 | + |

The Orbit Longitude and Log. r. Washington Mean Noon.

| $\begin{aligned} & \text { Date. } \\ & 1>74 . \end{aligned}$ | $\begin{array}{\|l} \text { Diay of } \\ \text { Year. } \end{array}$ | Arg. 1. | $\begin{aligned} & \text { Mean Longitude } \\ & \text { from Tables } \\ & \text { V1.-V11I. } \end{aligned}$ | Equa. of the Centre from Table X. | Pert. of the long. | Orbit Long. | Log. Elliptie $r$ from Table xxvi. | Pert. of Log. $r$. | Log. $r$. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Dec. 3 | $337^{4}$ | 186.6505 | $68 \quad 3 \quad 8.37$ | ${ }^{\prime} 45.10$ | 41.54 | $68^{\circ} \quad 9 \quad 35^{\prime \prime} .11$ | 9.8578827 | 298 | 9.857912 |
|  | 339 | 188.6505 | $71 \quad 15 \quad 23.98$ | 75.00 | 41.40 | 712310.38 | 9.8577382 | 301 | 9.857768 |
| 7 | 341 | 190.6505 | 742739.59 | 832.38 | 41.24 | 743653.21 | 9.8575986 | 305 | 9.857629 |
| 9 | 313 | 192.6505 | 773955.21 | $10 \quad 7.11$ | 41.07 | 775043.39 | 9.8574644 | 309 | 9.857495 |
| 11 | 345 | 194.6505 | 805210.82 | 1148.87 | 40.87 | 81440.56 | 9.8573358 | 313 | 9.857367 |
| 13 | 317 | 196.6505 | $84 \quad 426.44$ | 1337.36 | 40.64 | 841844.44 | 9.8572135 | 318 | 9.857215 |

Inequalities of $\boldsymbol{K}_{\mathrm{x}}, \boldsymbol{K}_{\boldsymbol{y}}, \& c$.

| Day of Year. | $\Delta K_{x}$. |  |  | $\Delta K_{\mathrm{y}}$. |  |  | $\Delta I_{\text {z }}$. |  |  | $\Delta \log k_{y}$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { Table } \\ & \text { NL. } \end{aligned}$ | $\begin{aligned} & \text { Table } \\ & \text { XII. } \end{aligned}$ | Sum. | $\begin{aligned} & \text { Table } \\ & \text { XL } \end{aligned}$ | $\begin{aligned} & \text { Table } \\ & \text { XLI. } \end{aligned}$ | Sum. | $\begin{aligned} & \text { Table } \\ & \text { XL. } \end{aligned}$ | Table <br> XLI. | Sum. | $\begin{aligned} & \text { Table } \\ & \text { XL. } \end{aligned}$ | $\begin{aligned} & \text { Table } \\ & \text { XLI. } \end{aligned}$ | Sum. |
| $310{ }^{\text {a }}$ | 10.68 | 0.78 | 11.46 | 11.23 | ${ }^{\prime \prime} .83$ | 12.06 | 12.81 | ${ }_{0}^{\prime \prime} 21$ | 13.05 | 5 | 19 | 24 |
| $3: 0$ | 10.82 | 0.85 | 11.67 | 11.37 | 0.90 | 12.27 | 12.96 | 0.19 | 13.15 | 5 | 21 | 26 |
| 330 | 10.96 | 1.07 | 12.03 | 11.52 | 1.11 | 12.63 | 13.11 | 0.28 | 13.39 | 5 | 23 | 28 |
| 340 | 11.11 | 1.39 | 12.50 | 11.66 | 1.42 | 13.08 | 13.26 | 0.49 | 13.75 | 4 | 25 | 29 |
| 350 | 11.25 | 1.80 | 13.05 | 11.81 | 1.83 | 13.64 | 13.40 | 0.80 | 14.20 | 4 | 27 | 31 |
| 360 | 11.40 | 2.26 | 13.66 | 11.95 | 2.30 | 14.25 | 13.55 | 1.19 | 14.74 | 4 | 28 | 32 |
| 370 | 11.51 | 2.68 | 14.2: | 12.10 | 2.72 | 14.82 | 13.70 | 1.57 | 15.27 | 3 | 28 | 31 |


| Day of Year | $\Delta \log k_{z}$. |  |  | $K_{x}$. | $K_{\text {y }}$. | $K_{\text {g }}$. | $\log k_{x}$. | Log $k_{\mathrm{y}}$. | $\log k_{z}$. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} \text { Table } \\ \text { XL. } \end{gathered}$ | $\begin{aligned} & \text { Table } \\ & \text { XlI. } \end{aligned}$ | Sum. |  |  |  |  |  |  |
| $3110^{\text {a }}$ | 828 | 46 | 874 |  | 127 ²'.22 | $352^{\circ} 44{ }^{\prime} 25.01$ | 9.9992854 | 9.9598380 |  |
| 320 | 829 | 34 | 863 | 24.11 | - 22.43 | 352 25.11 | 2.9392854 | 9.9598380 82 | $\begin{aligned} & 9.135 \\ & 424 \end{aligned}$ |
| 330 | 830 | 23 | 853 | 24.47 | 22.79 | 25.35 | 4 | 84 | 414 |
| 310 | 831 | 14 | 845 | 24.94 | 23.24 | 25.71 | 4 | 85 | 406 |
| 350 | 833 | 7 | 840 | 25.49 | 23.80 | 26.16 | 4 | 87 | 401 |
| 360 | 831 | 3 | 837 | 26.10 | 24.41 | 26.70 | 4 | 88 | 398 |
| 370 | 835 | 2 | 837 | 26.66 | 24.98 | 27.23 | 4 | 87 | 398 |

## INTRODUCTION.

Computation of the Rectangular Coördinates.

| Date, 1874. | $\lambda+K_{x}$. | $\lambda+K_{y}$. | $\lambda+K_{2}$. | $\log k_{x} \sin \left(\lambda+K_{x}\right)$. | $\log k_{y} \sin \left(\lambda+K_{y}\right)$. | $\log k_{z} \sin \left(\lambda+K_{2}\right)$. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Dec. 3 | 158 ¢ 7 ¢ 59.90 | $69^{\circ} 3666^{\prime \prime} 58.20$ | $60^{60} 544^{\prime \prime} \quad 0.70$ | 9.5703515 | 9.9317544 | 9.5593398 |
| 5 | 1612135.27 | 725033.57 | $\begin{array}{llll}64 & 7 & 36.05\end{array}$ | 9.5039252 | 9.9400684 | 9.5720679 |
| 7 | $16435 \quad 18.20$ | $\begin{array}{llll}76 & 4 & 16.50\end{array}$ | 672118.96 | 9.4237611 | 9.9468769 | 9.5830998 |
| 9 | $\begin{array}{llll}167 & 49 & 8.49\end{array}$ | $\begin{array}{llll}79 & 18 & 6.79\end{array}$ | $\begin{array}{llll}70 & 35 & 9.22\end{array}$ | 9.3235684 | 9.9522237 | 9.5925170 |
| 11 | $\begin{array}{llll}171 & 3 & 5.76\end{array}$ | $\begin{array}{llll}82 & 32 & 4.07\end{array}$ | $\begin{array}{llll}73 & 49 & 6.48\end{array}$ | 9.1911412 | 9.9561415 | 9.6003850 |
| 13 | $\begin{array}{llll}174 & 17 & 9.75\end{array}$ | $\begin{array}{llll}85 & 46 & 8.06\end{array}$ | $\begin{array}{llll}77 & 3 & 10.45\end{array}$ | 8.9973798 | 9.9586533 | 9.6067565 |
| Date, 1874. | $\log x$. | $\log y$. | $\log z$. | $x$. | $y$. | $z$ |
| Dec. 3 | 9.4282640 | 9.7896669 | 9.4172523 | $+0.2680798$ | +0.6161223 | $+0.2613680$ |
| 5 | 9.3616935 | 9.7978367 | 9.4298362 | 0.2299818 | 0.6278223 | 0.2690520 |
| 7 | 9.2813902 | 9.8045060 | 9.4407289 | 0.1911570 | 0.6375379 | 0.2758855 |
| 9 | 9.1810637 | 9.8097190 | 9.4500123 | 0.1517273 | 0.6452366 | 0.2818463 |
| 11 | 9.0485083 | 9.8135086 | 9.4577521 | 0.1118171 | 0.6508915 | 0.2869142 |
| 13 | 8.8546251 | 9.8158986 | 9.4640018 | +0.0715525 | +0.6544833 | +0.2910729 |

TABLE XLII.

2. Required the heliocentric longitude and latitude and the logarithm of the radius vector of Venus for 1769 , June $3^{\mathrm{d}} 10^{\mathrm{h}} 10^{\mathrm{m}}$ Paris mean time.

This is equivalent to June $3^{\mathrm{d}} 4^{\mathrm{h}} 52^{\mathrm{m}} 26^{\mathrm{s}} .98$ Washington mean time $=154^{\mathrm{d}} .20309$ from the beginning of the year.

Preparation of the Arguments.


## INTRODUCTION.

## Mean Longitude.



Table VIII., $1769,\left(-0^{\prime \prime} .015 \times 0.4\right)=\frac{-0.006}{252 \quad 041.40}$
Mean Longitude,

## Longitude.

| Mean Longitude |  |  |  | ${ }_{0}{ }^{\prime} 411.40$ |
| :---: | :---: | :---: | :---: | :---: |
| Equation of the Centre |  |  | 1 | 2539.70 |
| Table XI., $-10.363 \times(-131)$ |  |  |  | $\pm 13.57$ |
| Table XII., $+1.66 \times(-1.31)^{2}$ |  |  |  | + 0.03 |
| Table XIII., |  |  |  | 4.66 |
| Table XIV., |  |  |  | 0.32 |
| Table XV., |  |  |  | 1.12 |
| Table XVI., |  |  |  | 4.45 |
| Table XVII., |  |  |  | 16.68 |
| Table XVIII, |  |  |  | 2.05 |
| Table XIX., |  |  |  | 1.21 |
| Table XX., |  |  |  | 2.93 |
| Arg. I., | 72 | 80 |  |  |
| Table XXI., | 82 | 80 |  |  |
| Table XXII., | 145 | 150 |  |  |
| Table XXIII., | 10 | 8 |  |  |
| Table XXIV., | 310 | 308 |  |  |
| Table XXV., | 15 | 17 |  |  |
| Sums | 562 | 563 |  |  |
| Interpolated, |  |  |  | 5.63 |
| Grbit Longitude, |  |  | 253 | 2713.75 |
| Red. to Ecliptic, Table XLVI., |  |  |  | +7.26 |
| Lunar Nutation, Table XL., |  |  |  | +17.29 |
| Solar Nutation, Table XLI., |  |  |  | $-0.68$ |
| Heliocentric Longitude, |  |  | 253 | 2737.62 |


| Mean Longitude |  |  |  | ${ }_{0}{ }^{\prime} 41{ }^{\prime \prime} .40$ |
| :---: | :---: | :---: | :---: | :---: |
| Equation of the Centre |  |  | 1 | 2539.70 |
| Table XI., $-10.363 \times(-131)$ |  |  |  | $\pm 13.57$ |
| Table XII., $+1.66 \times(-1.31)^{2}$ |  |  |  | + 0.03 |
| Table XIII., |  |  |  | 4.66 |
| Table XIV., |  |  |  | 0.32 |
| Table XV., |  |  |  | 1.12 |
| Table XVI., |  |  |  | 4.45 |
| Table XVII., |  |  |  | 16.68 |
| Table XVIII, |  |  |  | 2.05 |
| Table XIX., |  |  |  | 1.21 |
| Table XX., |  |  |  | 2.93 |
| Arg. I., | 72 | 80 |  |  |
| Table XXI., | 82 | 80 |  |  |
| Table XXII., | 145 | 150 |  |  |
| Table XXIII., | 10 | 8 |  |  |
| Table XXIV., | 310 | 308 |  |  |
| Table XXV., | 15 | 17 |  |  |
| Sums | 562 | 563 |  |  |
| Interpolated, |  |  |  | 5.63 |
| Crbit Longitude, |  |  | 253 | 2713.75 |
| Red. to Ecliptic, Table XLVI., |  |  |  | +7.26 |
| Lunar Nutation, Table XL., |  |  |  | +17.29 |
| Solar Nutation, Table XLI., |  |  |  | $-0.68$ |
| Heliocentric Longitude, |  |  | 253 | 2737.62 |

## INTRODUCTION.

Encke's reduction of the observations of the Transit of Venus in 1769 gives $253^{\circ} 27^{\prime} 13^{\prime \prime} .17$ and $+0^{\circ} 4^{\prime} 4^{\prime \prime} .56$ as the orbit longitude and latitude.* But according to the Tables du Soleil of Hansen and Olufsen, the longitude and latitude of the Sun, adopted by Encke, must be corrected, respectively, by $+0^{\prime \prime} .64$ and $+0^{\prime \prime} .04$. Thus we may adopt $253^{\circ} 27^{\prime} 13^{\prime \prime} .81$ and $+0^{\circ} 4^{\prime} 4^{\prime \prime} .52$ as the values given by observation, and the residuals, Obs. - Cal., are respectively $+0^{\prime \prime} .06$ and $-0^{\prime \prime} .38$.

If Encke's reduction of the Transit of 1761 is compared with the Tables, in the same way, the residuals will De found to be $-0^{\prime \prime} .33$ and $+0^{\prime \prime} .40$.
3. Required the heliocentric position of Venus for 1639 , Dec. $4^{\mathrm{d}} 3^{\mathrm{h}} 44^{\mathrm{m}} 55^{\mathrm{s}}$ Paris mean time.

This time is equivalent to Dec. $3^{\mathrm{d}} 22^{\mathrm{h}} 27^{\mathrm{m}} 21^{\mathrm{s}} .98$ Washington mean time $=337^{\mathrm{d}} .93567$ from the beginning of the year.

Preparation of the Arguments.

|  | m | 1. | 11. | III. | IV. | V. | VI. | VII. | VIII. | IX. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Table VI., 1839 | $-18$ | 98.2956 | 156.9 | 7786 | 2358 | 1108.9 | 303.49 | 196.3 | 138.7 | ${ }^{\text {d }}$ |
| Table XLIV, 1600. | $-326$ | 204.4585 | 38.9 | 10863 | 932 | 1153.7 | 526.09 | 144.6 | 180.0 | 182.50 |
| Ferms $\times\left(t^{\prime}-50\right)$, |  | +0.0005 337.9357 | 0.9 | 338 | 338 | 337.9 | 337.94 | 337.9 |  |  |
| Periods, . | $+2$ | -449.4016 | 0.9 | -11987 | -2959 | -1454.9 | -583.92 | -486.3 | -440.1 | 337.94 -473.98 |
| Arguments for date, | -342 | 191.2887 | 196.7 | 7000 | 669 | 1145.6 | 583.60 | 192.5 | 216.5 | 112.85 |


|  | X . | X1. | XII. | XIII. | XIV. | $\log \sin i$. | $360^{\circ}-8$. | XV. | XVI. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Tables VI., XXXIX, } \\ & 1839 \end{aligned}$ | 6.46 | 1.97 | 14.4 | 29.66 | 23.7 | 8.7721999 | $28446{ }^{\prime \prime} \quad 4.6$ | 19.4 | ${ }_{1.3}^{\text {d }}$ |
| Table XLIV., 1600 | 17.69 | 107.80 | 22.2 | 5.56 | 6.9 | $-0.0002732$ | +14817.0 | 1732.9 | +0.4 |
| Terms $\times\left(t^{\prime}-50\right)$, |  |  |  |  |  | -24 | - 0.6 |  |  |
| Day of Year, or Periods Periods | 6.52 | 55.29 | $\begin{array}{r} 39.3 \\ -60.0 \end{array}$ | 6.22 | 1.5 | +12 | 30.1 | 337.9 | 337.9 |
| Arguments for date, | 30.67 | 165.06 | 15.9 | 41.44 | 32.1 | 8.7719255 | 2863350.9 | 2090.2 | 339.6 |

## Mean Longitude.

Table VI., 1839
Table XLIV., 1600 ,
Term $\times\left(t^{\prime}-50\right)$,
Table VII., Dec. 3,
Table IX., $22^{\text {h }}$,
" " $27^{\mathrm{m}}$,
" " $21^{\mathrm{s} .98}$,
Table XLV., 1839.9 with opp. sign,
" $\quad$ " $1942.3=1639.9+302.4$,
Mean Longitude,
$L$.

- , "
$285 \quad 5948.72$
3244655.79
$+0.458$
1795551.07
$128 \quad 7.157$
148.146
1.466
$-0.176$
$-0.279$
721232.35

[^3]
## INTRODUCTION.

## Longitude.



If Encke's reduction of Horrox's observations of the Transit at this time be corrected to conform with the position of the Sun as derived from Hansen and Olufsen's Tables, the residuals of the orbit longitude and heliocentric latitude are found to be respectively $+11^{\prime \prime} .4$ and $-18^{\prime \prime} .9$.

## INTRODUCTION.

## CORRECTION OF THE ELEMENTS OF THE ORBIT OF VENUS.

The Elements, adopted for comparison with observation, are, in the main, those on which Leverrier has based his Tables.

They are-

$$
\begin{aligned}
& \text { Epoch, 1850, Jan. 1.0, Paris Mean Time. } \\
& \qquad \begin{array}{c}
\circ \\
L^{\prime}=25
\end{array} 3^{\prime} \quad 14.70 \\
& \pi^{\prime}=1292714.5 \\
& 8^{\prime}=751952.3 \\
& i^{\prime}=32334.83 \\
& e^{\prime}=0.00684331 \\
& n^{\prime}= \\
& \hline 106641^{\prime \prime} .3831
\end{aligned}
$$



The value of $n^{\prime}$ has been changed in order to make the adopted tropical motion coincide with Leverrier's value. The values of the disturbing masses, and, in fact, of all the constants needed in the theory, are, with two exceptions, those given in the Introduction. But the annual tropical motion of the node at the epoch 1850 employed is $32^{\prime \prime} .2931$ as it results from the adopted values of the planetry masses : and the true longitude of the Sun is derived from the apparent longitude of Hansen's and Olufsen's Tables du Soleil by subtracting the effect of aberration corresponding to the constant $20^{\prime \prime} .255$.

All the elements, except the mean motion, are determined, with nearly all the precision possible by the modern observations; that is to say, those comprehended in the interval from 1836 up to the present time. The addition of the observations made previously to 1836 to the discussion, would scarcely increase this precision. For the mean motion we must employ ancient observations; and for this purpose it seems better to depend on the data furnished by the Transits of 1761 and 1769 , than on the somewhat uncertain observations of Bradley.

Encke's reduction of these Transits, corrected to conform with the positions of the Sun derived from the Tables du Soleil, will be adopted. All the longitudes mentioned here are referred to the mean equinox of date.

For the Transit of 1761 Encke gives


But the Tables du Soleil give $75^{\circ} 35^{\prime} 52^{\prime \prime} .05$ and $+0^{\prime \prime} .53$ as the longitude and latitude of the Sun. Consequently the adopted position of Venus is

|  | $\quad \circ$ | $\prime$ | $\prime \prime$ |
| :--- | :--- | :--- | :--- |
| Orbit Longitude | $=$ | $5^{\prime} 35$ | 36.90 |
| Heliocentric Latitude | $=$ | -345.84. |  |

For the Transit of 1769, Encke gives

$$
\begin{aligned}
& \text { Paris Mean Time }=1769 \text {, June } 3^{\mathrm{d}} 10^{\mathrm{h}} 10^{\mathrm{m}} \text {. } \\
& \text { True Longitude of the Sun }=7327^{\prime} 13.8 \text {, } \\
& \text { Latitude of the Sun } \quad=\quad 0.0 \text {, } \\
& \text { Orbit Longitude of Venus }=25327 \text { 13.17, } \\
& \text { Heliocentric Latitude of Venus }=\quad+44.56 .
\end{aligned}
$$

The Tables $d u$ Soleil give $73^{\circ} 27^{\prime} 14^{\prime \prime} .25$ and $+0^{\prime \prime} .04$ as the longitude and latitude of the Sun. Consequently the adopted position of Venus is

| Orbit Longitude of Venus | $=$ | 253 | $\circ$ |
| :--- | ---: | ---: | ---: |
| $27^{\prime}$ | 13.62, |  |  |
| Heliocentric Latitude of Venus $=$ | +4 | 4.52. |  |

## INTRODUCTION.

The meridian observations have been corrected to conform with the constant $8^{\prime \prime} .818$ of solar parallax, and to the following expression for the semi-diameter:

$$
\frac{8^{\prime \prime} .516}{\Delta}+0^{\prime \prime} .57
$$

In other respeets Leverrier's reduction has been adopted. With regard to the Greenwich and Paris observations which have accumulated since Leverrier made his investigation, that is, from 1858 forward, as, on comparing the places, given in the several annual volumes, for the fundamental time-stars, with Dr. Gould's Standard Places, $\mathcal{S} \cdot$., no sensible average diflerence in the right ascensions could be discovered, no correction for difference of equinoxes has been applied to them. To the Washington observations in deelination in the years 1866,1867 , has been applied the correction $+0^{\prime \prime} .75$. (See W'ashington Observations for 1867 , Appendix III., pp. 20, 21.)

In forming the following normals, Paris observations have been combined with Greenwich; but Washington ubscrvations have been kept separate. The normals, formed from them, are those given for Washugton Mean Noon. The Paris Observations used are not in great number, and belong to the years 1838 and 1856-1866. The comparisons are Obs. - Cal.

Normals in the inferior part of the Orbit.


INTRODUCTION.

| No. | Greenwich M. 'T\% |  |  | App. J. A. | App. Dec. | No. Obs. | $\triangle n$ | $\triangle \delta$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 17 | 185\%, | June | $26.0$ | $3^{11} \because 0^{112}+19.536$ | + $11^{\circ} 16^{\prime} \cdot 16^{\prime \prime} 18$ | 12 | +0.081 | + ${ }^{\prime \prime} .07$ |
| 48 | 1858, | Aug. | 17.0 | $12: 2181.3: 1$ | - 21032.51 | 9 | -0.139 | +1.03 |
| 49 |  | Sejpr. | 18.0 | 113157.511 | - 172117.16 | 4 | -0.0.58 | -1.56 |
| 50 |  | Oct. | 10.0 | 16 ご 1.666 | - 214217.26 | 10 | - 0.086 | - 0.62 |
| 5 |  | Nov. | 7.0 | 173719.017 | -28 151.96 | 11 | +0.0.0 | -3.24 |
| 52 |  | Nov. | 29.0 | $175.5 \quad 9.651$ | -25 3131.11 | 3 | +0.311 | $-4.70$ |
| 53 |  | Dec. | 21.0 | $\begin{array}{llll}17 & 752.455\end{array}$ | - 20 1 43.16 | 4 | +0.203 | -2.23 |
| 5 | 1859, | Jith. | 10.0 | 165827.618 | - 1721 2 38.11 | 7 | +0.051 | +3.60 |
| 55 |  | Jan. | 29.0 | 174025.353 | - 18208201 | 8 | +0.138 | +0.17 |
| 5 ) | 1860, | May | 3.0 | 5) 5318.56 .1 | +2636 37.27 | 4 | +0.031 | +1.43 |
| 57 |  | May | $2: 3.0$ | $716 \quad 2.843$ | +25 2336.95 | 5 | +0.012 | +1.53 |
| 58 |  | June | 19.0 | 82355.823 | +195830.41 | 5 | +0.103 | +2.43 |
| 59 |  | July | 10.0 | 81115.899 | +16 82 2.57 | 6 | +0.103 | +2.50 |
| 60 |  | Aug. | 31.0 | 74810.699 | + 162114.53 | 7 | +0.203 | +0.18 |
| 61 |  | Sept. | $\geq 2.0$ | $\begin{array}{llllll}9 & 1 & 57.720\end{array}$ | +144121.01 | 11 | +0.171 | -0.67 |
| 62 | 1861, | Dee. | 10.0 | 20.3139 .810 | -21 9 42.34 | 4 | $-0.020$ | $-1.41$ |
| 63 |  | Dec. | 260 | 213751.853 | - 152911.52 | 7 | $+0.036$ | - 1.41 |
| 61 | 186: | Jan. | 16.0 | 2 2 38 24.381 | - 6592.66 | 9 | +0.063 | -0.43 |
| 65 |  | Feb. | 12.0 | 225059.987 | + 01757.58 | 2 | +0.201 | -2.41 |
| 66 |  | March | 11.0 | 215859.897 | - 35931.67 | 5 | $+0.211$ | +3.72 |
| 67 |  | April | 23,0 | 231466.685 | - 42027.06 | 9 | +0.061 | +0.09 |
| 68 |  | May | 13.0 | 0263.479 | + 11959.00 | 4 | $-0.069$ | +2.83 |
| 69 | 1863, | July | 11.0 | 102137.937 | + 105331.89 | 7 | -0.014 | +0.74 |
| 70 |  | Aug. | 1.0 | $1135 \quad 5.496$ | + 1221.05 | 6 | $-0.004$ | $-2.34$ |
| 71 |  | Aug. | 12.0 | $12425.88:$ | - 32649.57 | 7 | $+0.106$ | $-4.25$ |
| 72 |  | Sept. | 1.0 | 123555.78 .5 | - 102346.78 | 6 | -0.108 | +0.38 |
| 73 |  | Scpt. | 19.0 | 122454.206 | - 114946.67 | 6 | +0.117 | +1.85 |
| 3 |  | Oct. | 28.0 | 115036.106 | - 14320.76 | 2 | +0.117 | -3.63 |
| 75 |  | Nov. | 20.0 | 1247 333:271 | - 35337.08 | 5 | + 0.202 | - 2.15 |
| 76 | 1865, | Fob. | 13.0 | 03811.720 | + 584.61 | 4 | -0.01: | $-1.17$ |
| 77 |  | March | 25.0 | 2519.300 | +214433.17 | 7 | -0.008 | +0.69 |
| 78 |  | April | 9.0 | 3231.559 | +24 4629.99 | 10 | +0.057 | +0.96 |
| 79 |  | April | 25.0 | 32045.253 | +213133.59 | 11 | +0.102 | - 0.08 |
| 80 |  | Miny | 7.0 | 25028.201 | +2183.49 | 7 | +0.201 | +1.48 |
| 81 |  | May | $\stackrel{21.0}{ }$ | 22859.092 | +145817.96 | 9 | + 0.2333 | +1.59 |
| 8: |  | Junc | 11.0 | 2 42 18.347 | +13 419.61 | 8 | +0.208 | +0.26 |
| 83 |  | June | 22.0 | 37828.235 | +14 5 20.47 | 7 | +0.139 | -0.07 |
| 81 |  | July | 11.0 | $4 \quad 916.618$ | +1722 1.01 | 9 | +0106 | +0.31 |
| 85 | 1866, | Scpt. | 25.0 | $\begin{array}{lll}15 & 1 & 14.407\end{array}$ | -2015 30.52 | 3 | $+0.066$ | +0.55 |
| 86 |  | Oct. | 16.0 | 162417.041 | -26 5 30.30 | 7 | + 0.017 | -1.53 |
| 87 |  | Oct. | 27.0 | 17 2 22.875 | -273658.50 | 3 | $-0.002$ | +0.46 |
| 88 |  | Nov. | 15.0 | 174428.584 | - 274220.26 | 9 | +0.208 | -0.31 |
| 89 |  | Nov. | 30.0 | $17 \quad 392.404$ | -25 2542.81 | 4 | +0.417 | +0.05 |
| 90 |  | Dec. | 28.0 | 164436.668 | -18 5 53.53 | 2 | +0.359 | +0.19 |
| 91 | 1867, |  | 7.0 | $\begin{array}{lllll}18 & 9 & 47.5837\end{array}$ | -19 $\quad 58.09$ | 6 | +0.174 | +1.01 |
| 92 |  | March | 30.0 | 215248.772 | -125121.47 | 2 | $+0.015$ | -0.29 |
| 93 | 1868, |  | 6.0 | $\begin{array}{llll}6 & 7 & 11.831\end{array}$ | +264251.56 | 6 | -0.111 | +0.76 |
| 94 |  | May | 19.0 | $7 \quad 021.501$ | +25 576.61 | 3 | $+0.0 .1$ | +0.95 |
| 95 |  | May | 29.0 | 73452.419 | +242940.91 | 4 | +0.103 | +0.74 |
| 96 |  | June | 12.0 | $8850.82:$ | +214150.55 | 9 | +0.059 | +0.79 |
| 97 |  | Junc | 29.0 | 81630.999 | +181310.72 | 7 | +0.203 | -0.09 |
| 98 |  | July | 14.0 | 7479.381 | +16 9 52.23 | 6 | $\underline{+0.177}$ | +1.23 |
| 99 |  | July | 28.0 | 71421.065 | +153415.57 | 4 | +0.173 | -1.35 |
| 100 |  | Aug. | 15.0 | 71141.426 | +161352.99 | 1 | +0.050 | -0.96 |
| 101 |  | Aug. | 26.0 | 73223.633 | +163818.77 | 4 | +0.10.1 | +0.03 |
| 10: |  | Sept. | 4.0 | 75743.509 | +1635 5.21 | 4 | $-0.069$ | -0.37 |
| 103 |  | Sept. | 18.0 | 84643.419 | +1525 27.66 | 6 | $+0.001$ | -0.63 |
| 104 | 1869, | Dec. | 1.0 | $\begin{array}{lll}19 & 55 & 0.743\end{array}$ | -233319.35 | 2 | +0.033 | $+0.09$ |
| 105 |  | Dec. | 23.0 | 212628.614 | -1637 52. 39 | 1 | +0.038 | +0.94 |
| 106 | 1870, | Jan. | 3.0 | $22 \quad 246.594$ | -12180.76 | 1 | + 0.092 | +1.72 |
| 107 |  | Jan. | 27.0 | 224813.855 | - 32426.46 | 4 | +0.339 | +2.61 |
| 108 |  | Feb. | 21.0 | 221912.992 | - 11410.51 | 3 | +0.257 | +2.49 |
| 109 |  | March | 19.0 | 21496.160 | - 64237.21 | 2 | +0.195 | $+1.21$ |
| 110 |  | April | 5.0 | 221834.856 | - 71836.33 | 2 | +0.087 | $+2.55$ |
| 111 |  | April | 12.0 | 223759.07 2 | - 6362.61 | 3 | +0.266 | +2.67 |
| 112 |  | April | 22.0 | $2310 \quad 0.139$ | - 49621.21 | 3 | +0.060 | +:31 |
|  | 4 V |  |  |  | 25 |  |  |  |

## INTRODUCTION.



Normals in the superior part of the Orbit.

| No. | Greenwich M. 'T. |  | App. R. A. | App. Dec. | No. Obs. | $\triangle a$ | $\Delta \delta$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 146 | 1858, | Jan. 23.0 |  | --215 53́ 48.46 | 3 | +0.022 | -2.26 |
| 117 |  | April 23.0 | 25659.252 | $+163527.79$ | 5 | -0.005 | -0.10 |
| 118 |  | Junc 14.0 | 72755.977 | +233318.26 | 13. | +0.078 | -0.13 |
| 149 |  | July 19.0 | 101752.788 | +121047.22 | 5 | -0.035 | +0.11 |
| 150 | 1859, | Feb. 23.0 | 191456.589 | -191537.66 | 7 | +0.022 | -0.82 |
| 151 |  | Mareh 18.0 | 20574.220 | -161130.29 | 6 | +0.188 | +2.39 |
| 150 |  | Junc 17.0 | 34635.988 | + 18291.65 | 4 | +0.033 | $-0.10$ |
| 153 |  | July 19.0 | 63141.515 | +23657.50 | 11 | -0.021 | - 0.31 |
| 154 |  | Aug. 23.0 | $93320.65 \%$ | + 154911.42 | 8 | $-0.016$ | -0.44 |
| 155 |  | Nov. 13.0 | 161334.918 | -20 4538.42 | 5 | +0.014 | $-1.75$ |
| 156 |  | Dec. 17.0 | $\begin{array}{llll}19 & 5 & 56.987\end{array}$ | - 235527.75 | 4 | +0.043 | -3.39 |
| 157 | 1860, | Jan. 17.0 | 214614.280 | -1510 47.89 | 5 | +0.016 | -2.66 |
| 158 |  | Feb. 29.0 | $1 \begin{array}{lll}1 & 0 & 24.170\end{array}$ | + 61555.78 | 3 | -0062 | -0.77 |
| 159 |  | April 19.0 | 44831.013 | +25 1019.92 | 4 | -0.014 | -0.01 |
| 160 |  | Oct. 21.0 | $111: 317.826$ | + 55146.41 | 5 | $+0.086$ | -0.8: |
| 161 |  | Dec. 10.0 | 144235.914 | -134052.46 | 5 | -0.060 | $-0.81$ |
| 162 | 1867, | May 14.0 | 11119.973 | + 53441.60 | 6 | +0.113 | +0.44 |
| 163 |  | Junc 17.0 | 3498.762 | + 183858.87 | 5 | +0.050 | +1.11 |
| 164 |  | Aug. 18.0 | $9 \quad 10 \quad 1.066$ | + 172341.04 | 6 | -0.059 | + 0.60 |
| 165 |  | Oct. 15.0 | $1341 \quad 6.075$ | - 92837.18 | 1 | +0.009 | -1.01 |

## INTRODUCTION.

Normats in the superior part of the Orlit.

| No. | Greenwich M. 't'. |  |  | App. IR. A | App. Dee. | Nu.Obs. | $\triangle a$ | $\Delta s$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 166 | 1867, | Nor. | 19.0 |  |  | 5 | -0.007 | -0.51 |
| $16 \%$ | 1868, | Oct. | 16.0 | $1040 \quad 43.171$ | + 8: 1839.88 | 9 | +0.100 | +0.01 |
| 168 |  | 1)ee. | 17.0 | 15 18 16.956 | - 1603836.95 | 6 | +0.083 | $+0.83$ |
| 169 | 1869, | Ian. | 12.0 | $17 \quad 3257.506$ | -2202025.57 | 5 | $+0.050$ | -1.48 |
| 170 |  | April |  | 1367.195 | + 84359.95 | 6 | -0.070 | +0.55 |
| 171 |  | June | 17.0 | 64955.781 | + 24755.16 | 5 | -0.020 | + 0.35 |
| 172 |  | July | 16.0 | 9616.090 | +1833 2.87 | 4 | -0.208 | +0.78 |
| 173 |  | Aug. | 26.0 | ${ }^{1} 1210 \quad 0.081$ | - 07381.79 | 5 | -0.010 | + 0.29 |
| 171 |  | Sopt. | 21.0 | $14 \quad 526.8333$ | - 13817.72 | 4 | -0.18:3 | $+1.02$ |
| 17.5 |  | Oct. | 13.0 | 15. 49 4(6.368 | -21 1241.87 | 5 | -0.020 | +1.43 |

In order to have as feew unkown quantities, in the equations of condition, as possible, the differenees $f$ a and So have been changed into ens $\gamma$. $J 0$ and $J_{\gamma} ; 0$ denoting the geocentric longitude of Venus referred to a plane drawn throngh the eentre of the Earth parallel to the plane of the orbit of Venus, and $\eta$ denoting the corresponding latude. The formula used are given in Watsos's Theoretical Astronomy, pp. 153-159.

In the following equations, we have put

$$
\left.\left.\left.x=\lrcorner L_{0}^{\prime}-2 \sin ^{2} \frac{i^{\prime}}{2} \Delta \Omega^{\prime}, \quad y=100\right\lrcorner u^{\prime}, \quad z=\Delta e^{\prime}, \quad u=e^{\prime}( \lrcorner \pi^{\prime}-2 \sin ^{2} \frac{i^{\prime}}{2}\right\lrcorner \Omega^{\prime}\right)
$$

all expressed in seconds of are; and $x^{\prime}, y^{\prime}, z^{\prime}$ and $u^{\prime}$ denote the similar quamtities in reference to the solar elements. In the computation of the cocflicients of the last, roughly approximate formule have been used.

A mean of the Transits of 1761 and 1769 gives

$$
+0.992 x-0.839 y+1.61 z+1.17 u+1.00 x^{\prime}-0.84 y^{\prime}+0.83 z^{\prime}-1.8 u^{\prime}=+1^{\prime \prime} .745
$$

The indeterminate correction of the Sun's semi-diameter nearly disappears from this mean.
The following equations of condition are numbered with the same number es the normals, from which they arr lerived. The last column eontains the residuals-which remain after the elements have been corrected as shown in the sequel.

## Equations of condition.

No.


## INTRODUCTION.

Equations of condition.

| No | ( ${ }^{\text {c }}$ |  |  |  |  |  | Residuals. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | " |  |
|  | $-0.47 x+0.02 y-0.47 z+1.64 u+1.47 x^{\prime}-0.06 y^{\prime}+2.19 z^{\prime}+2.48 u^{\prime}=-0.98$ |  |  |  |  |  | . 79 |
| 22 | - 1.51 | $+0.06-1.31+3.16+2.54$ | $-0.10$ | + 4.37 | +3.00 | $=-1.19$ | -2.93 |
| 23 | $-1.95$ | $+0.07-2.61+3.15+2.95$ | -0.11 | +5.79 | +2.51 | $=+1.81$ | 0.20 |
| 21 | -0.40 | $+0.01+1.03-1.15+1.40$ | $-0.03$ | -2.79 | -1.18 | $=+0.42$ | $+0.24$ |
| 25 | $-2.29$ | $+0.05+3.87-2.60+3.28$ | -0.07 | $-6.58$ | -0.29 | $=-2.95$ | 3.92 |
| 26 | -0.55 | $+0.01+1.78-0.38+1.55$ | $-0.03$ | $-3.33$ | $+1.04$ | $=+3.15$ | +2.75 |
| 27 | -2.22 | $+0.02-4.51-0.53+3.22$ | -0.02 | +4.94 | $-4.09$ | $=+2.47$ | $+0.72$ |
| 28 | - 1.22 | $+0.01-2.59-1.14+2.22$ | -0.01 | +3.02 | -3.46 | $=+0.04$ | -0.85 |
| 29 | -1.55 | $-0.01+2.84+1.97+2.55$ | $+0.02$ | $-2.07$ | + 4.94 | $=-2.24$ | -3.81 |
| 30 | $-2.73$ | $-0.03+3.75+3.93+3.72$ | +0.04 | $-2.06$ | $+7.28$ | $=-0.41$ | - 3.18 |
| 31 | - 0.88 | $-0.01+1.17+2.02+1.88$ | + 0.02 | $-1.96$ | $+4.10$ | $=+4.28$ | $+3.11$ |
| 32 | - 2.18 | $-0.05-1.24-4.31+3.18$ | + 0.08 | - 1.77 | $-6.06$ | $=-0.38$ | - 1.64 |
| 33 | $-1.26$ | $-0.03+0.04-2.92+2.26$ | $+0.06$ | $-2.00$ | $-4.22$ | $=+2.07$ | +1.48 |
| 31 | - 0.44 | $-0.01+0.19-1.60+1.44$ | + 0.04 | -1.92 | $-2.50$ | $=+1.59$ | +1.39 |
| 35 | -0.68 | $-0.03-0.51+1.96+1.68$ | +0.07 | +2.58 | +2.70 | $=+0.46$ | -0.68 |
| 36 | -1.37 | $-0.06-1.02+2.96+2.37$ | $+0.10$ | $+3.95$ | $+3.09$ | + 0.71 | -1.20 |
| 37 | $-2.43$ | $-0.10-2.15+4.44+3.42$ | +0.14 | +5.83 | +3.70 | $=+2.52$ | -0.59 |
| 38 | -0.54 | $-0.03+1.14-1.33+1.54$ | +0.09 | -3.10 | $-1.20$ | $=-0.19$ | -0.52 |
| 39 | -2.27 | $-0.13+3.71-2.77+3.27$ | +0.19 | -6.49 | -0.59 | $=+0.25$ | - 1.20 |
| 40 | $-2.32$ | $-0.13+4.26-2.04+3.27$ | + 0.19 | -6.59 | -0.07 | $=+1.34$ | -0.27 |
| 41 | -0.46 | $-0.03+1.64-0.39+1.46$ | +0.09 | -3.12 | +0.99 | $=+2.17$ | +1.73 |
| 42 | +0.13 | $+0.01-0.89+0.28+0.87$ | +0.06 | +1.91 | +0.52 | $=+1.01$ | + 0.85 |
| 43 | -0.25 | $-0.02-1.34+0.16+1.24$ | +0.09 | $+2.71$ | -0.68 | $=-0.68$ | - 1.18 |
| 44 | - 1.37 | $-0.10-3.10+0.07+2.37$ | + 0.17 | +4.12 | $-2.66$ | $=+0.01$ | $-1.5 \%$ |
| 45 | $-2.17$ | $-0.16-4.30-1.15+3.17$ | +0.23 | +4.76 | $-4.18$ | $=+1.79$ | -0.31 |
| 46 | -0.86 | $-0.06-2.06-0.91+1.86$ | + 0.14 | $+2.50$ | $-3.03$ | $=+0.55$ | -0.31 |
| 47 | -0.41 | $-0.03-1.38-0.72+1.41$ | +0.11 | + 1.57 | -2.63 | $=+1.49$ | + 1.01 |
| 48 | +0.28 | $+0.02+0.81-0.23+0.72$ | $+0.06$ | - 1.45 | -0.59 | $=-2.32$ | -2,18 |
| 49 | +0.13 | $+0.01+0.92+0.17+0.87$ | $+0.08$ | - 1.91 | $+0.43$ | -0.21 | -0.26 |
| 50 | -0.05 | $0.00+1.06+0.48+1.04$ | $+0.09$ | - 1.96 | + 1.41 | $=-0.98$ | - 1.26 |
| 51 | -0.80 | $-0.07+1.95+1.04+1.79$ | $+0.16$ | $-2.15$ | $+3.30$ | $=+0.98$ | - 0.08 |
| 52 | -2.13 | $-0.19+3.57+2.60+3.10$ | +0.28 | $-2.37$ | +5.96 | $=+4.52$ | +1.97 |
| 53 | -2.58 | $-0.23+3.49+3.83+3.54$ | +0.32 | $-2.09$ | $+6.93$ | $=+3.16$ | -0.06 |
| 54 | -1.28 | $-0.12+1.70+2.46+2.26$ | +0.20 | -0.80 | +4.79 | $=+0.13$ | - 1.67 |
| 55 | -0.48 | $-0.04+0.81+1.49+1.47$ | +0.13 | $+0.19$ | +3.29 | $=+1.9 \pm$ | +1.03 |
| 56 | + 0.09 | $+0.01-0.55-0.78+0.92$ | +0.09 | +1.02 | - 1.78 | $=+0.55$ | + 0.58 |
| 57 | -0.17 | $-0.02-0.62-1.07+1.18$ | +0.12 | + 0.55 | -2.81 | $=+0.44$ | +0.27 |
| 58 | - 1.03 | $-0.11-1.08-2.31+2.05$ | +0.21 | -0.57 | -4.25 | $=+0.95$ | +0.14 |
| 59 | -2.27 | $-0.24-1.37-4.41+3.29$ | +0.35 | $-1.62$ | -6.32 | $=+1.02$ | $-0.62$ |
| 60 | $-0.52$ | $-0.05+0.10-1.72+1.52$ | +0.16 | $-1.83$ | $-2.76$ | $=+2.87$ | +2.42 |
| 61 | -0.06 | $-0.01+0.16-1.09+1.07$ | +0.11 | -1.89 | $-1.47$ | $=+2.61$ | $+2.58$ |
| 62 | + 0.07 | $+0.01-0.02+1.02+0.92$ | +0.11 | $+0.26$ | +2.12 | $=-0.58$ | -0,88 |
| 63 | -0.12 | $-0.01-0.16+1.21+1.11$ | +0.13 | +1.00 | +2.37 | $=+0.07$ | $-0.48$ |
| 64 | -0.62 | $-0.07-0.36+1.89+1.61$ | +0.19 | +2.35 | +2.74 | $=+0.72$ | -0.48 |
| 65 | -2.12 | $-0.26-1.60+4.07+3.07$ | + 0.37 | $+5.13$ | +3.73 | $=+1.87$ | - 1.35 |
|  |  |  | 28 |  |  |  |  |

## INTRODUCTION.

## Liquations of contition.

No.


## INTRODUCTION.

Equalions of condition.
No


## INTRODUCTION.

## Equations of condition.



The equations derived from the latitudes $\eta$ contain two more unknown quantities,

$$
v=\Delta i^{\prime} \quad, \quad w=\sin i^{\prime} \cdot \Delta \Omega^{\prime},
$$

but in them the variation of the solar elements will be neglected.
The mean of the Transits of 1761 and 1769 gives

$$
-0.059 x+0.050 y-0.095 z-0.069 u+0.00 v+1.000 w=-1^{\prime \prime} .165
$$

From this mean the indeterminate correction of the Sun's semi-diameter is nearly eliminated.
Equations of condition.

|  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $-0.01 x$ | $+0.00 y$ | $-0.01 z$ | $+0.00 u$ | $+0.61 v$ | $+1.24 w$ | $=+0.82$ |
| 2 | -0.10 | $+0.01$ | $-0.21$ | $-0.08$ | $-0.36$ | $+1.95$ | $=+0.41$ |
| 3 | -0.12 | + 0.02 | -0.31 | -0.11 | $-1.09$ | +2.04 | $-0.49$ |
| 4 | $+0.17$ | $-0.02$ | -0.41 | +0.25 | $-2.13$ | + 0.88 | -0.14 |
| 5 | $+0.20$ | $-0.03$ | $-0.37$ | $+0.17$ | -. 1.60 | $-0.4$ | 1.51 |
| 6 | $+0.09$ | $-0.01$ | $-0$. | $-0$. | + 0.12 | - 1.3 | $=+0.0$ |
| 7 | $+0.20$ | $-0.02$ | $-0.23$ | $-0.35$ | $+1.17$ | 1.42 | $=+5.6$ |
| 8 | + 0.19 | $-0.02$ | $-0.30$ | -0.49 | $+2.32$ | - 0.77 | $=+1$. |
| 9 | -0.14 | + 0.02 | $-0.54$ | -0.16 | +2.42 | $+0.46$ | $=+0.6$ |
| 10 | $-0.23$ | $+0.03$ | $-0.54$ | $-0.07$ | $+1.88$ | $+1.10$ | $=-1.7$ |
| 11 | $-0.18$ | $+0.02$ | $-0.36$ | $-0.10$ | + 1.05 | $+1.38$ | $=-1.48$ |
| 12 | $-0.22$ | $+0.02$ | -0.01 | $-0.58$ | $-2.34$ | $-0.09$ | $=-1.49$ |
| 13 | + 0.11 | - 0.01 | -0.33 | $-0.36$ | $-2.06$ | $-1.55$ | $=+1.0$ |
| 14 | + 0.12 | $-0.01$ | + 0.21 | -0.24 | $+1.57$ | +1.68 | $=+0.34$ |
| 15 | $\bigcirc 0.03$ | 0.00 | $-0.02$ | $-0.09$ | $+0.06$ | +2.34 | $=+0.63$ |

## INTRODUCTION.

Equations of condition.

| 16 | $+0.02 x$ | $0.00 y$ | $+0.01 z$ | +0.05 ¢ | $-0.75 v$ | + $1.69 w$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 17 | $+0.01$ | 0.00 | $-0.07$ | +0.04 | $+0.27$ | - 2.68 | $=+2.21$ |
| 18 | $-0.15$ | $+0.01$ | $-0.12$ | $+0.32$ | $+1.60$ | - 1.45 | $=+0.21$ |
| 19 | $+0.01$ | 0.00 | + 0.02 | 0.00 | $+0.78$ | + 0.97 | $=+1.13$ |
| 20 | $+0.10$ | 0.00 | $-0.38$ | $+0.18$ | $-2.05$ | $+1.36$ | $=-0.77$ |
| 21 | + 0.11 | 0.00 | $-0.17$ | -0.11 | $+0.33$ | $-1.45$ | $=+0.53$ |
| 22 | +0.23 | $-0.01$ | $-0.28$ | $-0.45$ | + 1.63 | $-1.35$ | $=+0.73$ |
| 23 | $-0.23$ | + 0.01 | $-0.57$ | $-0.06$ | +2.13 | + 0.86 | $=-4.0$ |
| 24 | $-0.13$ | 0.00 | -0.12 | $-0.25$ | $-0.86$ | + 1.09 | $=+0.95$ |
| 25 | $-0.17$ | 0.00 | $-0.07$ | $-0.56$ | -2.43 | $-0.35$ | - 0.67 |
| 26 | + 0.07 | 0.00 | $-0.09$ | - 0.11 | + 0.09 | $-1.54$ | $=+0$ |
| 27 | +0.10 | 0.00 | + 0.18 | -0.24 | + 1.52 | $+1.83$ | $=-0.65$ |
| 28 | + 0.01 | 0.00 | 0.00 | + 0.02 | $-0.62$ | +1.79 | + 3.82 |
| 29 | $-0.06$ | 0.00 | $+0.14$ | -0.05 | - 1.03 | - 1.91 | - 2.56 |
| 30 | 0.00 | 0.00 | $-0.07$ | + 0.07 | + 0.49 | -2.67 | -0.52 |
| 31 | $-0.15$ | 0.00 | $-0.15$ | $+0.29$ | $+1.60$ | -0.73 | $=-0.13$ |
| 32 | $-0.10$ | 0.00 | $-0.30$ | $-0.06$ | - 1.04 | +2.13 | $=+0.55$ |
| 33 | + 0.21 | + 0.01 | $-0.38$ | $+0.27$ | - 1.92 | + 0.18 | $-0.52$ |
| 34 | + 0.16 | 0.00 | $-0.30$ | $+0.10$ | - 1.27 | -0.63 | $-0.79$ |
| 35 | +0.14 | $+0.01$ | $-0.21$ | $-0.20$ | $+0.59$ | $-1.54$ | - 0.38 |
| 36 | $+0.22$ | $+0.01$ | $-0.27$ | $-0.39$ | $+1.41$ | $-1.47$ | $=+1.29$ |
| 37 | + 0.16 | $+0.01$ | $-0.37$ | -0.44 | +2.39 | $-0.81$ | $-0.72$ |
| 38 | -0.16 | $-0.01$ | $-0.12$ | $-0.30$ | -0.98 | $+1.12$ | $+0.33$ |
| 39 | -0.18 | -0.01 | $-0.09$ | -0.56 | - 2.43 | -0.21 | $=+2.84$ |
| 40 | + 0.17 | + 0.01 | $-0.42$ | -0.29 | $-1.88$ | $-1.59$ | - 1.00 |
| 41 | $+0.06$ | 0.00 | $-0.08$ | $-0.10$ | $+0.20$ | - 1.44 | $+0.10$ |
| 42 | $+0.06$ | 0.00 | $-0.06$ | -0.11 | +031 | $-0.86$ | $=+0.03$ |
| 43 | + 0.13 | $+0.01$ | $+0.04$ | -0.25 | $+1.18$ | $-0.46$ | $=+0.64$ |
| 44 | $+0.18$ | + 0.01 | $+0.22$ | $-0.32$ | + 1.78 | $+0.86$ | $-0.92$ |
| 45 | $-0.05$ | 0.00 | $-0.03$ | -0.14 | $+0.33$ | $+2.36$ | $-0.04$ |
| 46 | $+0.02$ | 0.00 | $+0.01$ | $+0.05$ | -0.80 | + 1.48 | $=+0.66$ |
| 47 | $+0.05$ | 0.00 | $-0.01$ | $+0.10$ | - 1.04 | $+0.90$ | $=+0.64$ |
| 48 | -0.03 | 0.00 | $-0.05$ | $-0.05$ | $+0.03$ | $+0.70$ | $=+0.07$ |
| 49 | $-0.07$ | $-0.01$ | $-0.02$ | $-0.13$ | $-0.68$ | $+0.61$ | $-1.75$ |
| 50 | $-0.09$ | $-0.01$ | $+0.09$ | $-0.16$ | $-1.15$ | $+0.14$ | $-0.90$ |
| 51 | $-0.11$ | $-0.01$ | $+0.19$ | -0.12 | - 1.37 | - 1.06 | $=-3.16$ |
| 52 | $-0.03$ | 0.00 | $+0.09$ | $-0.03$ | -0.71 | - 2.35 | $-4.41$ |
| 53 | -0.03 | 0.00 | $-0.07$ | $+0.13$ | $+0.84$ | -2.49 | $-1.78$ |
| 54 | $-0.14$ | $-0.01$ | $-0.10$ | $+0.29$ | $+1.51$ | - 1.26 | $=+3.67$ |
| 55 | $-0.12$ | $-0.01$ | $-0.14$ | $+0.19$ | $+1.45$ | $-0.21$ | $=+0.35$ |
| 56 | $+0.04$ | 0.00 | $+0.06$ | -0.05 | $+0.93$ | +0.14 | $=+1.39$ |
| 57 | $+0.03$ | 0.00 | + 0.05 | -0.02 | $+0.90$ | $+0.79$ | $=+1.57$ |
| 58 | $-0.05$ | 0.00 | $-0.10$ | $-0.02$ | $+0.18$ | + 1.80 | $=+2.67$ |
| 5 | $-0.08$ | $-0.01$ | $-0.30$ | $-0.03$ | - 1.11 | +2.13 | $=+2.72$ |
| 60 | $+0.16$ | $+0.02$ | $-0.31$ | + 0.13 | $-1.37$ | -0.50 |  |

## INTRODUCTION.

- Equations of condition.

No.

| 61 | $+0.10 x$ | $+0.01 y$ | $-0.19 z$ | $-0.01 u$ | $-0.63 v$ | $-0.90 w$ | $=-0.01$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 62 | 0.00 | 0.00 | $-0.01$ | 0.00 | $-0.70$ | $-0.73$ | $=-1.35$ |
| 63 | $+0.04$ | 0.00 | $-0.07$ | $-0.02$ | $-0.37$ | $+1.15$ | $=-1.50$ |
| 64 | + 0.13 | $+0.01$ | $-0.20$ | $-0.17$ | + 0.44 | -1.54 | $=-0.74$ |
| 65 | $+0.22$ | $+0.03$ | $-0.34$ | $-0.47$ | +2.04 | $-1.19$ | $=-3.38$ |
|  | $-0.21$ | -0.03 | $-0.59$ | -0.02 | $+2.26$ | $+0.54$ | $=+2.46$ |
| 67 | $-0.08$ | $-0.01$ | $-0.14$ | $-0.09$ | $+0.16$ | $+1.25$ | $=-0.29$ |
| 68 | $-0.03$ | 0.00 | $-0.03$ | $-0.05$ | -0.40 | $+0.89$ | $=+3.00$ |
| 69 | $-0.04$ | 0.00 | $-0.07$ | $-0.03$ | $+0.26$ | $+0.90$ | $=+0.62$ |
| 70 | $-0.07$ | $-0.01$ | $-0.09$ | $-0.11$ | $-0.36$ | $+1.15$ | $=-2.16$ |
| 71 | -0.14 | $-0.02$ | $-0.13$ | $-0.25$ | $-0.80$ | $+1.15$ | $=-3.21$ |
| 72 | $-0.23$ | $-0.03$ | $-0.07$ | $-0.49$ | $-1.74$ | $+0.76$ | $=-0.32$ |
| 73 | -0.17 | -0.02 | $-0.12$ | $-0.56$ | $-2.41$ | $-0.21$ | $=+2.40$ |
| 74 | $+0.16$ | $+0.02$ | $-0.28$ | $-0.18$ | $-0.74$ | $-1.75$ | $=-2.59$ |
| 75 | + 0.04 | $+0.01$ | $-0.05$ | $-0.07$ | $+0.33$ | $-1.30$ | $=-0.70$ |
| 76 | + 0.06 | + 0.01 | $-0.07$ | $-0.10$ | + 0.26 | $-0.86$ | $=-0.80$ |
| 77 | + 0.16 | $+0.02$ | $+0.09$ | $-0.30$ | $+1.43$ | $-0.21$ | $=+0.69$ |
| 78 | $+0.19$ | $+0.03$ | $+0.21$ | -0.34 | + 1.75 | $+0.50$ | $=+0.68$ |
| 79 | $+0.13$ | $+0.02$ | $+0.20$ | $-0.30$ | +1.72 | +1.54 | $=-0.50$ |
| 80 | $+0.01$ | 0.00 | $+0.03$ | $-0.17$ | +1.22 | $+2.20$ | $=+0.45$ |
| 81 | $-0.04$ | $-0.01$ | $-0.03$ | $-0.09$ | $+0.07$ | +2.22 | $=+0.26$ |
| 82 | $+0.02$ | 0.00 | $+0.01$ | $+0.04$ | $-0.76$ | $+1.50$ | $=-0.82$ |
| 83 | $+0.04$ | $+0.01$ | 0.00 | +0.08 | -0.99 | $+1.02$ | $=-0.72$ |
| 84 | $+0.05$ | + 0.01 | -0.04 | $+0.10$ | $-1.06$ | $+0.30$ | $=-0.07$ |
| 85 | $-0.08$ | $-0.01$ | $+0.01$ | $-0.16$ | $-0.88$ | + 0.49 | $=+0.83$ |
| 86 | $-0.11$ | $-0.02$ | +0.12 | $-0.17$ | - 1.29 | $-0.09$ | $=-1.35$ |
| 87 | $-0.12$ | $-0.02$ | $+0.17$ | $-0.16$ | $-1.41$ | $-0.56$ | $=+0.45$ |
| 88 | $-0.10$ | -0.02 | $+0.20$ | $-0.09$ | -1.26 | $-1.63$ | $=-0.07$ |
| 89 | $-0.03$ | 0.00 | $+0.07$ | $-0.04$ | $-0.61$ | $-2.49$ | $=+0.58$ |
| 90 | $-0.09$ | $-0.02$ | $-0.05$ | $+0.23$ | $+1.23$ | $-2.00$ | $=+1.14$ |
| 91 | $-0.11$ | $-0.02$ | $-0.17$ | + 0.15 | + 1.24 | $+0.17$ | $=+0.70$ |
| 92 | -0.04 | $-0.01$ | $-0.07$ | $-0.03$ | $+0.01$ | $+0.75$ | $=-0.49$ |
| 93 | $+0.04$ | $+0.01$ | $+0.06$ | $-0.05$ | + 0.96 | + 0.26 | $=+0.83$ |
| 94 | $+0.03$ | + 0.01 | $+0.06$ | $-0.02$ | $+0.95$ | $+0.69$ | $=+0.99$ |
| 95 | $+0.02$ | 0.00 | $+0.04$ | $-0.01$ | $+0.82$ | + 1.06 | $=+0.89$ |
| 96 | -0.02 | 0.00 | $-0.04$ | 0.00 | $+0.44$ | $+1.61$ | $=+0.92$ |
| 97 | -0.09 | $-0.02$ | $-0.21$ | $-0.05$ | -044 | $+2.14$ | $=+0.44$ |
| 98 | $-0.03$ | 0.00 | $-0.31$ | $+0.05$ | - 1.44 | +2.02 | $=+1.56$ |
| 99 | + 0.14 | $+0.03$ | -0.33 | $+0.27$ | -1.96 | +1.25 | $=-1.15$ |
| 100 | $+0.20$ | $+0.04$ | $-0.34$ | $+0.26$ | $-1.79$ | $+0.12$ | $=-0.91$ |
| 101 | $+0.17$ | $+0.03$ | $-0.31$ | $+0.17$ | $-1.48$ | $-0.35$ | $=+0.19$ |
| 102 | +0.14 | $+0.03$ | $-0.27$ | $+0.09$ | $-1.18$ | $-0.62$ | $=-0.52$ |
| 103 | +0.10 | +0.02 | $-0.20$ | 0.00 | $-0.72$ | $-0.86$ | $=-0.60$ |
| 104 | -0.01 | 0.00 | + 0.01 | 0.00 | $-0.79$ | $-0.52$ | $=+0.02$ |
| 105 | $+0.03$ | $+0.01$ | -0.06 | $-0.01$ | $-0.43$ | $-1.12$ | $=+0.74$ |

## INTRODUCTION.

## Equations of condition.



To apply to these equations the rigorous method of least squares would be very laborious: henee a method of "Equivalent Factors" has been used; the equations have been multiplied cither by whole numbers or by fractions which are ready multipliers. In this way, the following Normal Equations were derived from the equations of condition whieh have $\cos \eta . \Delta \theta$ for their absolute terms,

$$
\begin{array}{r}
+195.84 x-44.809 y+127.71 z+73.19 u-251.90 x^{\prime}+43.027 y^{\prime}-85.48 z^{\prime}+119.25 u^{\prime}=-8.77 \\
-44.78+47.099-83.68-62.84+41.04-48.460+41.17-96.06=-113.43 \\
+120.94-83.889+427.28+133.17-136.59+82.936-410.76+400.15 \\
+70.03-62.965+135.64+365.81-73.13+63.350+114.76+508.04 \\
=+162.30 \\
-255.15+42.172-138.12-80.06+425.61-27.182+91.22-132.67 \\
+40.68-48.373+82.84+61.99-26.27+51.815-41.45+94.13 \\
-83.42+41.537 \\
+422.53+119.76+102.83-40.091+64.06-11.82 \\
+112.81-95.792+406.68+505.65-126.69+94.62-120.34+902.21 \\
\\
\end{array}
$$

## INTRODUCTION.

If $u$ is eliminated from these equations, the result is

| $+181.83 x$ | $-32.213 y$ | $+100.57 z$ | $-237.27 x^{\prime}$ | $+30.352 y^{\prime}-108.44 z^{\prime}$ | $+17.60 u^{\prime}$ | $=-48.20$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| -32.75 | +36.284 | -60.38 | +28.48 | -37.577 | +60.88 | -8.78 | $=-79.58$ |
| +95.45 | -60.971 | +377.90 | -109.97 | +59.874 | -452.54 | +215.20 | $=+90.56$ |
| -239.82 | +28.394 | -108.43 | +409.63 | -13.317 | +116.34 | -21.48 | $=+135.76$ |
| +28.81 | -37.705 | +59.85 | -13.88 | +41.080 | -60.90 | +8.04 | $=+87.79$ |
| -106.35 | +62.147 | -466.94 | +126.77 | -60.831 | +606.49 | -278.15 | $=-88.38$ |
| +16.01 | -8.770 | +219.18 | -25.60 | +7.053 | -278.97 | +199.94 | $=-8.21$ |

And if from these $z$ is eliminated, the result is

| $+156.43 x$ | $-15.987 y$ | $-208.00 x^{\prime}$ | $+14.418 y^{\prime}$ | $+11.99 z^{\prime}$ | $-39.67 u^{\prime}$ | $=-72.30$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| -17.50 | +26.542 | +10.91 | -28.055 | -11.42 | +25.60 | $=-65.11$ |
| -212.43 | +10.900 | +378.08 | +3.863 | -13.51 | +40.27 | $=+161.74$ |
| +13.69 | -28.049 | +3.54 | +31.598 | +10.77 | -26.04 | $=+73.45$ |
| +11.59 | -13.190 | -9.11 | +13.151 | +47.33 | -12.25 | $=+23.52$ |
| -39.35 | +26.593 | +38.18 | -27.674 | -16.50 | +75.13 | $=-61.46$ |

It is evident now, that since the principal co-efficients of $z^{\prime}$ and $u^{\prime}$ have fallen from 644.06 and 902.21 to +7.33 and 75.13, no very reliable values of these quantities can be obtained from these equations. The elimination of $y$ gives

| $+145.89 x$ | $-201.43 x^{\prime}$ | $-2.480 y^{\prime}$ | $+5.11 z^{\prime}$ | $-24.25 u^{\prime}$ | $=-111.52$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| -205.24 | +373.60 | +15.384 | -8.82 | +29.76 | $=+188.48$ |
| -4.80 | -15.07 | +1.950 | -1.30 | -1.01 | $=+4.64$ |
| +2.89 | -3.69 | -0.791 | +41.65 | +0.47 | $=-8.84$ |
| -21.82 | +27.25 | +0.435 | -5.06 | +49.48 | $=+3.78$ |

The elimination of $x$ from these gives

$$
\begin{array}{lllll}
+90.23 x^{\prime}+11.895 y^{\prime} & -1.63 z^{\prime} & -4.35 u^{\prime} & =+31.63 \\
+8.44 & +1.868 & -1.13 & +0.21 & =+0.97 \\
+0.30 & -0.742 & +41.55 & +0.95 & =-6.63 \\
-2.88 & +0.064 & -4.30 & +45.85 & =-12.89
\end{array}
$$

The elimination of $x^{\prime}$ from these gives

$$
\begin{aligned}
& +0.755 y^{\prime}-0.98 z^{\prime}+0.62 u^{\prime}=-1.99 \\
& -0.782+41.56+0.96=-6.74 \\
& +0.444-4.35+45.71=-11.88
\end{aligned}
$$

The only condition, relative to the solar elements, which can be obtained with any weight, from these equations, is

$$
x^{\prime}+0.132 y^{\prime}=+0^{\prime \prime} .335
$$

That is, the mean longitude of the Sun of Hansen and Olufsen's Tables ought to be increased by a third of a second at the epoch 1863. As, however, these Tables will, probably, be used, for a long time to come, in computing the solar coördinates of the American Ephemeris, $y^{\prime}, z^{\prime}$ and $u^{\prime}$ will be put severally equal to zero; and as it has been decided to use the Pulkova constant of aberration, $x^{\prime}$ will be put equal to $+0^{\prime \prime} .19$. With these assumptions, the values of $x, y, z$ and $u$ are

$$
x=-0^{\prime \prime} .502, \quad y=-2^{\prime \prime} .863, \quad z=-0^{\prime \prime} .040, \quad u=+0^{\prime \prime} .195
$$

The equation of condition derived from the Transits of 1761 and 1769 being excluded, the normal equations, determining the corrections of the inclination and the longitude of the ascending node, are

$$
\begin{gathered}
+2.51 x+0.390 y+1.84 z-0.67 u+163.26 v-0.42 w=+26^{\prime \prime} .02 \\
-4.46-0.105-0.29-1.06-5.86+188.58=+24.11 \\
35
\end{gathered}
$$

## INTRODUCTION.

From these are obtained the following values of $v$ and $w$.

$$
v=+0^{\prime \prime} \cdot 18_{\mathrm{z}} \quad w=+0^{\prime \prime} .12 \text { or } \Delta \delta^{\prime}=+2^{\prime \prime} .0
$$

But from the equation furnished by the Transits in 1761 and 1769,

$$
\Delta \delta^{\prime}=-17^{\prime \prime} .84
$$

If the first result is supposed to belong to 1855.0 , and the second to 1765.4 , the proper value of the correction is

$$
\Delta \Omega^{\prime}=+0^{\prime \prime} .9+0^{\prime \prime} 222 t
$$

The origin of the pretty large correction - $0^{\prime \prime} .02863$, of the mean motion of Venus, is easily shown. In his investigation, Leverrier (Annales, Vol. VI., p. 72) found the following value of $\Delta n^{\prime}$,

$$
\Delta n^{\prime}=+0^{\prime \prime} .00035+0^{\prime \prime} .0689 \nu+0^{\prime \prime} .0959 \nu^{\prime}+0^{\prime \prime} .1207 \nu^{\prime \prime} ;
$$

but the value of this quantity used in forming his Tables is the first term only. If the values of $\nu, \nu^{\prime}$ and $\nu^{\prime \prime}$ corresponding to the change from Leverrier's values of the masses to those here adopted, be substituted in this expression, the correction of Leverrier's mean motion, from this cause, is found to be

$$
\Delta n^{\prime}=-0^{\prime \prime} .01588
$$

Moreover, a comparison of the values of the Sun's mean longitude in the Tables of Hansen and Olufsen and of Leverrier, gives

$$
\text { Han. }- \text { Lev. }=-0^{\prime \prime} .93-0^{\prime \prime} .01074 t
$$

From the way in which $\Delta n^{\prime}$ and $\Delta n^{\prime \prime}$ are involved in the equations of condition, it may be concluded, that if $\Delta n^{\prime \prime}$ were left indeterminate in the solution, the value of $\Delta n^{\prime}$, obtained, would be roughly,

$$
\Delta n^{\prime}=\left(\Delta n^{\prime}\right)+1.2 \Delta n^{\prime \prime},
$$

( $\Delta n^{\prime}$ ) denoting the value of $\Delta n^{\prime}$ on the supposition of $\Delta n^{\prime \prime}=0$. Thus on making $\Delta n^{\prime \prime}=-0^{\prime \prime} .01074$, the correction of the mean motion of Venus, from this cause is

$$
\Delta n^{\prime}=-0^{\prime \prime} .01289
$$

The sum of these two corrections is

$$
\Delta n^{\prime}=-0^{\prime \prime} .02877
$$

which is almost identical with that derived from the equations of condition.
The increment of the motion of the node, $0^{\prime \prime} .222$, requires that the mass of Venus should be reduced from $\frac{1}{408134}$ to $\frac{1}{427240}$. This agrees with Leverrier's result: setting out with the mass 0.0000024885 , he found that it should be multipled by the factor 0.948 , which would make the mass $\frac{1}{423900}$.

The corrections to be added to the elements, with which we set out, to obtain the elements, from which the Tables are constructed, are

$$
\begin{aligned}
& \Delta L^{\prime}=-0^{\prime \prime} .502 \\
& \Delta \pi^{\prime}=+28^{\prime \prime} .46, \\
& \Delta \Omega^{\prime}=+0^{\prime \prime} .90+0^{\prime \prime} .222 t \\
& \Delta i^{\prime}=+0^{\prime \prime} .18, \\
& \Delta e^{\prime}=-0.000000196, \\
& \Delta n^{\prime}=-0^{\prime \prime} .02863
\end{aligned}
$$

The Tables have been compared with the occultation of Mercury by Venus, observed at Greenwich May 28, 1737. The observations made are

Greenwich M. T.

| h m s <br> 9 40 3.9. | Mercury distant from Venus not more than a tenth part of the diameter of Venus. |  |  |
| :--- | :--- | :--- | :--- |
| 9 | 48 | 10.2. | Mercury wholly occulted by Venus. |

## INTRODUCTION.

The position of Mercury being derived from Prof. Winloek's Tables, the apparent position of the two planets, as seen from Greenwich, and in longitude and latitude, are


And interpolating

| Greenwich M. T. | $l^{\prime}-l$. | $b^{\prime}-b$. | Dist. of Centres. |  |
| :---: | :---: | :---: | :---: | :---: |
| h | m | s | ${ }^{\prime \prime}$ | $\prime \prime$ |

With the addition of $0^{\prime \prime} .57$ for irradiation, the semi-diameters of Mercury and Venus are respectively $3^{\prime \prime} .98$ and $26^{\prime \prime} .97$ : hence at the first observation, the distance of the limbs of the planet is $8^{\prime \prime} .01,2^{\prime \prime} .6$ more than a tenth part of the diameter of Venus; at the second observation, the distance of the centres is less than the difference of semi-diameters; hence the Tables are verified by the statement of the observer. Venus being, at the time, a thin erescent, and about half of Mercury's disc being illuminated, it is plain that it would be difficult for the obsever .o estimate the distance in fractional parts of the apparent diameter of Venus.

Leverrier's remarks on this occultation are impaired by a mistake made in the last line of his computation.


## TABLES OF VENUS.

LONGITUDE OF TIE PRINCIPAL OBSERVATORIES FROM WASIING'ION.
West Longitudes are marked +

| Place. | Longitude from Washington in Time. | In Decimals of a Day. | Place. | $\begin{gathered} \text { Longitude } \\ \text { from Washington } \\ \text { in 'Time. } \end{gathered}$ | In Decimals of a Day. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Åbo, |  | - ${ }^{\text {d }} .2759296$ | Leipsic, | - ${ }^{\text {h }} 5{ }^{\text {m }}{ }^{\text {\% }} 46.87$ | -0.2484592 |
| Albany, ${ }^{\text {\% }}$ | -0 1312.87 | -0.0091767 | Leyden, | 5268.57 | $-0.2264881$ |
| Allegheny,* | +0 1150.20 | +0.008\%199 | Liverpool, | - 45612.31 | -0.20:6984 |
| Altona, | -5 4758.54 | -0.2116498 | Madras, | -10 299.67 | -0.4369175 |
| Anu Arbor, | +0 2642.67 | +0.0185 194 | Madrid, | - 45327.00 | -0.2037847 |
| Armagh, | -4 4136.92 | -0.1955662 | Mannheim, | - 5423.06 | -0.2375354 |
| Athens, | -6 $43 \quad 7.58$ | $-0.2799488$ | Markrec, | - 43424.00 | -0.1905556 |
| Berlin, | -6 1147.77 | -0.2512473 | Marscilles, | - 52940.55 | -0.2289415 |
| Bilk, | -5 3517.77 | -0.2328445 | Melbourne, | -14 487.17 | -0.6167496 |
| Bonn, | -5 3636.02 | -0.2337502 | Milan, | - 54458.20 | -0.2395625 |
| Breslau, | -6 1622.19 | -0.2613679 | Modena, | - 55155.53 | -0.2443927 |
| Brussels, | -5 2541.29 | -0.2261723 | Moscow, | - 73829.29 | -0.3183946 |
| Cambridge, (Eng.) | -5 $\quad 838.08$ | -0.2142949 | Munich, | - 55438.00 | -0.2462731 |
| Cambridge, (Mass.) | -0 2341.51 | -0.0164530 | Naples, | - $6 \quad 5 \quad 10.95$ | $-0.2535990$ |
| Cape of Good Hope, | $\begin{array}{lll}-6 & 22 & 8.09\end{array}$ | -0.2653711 | Now York,* | - 01215.47 | -0.0085124 |
| Chieago, | +0 4214.26 | +0.0293317 | Nicolajew, | - 7166.53 | -0.3028534 |
| Cincinnati,* | +0 2946.94 | +0.0206822 | Olmütz, | - 61715.43 | -0.29619811 |
| Cliristiania, | $-551 \quad 6.69$ | -0.2438274 | Oxford, | -5 $\begin{array}{llll}6 & 9.79\end{array}$ | -0.2105300 |
| Clinton, | -0 633.08 | -0.0045727 | Padua, | - 55541.17 | $-0.2470013$ |
| Copenlagen, | -5 5831.05 | -0.2489703 | Palermo, | - 6 1 137.00 | $-0.2511227$ |
| Cracow, | -6 $28 \quad 2.80$ | -0.2694768 | Paramatta, | -15 1218.61 | -0.6335191 |
| Dorpat, | $\begin{array}{llll}-6 & 55 & 6.02\end{array}$ | -0.2882641 | Paris, | - 51733.02 | $-0.2205211$ |
| Dublin, | -4 4250.39 | -0.1964165 | Pliladelphia,* | -0 733.64 | -0.005250.5 |
| Durham, | -5 152.64 | -0.2096370 | Prague, | - 6 5 53.52 | -0.2510917 |
| Edinburgh, | -4 5529.34 | -0.2052007 | Pulkowa, | -7 931.06 | -0.2982757 |
| Florence, | -5 5315.12 | -0.2453139 | Rome, | - 5588.58 | -0.2.187098 |
| Geneva, | -5 3249.24 | -0.2311344 | San Fernaudo, | - 44322.42 | -0.1967873 |
| Georgetown,* | +0 006.20 | +0.0000718 | Santiago, | - 02530.00 | $-0.0177083$ |
| Göttingen, | -5 4758.49 | -0.2416192 | Senftenberg, | - 6143.00 | $-0.2597570$ |
| Gotha, | -5 5133.39 | -0.2437892 | Speyer, | - 54158.00 | $-0.2374769$ |
| Greenwich, | $\begin{array}{lllll}-5 & 8 & 12.39\end{array}$ | $-0.2140323$ | Stockholm, | - 62028.35 | -0.2641939 |
| Hamburg, | -5 $48 \quad 5.95$ | -0.2417355 | St. Petersburg, | 925.87 | -0.2982161 |
| Helsingfors, | -6 481.32 | $-0.2833486$ | Sydney, | -15 131212.77 | -0.6341758 |
| Hudson,* | +0 1732.06 | $+0.0121766$ | Upsala, | - 61842.70 | -0.2629942 |
| Kasan, | -8 2441.14 | $-0.3501761$ | Utrecht, | - 52843.67 | -0.2282832 |
| Königsberg, | -6 3011.87 | -0.2709707 | Vienna, | - 61344.09 | $-0.2595381$ |
| Kremsmunster, | -6 4 <br> 15.03  | -0.2532990 | Wilna, | - 64923.33 | -0.281297 |


| Number of Days clapsed since the lieginning of the Jutian Period, at the Date Jan. 0 in Common Years, and Jun. 1 in Bisscatilc Years. |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year. | Date in Mean Solar Days. | Year. | 1) ato in MeanSoiar Days. | $\begin{aligned} & \text { PrAR IN } \\ & \text { THE CENTEL } \end{aligned}$ |  | $\begin{gathered} \text { Das from } \\ \text { prevtous } \\ \text { Centminal } \\ \text { Date. } \end{gathered}$ | TEAR in THE CENTURY |  | $\begin{aligned} & \text { Days from } \\ & \text { previons Cen- } \\ & \text { teunial Date. } \end{aligned}$ |
|  |  |  |  | If Negative. | If Ponitive. |  | If Niggative. | If Positive. |  |
| -171313. | 0 | $-1000$ | 1356173 | 100 | 1 | 0 | 50 | 51 | 18262 |
| -1712 | 365 | -900 | 139:698 | 99 | 2 | 365 | 49 B . | $52 B$. | 18628 |
| - 1711 | 730 | - 800 | 1129:2:3 | 98 | 3 | 780 | 48 | 53 | 18993 |
| - 1710 | 1095 | - 700 | 1465718 | 9713. | $4 B$. | 1096 | 47 | 51 | 19358 |
| $-170913$. | 1161 | - 600 | 150®273 | 96 | 5 | 1461 | 46 | 55 | 197:3 |
| -4708 | 1820 | -500 | 1538798 | 95 | 6 | 1826 | 45 B. | 56 B. | 20089 |
| -4707 | 2191 | - 400 | 1575323 | 94 | 7 | 2191 | 44 | 57 | 20.51 |
| $-1706$ | 25.56 | - 300 | 1611818 | 93 B . | 8 B. | 2557 | 43 | 58 | 20819 |
| $-470.5 B$. | 2922 | - 200 | 16.18373 | 92 | 9 | 2922 | 42 | 59 | 2118.4 |
| -4704 | $3: 57$ | $-100$ | 1681898 | 91 | 10 | 32 ¢7 | 418. | 60 B. | 21550 |
| -4:03 | 3652 | 1 | $1721 / 123$ | 90 | 11 | 3652 | 40 | 61 | 21915 |
| -4702 | 4017 | 101 | $175 \%$ a 18 | 89 B. | $1: B$. | 4018 | 39 | 62 | 22280 |
| $-47013$. | 4383 | 201 | 1791473 | 88 | 13 | 4383 | 38 | 63 | 22645 |
| - $4 \% 00$ | 4748 | 301 | $18: 30998$ | 87 | 14 | 4748 | 37 Br . | 618. | 23011 |
| $-4600$ | 41273 | 401 | 18675:3 | 86 | 15 | 5113 | 36 | 65 | 23376 |
| $-4500$ | 77798 | 501 | 1904018 | $85 B$. | $16 B$. | 5179 | 35 | 66 | 23741 |
| $-4100$ | 1143:3 | 601 | 1910573 | 8.1 | 17 | 5814 | 34 | 67 | 24106 |
| -4300 | 150818 | 701 | 1977098 | 83 | 18 | 6209 | 33 B . | $68 B$. | 24472 |
| -1200 | 187373 | 801 | 2013623 | 82 | 19 | 6574 | 33 | 69 | 21837 |
| - 4100 | $2 \because 3898$ | 901 | 2050148 | 81 B . | 20 B . | 69.10 | 31 | 70 | 25202 |
| - 1000 | 260123 | 1001 | 2086673 | 80 | 21 | 7305 | 30 | 71 | 25567 |
| -3900 | 296948 | 1101 | $\stackrel{123198}{ }$ | 79 | 2. | 7670 | 29 B . | $72 B$. | 25933 |
| - 3800 | 333473 | 1201 | 2159723 | 78 | 23 | 8035 | 28 | 73 | 26298 |
| -3700 | 369998 | 1501 | 2196218 | 77 B . | $21 B$. | 8401 | 27 | 74 | 26663 |
| -3600 | 406523 | 1401 | 2232773 | 76 | 25 | 8766 | 26 | 75 | 27028 |
| $-3500$ | 4130.18 | 1501 | 2269298 | 75 | 26 | 9131 | 2513. | 76 B. | 27394 |
| -3100 | 479573 | 1583 | 2299238 | 74 | 27 | 9196 | 21 | 71 | 27759 |
| -3300 | 516098 | 15818. | 2299604 | 73 B . | $28 B$. | 9862 | 23 | 78 | 28124 |
| -3200 | 552623 | 1585 | 2299969 | 72 | 29 | 10227 | 22 | 79 | 28489 |
| $-3100$ | 589148 | 1586 | 2300331 | 71 | 30 | 10592 | 21 B. | 80 B . | 28855 |
| -3000 | 625673 | 1587 | 2300699 | 70 | 31 | 10957 | 20 | 81 | 29220 |
| -2900 | 66:198 | 1588 B. | 2301065 | 69 B. | $32 B$. | 11323 | 19 | 82 | 29585 |
| -2800 | 698723 | 1589 | 2301430 | 68 | 33 | 11688 | 18 | 83 | 29950. |
| -2700 | 735218 | 1590 | 2301795 | 67 | 31 | 12053 | $17 B$. | 84 B . | 30316 |
| -2600 | 771773 | 1591 | 2302160 | 66 | 35 | 12118 | 16 | 85 | 30681 |
| -2500 | 808:98 | $1592 B$. | 2302526 | 6518. | 36 B . | 12781 | 15 | 86 | 31046 |
| -2100 | 811823 | 1593 | 2302891 | 64 | 37 | 13149 | 14 | 87 | 31411 |
| -2300 | 881318 | 1591 | 2303256 | 63 | 38 | 13514 | 133. | $88 B$. | 31777 |
| -2200 | 917873 | 1595 | 2303621 | 62 | 39 | 13879 | 12 | 89 | 32142 |
| -2100 | 951398 | $1596 B$. | 2303987 | 61 B. | 40 B . | 14215 | 11 | 90 | 32507 |
| -2000 | 990923 | 1597 | 2301352 | 60 | 41 | 14610 | 10 | - 91 | 32872 |
| -1900 | 1027.448 | 1598 | 2304717 | 59 | 42 | 14975 | 9 L. | 92 B . | 33238 |
| -1800 | 1063973 | 1599 | $230508:$ | 58 | 43 | 153310 | 8 | 93 | 33603 |
| -1700 | 1100198 | 1600 B . | 2305448 | $57 B$. | 44 B . | 15706 | 7 | 94 | 33968 |
| -1600 | 1137023 | 1601 | 2305813 | 56 | 45 | 16071 | 6 | 95 | 34333 |
| -1500 | 1173518 | 1701 | 2312337 | 55 | 46 | 16436 | $5 B$. | 96 B . | 31699 |
| -1400 | 1210073 | 1801 | 2378861 | 51 | 47 | 16501 | 4 | 97 | 35061 |
| $-1300$ | 1216598 | 1901 | 2415383 | $53 B$. | 48 B. | 17167 | 3 | 98 | 35429 |
| -1:200 | 1283123 | 2001 | 2451910 | 53 | 49 | 1753: | 9 | 99 | 3579.1 |
| -1100 | 1319648 | 2101 | 218843.1 | 51 | 50 | 17899 | 11. | 100B. | 36160 |
| -1000 | 1358173 | 2201 | 2524958 | 50 | 51 | 18:6: |  | 100 | 36159 |

Number of Days from Jan. 0 in Common Iears, and Jan. 1 in Bissextite Years.


Reduction of Hours, Minutes, and Sicomels of Time to Decimals of a Day.

| Hours. | Decimal of a Day. | Min. | Decimal of a Day. | Min. | $\begin{aligned} & \text { Decimal of a } \\ & \text { Day. } \end{aligned}$ | Sec. | $\begin{aligned} & \text { Decimal of it } \\ & \text { Day. } \end{aligned}$ | Scc. | $\begin{gathered} \text { Decimal of a } \\ \text { Day. } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.0116667 | 1 | 0.0006914 | :31 | 0.0215:278 | 1 | 0.0000116 | 31 | 0.0003.388 |
| 2 | 0.081333:33 | 2 | 0.0013889 | 32 | $0.020^{2}$ | 2 | $0.0000: 31$ | 3: | 0.0003701 |
| 3 | 0.1250000 | 3 | 0.00:20833 | 33 | $0.02: 29167$ | 3 | 0.0000317 | 33 | 0.0003819 |
| 4 | 0.1666667 | 1 | 0.0027778 | 31 | 0.0236111 | 4 | 0.0000163 | 31 | 0.00039395 |
| 5 | 0.2083333 | 5 | 0.0031722 | 35 | 0.0213056 | 5 | 0.0000579 | 35) | 0.0001051 |
| 6 | 0.2500000 | 6 | 0.0011667 | 36 | 0.0250000 | 6 | 0.0000691 | 36 | 0.000 .1167 |
| 7 | 0.2916667 | 7 | 0.00 .18611 | 37 | 0.02569 .11 | 7 | 0.0000810 | :37 | 0.000-128: |
| 8 | 0.3:3333:33:3 | 8 | 0.0055556 | 38 | 0.020613889 | 8 | 0.0000926 | 38 | 0.0004398 |
| 9 | 0.37 .50000 | 9 | $0.006: 2500$ | 39 | 0.02708333 | 9 1 | 0.0001012 | 39 | 0.0001514 |
| 10 | 0.1166667 | 10 | 0.006944 | 40 | 0.027775 | 10 | 0.0001157 | 40 | 0.0001630 |
| 11 | $0.45833: 333$ | 11 | 0.0076389 | 41 | 0.0284722 | 11 | 0.0001273 | 41 | 0.0001745 |
| 12 | 0.5000000 | 12 | 0.00833333 | 42 | 0.0291667 | 12 | 0.0001389 | 4. | 0.0001861 |
| $1: 3$ | 0.5116667 | 13 | 0.0090278 | 43 | 0.0298611 | 13 | $0.000150 \%$ | 43 | 0.000497 |
| 11 | 0.58:3:33:33 | 14 | 0.0097292 | 44 | 0.0305556 | 14 | 0.000160 | 4. | 0.0005093 |
| 15 | 0.6250000 | 15 | 0.0104167 | 45 | 0.0312500 | 15 | 0.0001736 | 45 | 0.0005208 |
| 16 | 0.6666667 | 16 | 0.0111111 | 45 | 0.0319414 | 16 | 0.0001852 | 46 | 0.0005321 |
| 17 | 0.70833333 | 17 | 0.0118056 | 47 | 0.03:6389 | 17 | 0.0001968 | 47 | $0.00051 \cdot 10$ |
| 18 | 0.7500000 | 18 | $0.012 \% 000$ | 48 | 0.0333333 | 18 | 0.0002083 | 48 | 0.0005555 |
| 19 | 0.7916667 | 19 | 0.0131941 | 49 | 0.0340278 | 19 | 0.0002199 | 49 | 0.0005671 |
| 20 | 0.83333333 | 20 | 0.0138889 | 50 | 0.0317222 | 20 | 0.0002315 | 50 | 0.0005787 |
| 21 | 0.8750000 | 21 | 0.0145833 | 51 | 0.0351167 | 21 | 0.0002131 | 51 | 0.0005903 |
| 2\% | 0.9166667 | 22 | 0.0159778 | 52 | 0.0361111 | 22 | 0.0002516 | 52 | 0.0006019 |
| 23 | 0.958833833 | 23 | 0.015972: | 53 | 0.0368056 | 23 | 0.0002662 | 53 | 0.0006134 |
| 21 | 1.0000000 | 24 | 00166667 | 51 | 0.0375000 | 24 | 0.0002778 | 51 | 0.0006250 |
|  |  | 25 | 0.0173611 | 55 | 0.0381914 | 25 | 0.0002894 | 55 | 0.0006366 |
|  |  | 26 | 0.0180556 | 56 | 0.0388889 | 26 | 0.0003009 | 56 | 0.0006481 |
|  |  | 27 | 0.0187500 | 57 | 0.0395833 | 27 | 0.0003125 | 57 | 0.0006597 |
|  |  | 28 | 0.0194444 | 58 | 0.040:2778 | 28 | 0.0003241 | 58 | 0.0006713 |
|  |  | 29 | 0.0201389 | 59 | 0.0109722 | 29 | 0.0003356 | 59 | 0.0006829 |
|  |  | 30 | 0.0:08333 | 60 | 0.0116667 | 30 | 0.0003472 | 60 | 0.00069 .4 |

## TABLEV.

Periods of the Arguments with their multiples.

|  | 1 Period. | 2 Perinds. | 3 Periods. |
| :---: | :---: | :---: | :---: |
| Argrument 1 | 22.4 .7008 | $449^{\text {d }} .4016$ | $674{ }^{\text {d }} 1023$ |
| "\% 11 | 2385.9 | 4775.8 | 7165.8 |
| " III | 11987 ${ }^{1 .}$ | $23974{ }^{\text {d }}$. | $3596{ }^{\text {d }}$. |
| " IV | $2959{ }^{4}$ | $5918^{\text {4 }}$. | $8878{ }^{\text {d }}$ |
| " V | $145.1^{\text {d }} .9$ | $2909{ }^{4} .9$ | $4364^{4} .8$ |
| VI | $583{ }^{4.92}$ | $1167^{4.84}$ | $17.51^{\text {d }} .76$ |
| " VII | $2.433^{1.16}$ | $486{ }^{4} .33$ | $729^{1} .49$ |
| " VIII | $2200^{4} .6$ | $440{ }^{1} .1$ | $661{ }^{1 / .7}$ |
| IX | $236^{4} .99$ | $473{ }^{\text {d }} .98$ | $710^{\text {d }} .98$ |
| X | 60 units | 120 units | 180 units |
| " XI | 240 units | 480 units | 720 units |
| " XII | 60 units | 120 units | 180 units |
| XIII | 60 units | 120 units | 180 units |
| ". XIV | 36 units | 72 units | 108 units |
| " XV | $6799^{\text {c }}$. 3 | $135.96{ }^{4} .5$ | $2039.1{ }^{1 / 8}$ |
| " XVI | $365{ }^{1.2}$ | $730{ }^{\text {d }} .5$ | 1095'.7 |

Inercments of Arguments X-XIV for un inerease of 1,2 and 3 in the integer 1月4.

|  | Increment of $\mathrm{m}=1$. | Increment of $m=2$. | Increment of $m=3$. |
| :---: | :---: | :---: | :---: |
| Argument X | 33.26 | 6.52 | 39.78 |
| " XI | 147.64 | 55.29 | 20:.93 |
| " XII | 19.6 | 39.3 | 58.9 |
| " XIII | 3.11 | 6.22 | 9.3 .4 |
| " XIV | 0.8 | 1.5 | 2.3 |
|  |  |  |  |

Mean Longitude, Arguments, \&.c., for W'ashington Mean Noon of Jan. 0 in common years, Jan. 1 in bisscxitilc years.

| Year. | $L$ | nin. | I. | 11. | 111. | IV. | V. | VI. | VII. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1750 | $45^{\circ} 54 \quad$ "124 | -163 | 173.9096 | 67.9 | $11212^{\text {a }}$ | $2103^{41}$ | 611.5 | 497.08 | 31.2 |
| 1751 | 2704131.89 | 161 | 89.5080 | 68.9 | 11607 | 2768 | 976.5 | 278.16 | 153.0 |
| $1752 B$. | $\begin{array}{lllll}137 & 5 & 12.35\end{array}$ | 159 | 6.1064 | 69.9 | 11973 | 175 | 1342.5 | 60.24 | 32.7 |
| 1753 | 15242.00 | 158 | 146.4056 | 70.9 | 351 | 540 | 252.5 | 425.21 | 154.5 |
| 1754 | 2264011.66 | 156 | 62.0010 | 71.9 | 716 | 905 | 617.5 | 206.32 | 33.2 |
| 1755 | 912741.31 | $-15.5$ | 202.3032 | 72.9 | 1081 | 1270 | 982.5 | 571.32 | 155.0 |
| $1756 B$. | 3175118.77 | 153 | 118.9016 | 73.9 | 1447 | 1636 | 1348.5 | 353.40 | 34.7 |
| $1 \% .57$ | 1823848.42 | 151 | 31.5000 | 74.9 | 1812 | 2001 | 258.6 | 134.48 | 156.5 |
| 17.58 | 472618.08 | 150 | 174.7993 | 75.9 | 2177 | 2366 | 623.6 | 499.48 | 35.2 |
| 1759 | 2721347.73 | 148 | 90.3977 | 76.9 | 2542 | 2731 | 988.6 | 280.56 | 157.1 |
| 1760 B . | 1383725.19 | -146 | 6.9961 | 77.9 | 2908 | 137 | 1354.6 | 62.63 | 36.7 |
| 1761 | 32454.84 | 145 | 147.2953 | 78.9 | 3273 | 502. | 264.7 | 427.63 | 158.6 |
| 1762 | 2281224.50 | 143 | 62.8937 | 79.9 | 3638 | 867 | 629.7 | 208.71 | 37.2 |
| 1763 | 925954.15 | 142 | 203.1929 | 80.9 | 4003 | 1232 | 994.7 | 573.71 | 155.1 |
| $1764 B$. | 3192331.61 | 140 | 119.7913 | 81.9 | 4369 | 1598 | 1360.7 | 355.79 | 38.7 |
| 1765 | 184111.27 | -138 | 35.3898 | 82.9 | 4734 | 1963 | 270.7 | 136.87 | 160.6 |
| 1766 | 485830.92 | 137 | 175.6890 | 83.9 | 5099 | 2328 | 635.7 | 501.87 | 39.2 |
| 1767 | 273460.58 | 135 | 91.2874 | 84.9 | 5464 | 2693 | 1000.7 | 282.95 | 161.1 |
| 1768 B. | 140 | 133 | 7.8858 | 85.9 | 5830 | 100 | 1366.7 | 65.03 | 40.7 |
| 1769 | $457 \quad 7.69$ | 132 | 148.1850 | 86.9 | 6195 | 465 | 276.8 | 430.03 | 162.6 |
| 1770 | 2294437.35 | -130 | 63.7834 | 87.9 | 6560 | 830 | 641.8 | 211.11 | 41.3 |
| 1771 | 94327.00 | 129 | 204.0826 | 88.9 | 6925 | 1195 | 1006.8 | 576.11 | 163.1 |
| $1772 B$. | 3205544.47 | 127 | 120.6811 | 89.9 | 7291 | 1561 | 1372.8 | 358.18 | 42.8 |
| 1773 | 1854314.12 | 125 | 36.2795 | 90.9 | 7656 | 1926 | 282.9 | 139.26 | 164.6 |
| 1774 | $50 \quad 3043.78$ | 124 | 176.5787 | 91.9 | 8021 | 2291 | 617.9 | 504.26 | 43.3 |
| 1775 | 2751813.43 | -122 | 92.1771 | 92.9 | 8386 | 2656 | 1012.9 | 285.31 | 165.1 |
| 1776 B . | 1414150.89 | 120 | 8.7755 | 93.9 | 8752 | 63 | 1378.9 | 67.42 | 44.8 |
| 1777 | 62920.55 | 119 | 149.0748 | 94.9 | 9117 | 428 | 288.9 | 432.42 | 166.6 |
| 1778 | 2311650.21 | 117 | 64.6732 | 95.9 | 9482 | 793 | 653.9 | 213.50 | 45.3 |
| 1779 | $\begin{array}{llll}96 & 4 & 19.86\end{array}$ | 116 | 204.9724 | 96.9 | 9847 | 1158 | 1018.9 | 578.50 | $16 \% .1$ |
| 1780 B . | 3222757.32 | -114 | 121.5708 | 97.9 | 10213 | 1524 | 1384.9 | 360.58 | 46.8 |
| 1781 | 1871526.98 | 112 | 37.1692 | 98.9 | 10578 | 1889 | 295.0 | 141.66 | 168.6 |
| 1782 | 52.256 .64 | 111 | 177.4684 | 99.9 | 10943 | 2254 | 660.0 | 506.66 | 47.3 |
| 1783 | 2765026.29 | 109 | 93.0669 | 100.9 | 11308 | 2619 | 1025.0 | 287.74 | 169.1 |
| 1781 B. | $\begin{array}{llll}143 & 14 & 3.76\end{array}$ | 107 | 9.6653 | 101.9 | 11674 | 26 | 1391.0 | 69.81 | 48.8 |
| 1785 | $8 \quad 133.41$ | -106 | 149.9645 | 102.9 | 52 | 391 | 301.0 | 434.81 | 170.6 |
| 1786 | 23249 | 104 | 65.5629 | 103.9 | 417 | 756 | 666.0 | 215.89 | 49.3 |
| 1787 | 973632.73 | 103 | 205.8621 | 104.9 | 782 | 1121 | 1031.0 | 580.89 | 171.1 |
| $1788 B$. | $\begin{array}{lll}321 & 0 & 10.19\end{array}$ | 101 | 122.4605 | 105.9 | 1148 | 1487 | 1397.0 | 362.97 | 50.8 |
| 1789 | 1884739.85 | 99 | 38.0590 | 106.9 | 1513 | 1852 | 307.1 | 144.05 | 172.6 |
| 1790 | 53359.51 | -98 | 178.3582 | 107.9 | 1878 | 2217 | 672.1 | 509.05 | 51.3 |
| 1791 | 2782239.16 | 96 | 93.9566 | 108.9 | 2243 | 2582 | 1037.1 | 290.13 | 173.1 |
| 1792 B. | 1444616.63 | 94 | 10.5551 | 109.9 | 2609 | 2948 | 1403.1 | 72.21 | 52.8 |
| 1793 | 93346.28 | 93 | 150.8513 | 110.9 | 2974 | 354 | 313.2 | 437.21 | 174.6 |
| 1794 | 2342115.94 | 91 | 66.4527 | 111.9 | 3339 | 719 | 678.2 | 218.29 | 53.3 |
| 1795 | $99 \quad 845.60$ | - 90 | 206.7519 | 112.9 | 3704 | 1084 | 1043.2 | 583.29 | 175.2 |
| $1796 B$. | 3253223.07 | 88 | 123.3503 | 118.9 | 4070 | 1450 | 1409.2 | 365.36 | 54.8 |
| 1797 | $\begin{array}{llll}190 & 19 & 52.72\end{array}$ | 86 | 38.9488 | 114.9 | 4435 | 1815 | 319.2 | 146.44 | 176.7 |
| 1798 | $55 \quad 782.38$ |  | 179.2480 | 115.9 | 4800 | 2180 | 681.2 | 511.44 | 55.3 |
| 1799 | 2795452.04 | -83 | 94.8164 | 116.9 | 5165 | 2545 | 1049.2 | 292.52 | 177.2 |


| Year. | VIII. | Ix. | X | XI. | XII. | XIII. | Niv. | Log. sin i. | $350^{\circ}-8$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 17.50 | 55.9 | 28.28 | 43.96 | 193.18 | 48.7 | 58.45 | 22.7 | 8.7720788 | $285{ }^{3} 31416.8$ |
| 1731 | 200.3 | 156: | 50.18 | 8.77 | 28.0 | 4.67 | 24.2 | 0802 | ${ }_{313} 11.3$ |
| 1752b. | 125.2 | 48.30 | 56.99 | ${ }_{61.06}$ | $7:$ | 10.89 | 25.7 | 0815 | 3311.8 |
| 1753 | 19.1 | 176.31 | 30.25 | 211.70 | 26.9 | 14.01 | 26.5 | 0s:29 | 3239.3 |
| 1754 | 193.5 | 67.3:3 | 36.77 | 26.99 | 6.1 | 20.23 | 28.0 | 0812 | 32 6.9 |
| 175.5 | 117.1 | 195.34 | 10.03 | 171.63 | 25.7 | 23.31 | 28.7 | 8.7720856 | 28.3131 .4 |
| 175673. | 42. 2. | 87.35) | 16.55 | 229.9\% | 5.0 | 29.56 | 30.2 | 0870 | $\begin{array}{lll}31 & 1.8 \\ 30\end{array}$ |
| 17.57 | 186.7 | 215.36 | 23.06 | 45.21 | 41.2 | 35.79 | 31.7 | 0888 | 3029.4 |
| 17.58 | 110.5 | 106.38 | 56.39 | 192.86 | 3.9 | 38.90 | 32.5 | 0897 | 2955.9 |
| 1759 | 31.4 | 231.38 | 2.81 | 8.15 | 43.1 | 45.12 | 34.0 | 0911 | 2921.4 |
| 1760 B. | 179.8 | 12 C .10 | 9.36 | 63.41 | 22.4 | 51.35 | 33.5 | 8.7720924 | 2852851.9 |
| 1761 | 103.7 | 17.12 | 42.62 | 211.08 | 42.0 | 51.46 | 0.2 | 0938 | 2819.1 |
| 1762 | 27.6 | 145.43 | 49.13 | 26.37 | 21.2 | 0.68 | 1.7 | 0951 | ${ }^{27} 47.0$ |
| 1763 | 172.0 | 36.44 | 22.39 | 174.02 | 40.9 | 3.79 | 2.5 | 0965 | $\stackrel{27}{ } 14.5$ |
| 1761 B. | 96.9 | 165.15 | 28.91 | 229.31 | 20.1 | 10.02 | 4.0 | 0979 | 2641.9 |
| 1765 | 20.7 | 56.47 | 35.43 | 44.60 | 59.4 | 16.24 | 5.5 | 8.7720992 | $285 \quad 269.5$ |
| 1766 | 16.5 .2 | 181.47 | 8.68 | 192.21 | 19.0 | 19.35 | 6.2 | 1006 | 2537.0 |
| 1767 | 89.0 | 75.49 | 15.20 | 7.53 | 58.2 | 25.58 | 7.7 | 10:0 | 254.5 |
| 17683 B. | 13.9 | 201.50 | 21.72 | 62.82 | 37.5 | 31.80 | 9.2 | 1033 | 2432.0 |
| 1769 | 15.4 | 95.51 | 51.98 | 210.46 | 57.1 | 31.91 | 10.0 | 1017 | 2359.5 |
| 17\%0 | 82.2 | 223.52 | 1.19 | 25.75 | 36.4 | 41.14 | 11.5 | 8.7721080 | 2852327.0 |
| 1771 | 6.1 | 114.51 | 34.75) | 173.10 | 56.0 | 44.25 | 12.3 | 1071 | 2.2 51.6 |
| 17728. | 151.5 | 6.55 | 41.27 | 228.69 | 35.2 | 50.47 | 13.8 | 1088 | 2222.0 |
| 1773 1774 | 75.1 219.8 | $\begin{array}{r}134.56 \\ 25.58 \\ \hline\end{array}$ | ${ }_{21.05}^{47.79}$ | 43.98 191.62 | 14.5 31.1 | 56.69 59.81 | 15.0 | 11115 | ${ }_{21} 214.17$ |
| 1775 | 143.7 | 153.59 | 27.56 | 6.91 | 13.4 | 6.03 | 17.5 | 8.7721128 | 2852044.6 |
| 1776 B. | 68.6 | 45.60 | 31.08 | 62.20 | 52.6 | 12.25 | 19.0 | 1142 | 2012.1 |
| 1777 | 213.0 | 173.61 | 7.31 | 209.85 | 12.2 | 15.37 | 19.8 | 1156 | 1939.6 |
| 1778 | 136.9 | 61.63 | 13.86 | 25.14 | 51.5 | 21.59 | 21.3 | 1169 | 197.1 |
| 1779 | 60.7 | 192.64 | 47.12 | 17278 | 11.1 | 24.70 | 22.0 | 1183 | 1831.6 |
| 1780B. | 206.2 | 81.65 | 53.63 | 228.07 | 50.4 | 30.92 | 23.5 | 8.7721197 | $28518 \quad 2.1$ |
| 1781 | 130.0 | 212.66 | 0.15 | 43.26 | 29.6 | 37.15 | 25.0 | 1210 | 1729.6 |
| 178\% | 53.9 | 103.68 | 33.41 | 191.00 | 49.2 | 40.26 | 25.8 | 1224 | 1657.1 |
| 1783 | 199.3 | 231.68 | 39.93 | 6.29 | 28.5 | 46.48 | 27.3 | 1237 | 1621.7 |
| 17843. | 123.2 | 123.70 | 46.44 | 61.58 | 7.7 | 52.71 | 28.8 | 1251 | 1552.1 |
| 1785 | 47.1 | 14.72 | 19.70 | 209.23 | 27.4 | 55.82 | 29.5 | 8.7721265 | 2851519.6 |
| 1786 | 191.5 | 142.72 | 20.22 | 21.52 | 6.6 | 2.04 | 31.1 | 1278 | 1447.1 |
| 1787 | 115.4 | 33.74 | 59.48 | 172.16 | 20.2 | 5. 15 | 31.8 | 1292 | 1414.7 |
| 1788 B. | 40.2 | 162.75 | 6.00 | 227.45 | 5.5 | 11.38 | 33.3 | 1306 | 1342.1 |
| 1789 | 181.7 | 53.76 | 12.51 | 42.74 | 41.7 | 17.60 | 34.8 | 1319 | $13 \quad 9.6$ |
| 1790 | 108.5 | 181.77 | 45.77 | 190.39 | 4.4 | 20.71 | 35.6 | 8.7721333 | 2851237.2 |
| 1791 | 32.4 | 72.79 | 52.29 | 5.68 | 43.6 | 26.91 | 1.1 | 1316 | 124.7 |
| 17923. | 177.8 | 201.80 | 58.81 | 60.97 | 22.9 | 33.16 | 2.6 | 1360 | 1132.1 |
| 1793 | 101.7 | 92. 81 | 32.06 | 208.61 | 42.5 | 36.27 | 3.3 | 1374 | 1059.7 |
| 1791 | 25.6 | 220.82 | 38.58 | 23.90 | 21.7 | 42.50 | 4.8 | 1387 | 1027.2 |
| 1795 | 170.0 | 111.81 | 11.84 | 171.54 | 41.4 | 45.61 | 5.6 | 8.7721401 | 28.5951 .7 |
| 1796 B. | 91.9 | 3.85 | 18.36 | 226.83 | 20.6 | 51.83 | 7.1 | - 1415 | 922.1 |
| 1797 | 18.7 | 131.86 | 24.87 | 42.12 | 59.9 | 58.05 | 8.6 | 1428 | 849.7 |
| 1798 | 163.2 | 22. 88 | 58.13 | 189.77 | 19.5 | 1.17 | 9.3 | 1412 | 817.2 |
| 1799 | 87.0 | 150.89 | 4.65 | 5.06 | 58.7 | 7.39 | 10.8 | 8.7721456 | $285 \quad 741.7$ |

Mean Longitude, Arguments, (fe., for Wushington Moren Noon of Jan. 0 in comuron years, Jun. 1 in bissextile yeurs.

| Year. | $L$. | 512. | I. | II. | III. | IV. | V. | VI. | VII. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1800 | 114 4: 21.70 | -81 | 10.4 .48 | 117.9 | 5530 | $2910^{\text {a }}$ | 1414.4 | 733.60 | 50.8 |
| 1801 | 92951.36 | 80 | 150.7.41 | 118.9 | 5895 | 315 | 324.3 | 438.60 | 177.7 |
| 180: | 2311721.02 | 78 | 66.3125 | 119.9 | 6260 | 680 | 689.3 | 219.68 | 56.3 |
| 1803 | $99 \quad 450.67$ | 77 | 206.6117 | 120.9 | 6625 | 1015 | 1054.3 | 0.76 | 178.2 |
| $1804 B$. | 3252828.14 | 75 | 123.2101 | 121.9 | 6991 | 1411 | 1420.3 | 366.76 | 57.8 |
| 1805 | $190 \quad 15 \quad 57.80$ | -73 | 38.8386 | 122.9 | 7356 | 1776 | 330.4 | 147.84 | 179.7 |
| 1803 | $\begin{array}{llll}55 & 3 & 27.46\end{array}$ | 72 | 179.1378 | 123.9 | 77:1 | 2141 | 695.4 | 512.84 | 58.3 |
| 1807 | $\begin{array}{lllllllllllll}279 & 50 & 57.12\end{array}$ | 70 | 94.7362 | 121.9 | 8086 | 2503 | 1060.4 | 293.91 | 180.2 |
| 180813. | 1461431.58 | 68 | 11.3316 | 125.9 | 815: | 287: | 1426.4 | 75.99 | 59.9 |
| 1809 | 11 2 4.24 | 67 | 151.6339 | 1:6.9 | 8817 | 278 | 336.4 | 410.99 | 181.7 |
| 1810 | 2354933.30 | -65 | 67.2323 | 127.9 | 9182 | 613 | 701.4 | 222.07 | 60.4 |
| 1811 | $10037 \quad 3.56$ | 61 | 207.5315 | 128.9 | 9547 | 1008 | 1066.4 | 3.15 | 182.2 |
| 1812B. | $327 \quad 041.03$ | 62 | 124.1299 | 129.9 | 9913 | 1374 | 1433.4 | 369.15 | 61.9 |
| 1813 | 1914810.69 | 60 | 39.7284 | 130.9 | 10278 | 1739 | 342.5 | 150.23 | 183.7 |
| 181.4 | 563540.35 | 59 | 180.0276 | 131.9 | 10643 | 2104 | 707.5 | 515.23 | 62.4 |
| 1815 | 2812310.01 | -57 | 95.6260 | 132.9 | 11008 | 2469 | 1072.5 | 296.31 | 184.2 |
| $1816 B$. | 1474647.47 | 55 | 12.2215 | 133.9 | 11374 | 2835 | 1438.5 | 78.39 | 63.9 |
| 1817 | 123178.13 | 51 | 152.5237 | 134.9 | 11739 | 241 | 348.6 | 443.39 | 185.7 |
| 1818 | 2372146.79 | 52 | 68.1221 | 135.9 | 116 | 606 | 713.6 | 224.46 | 64.4 |
| 1819 | 102916.45 | 51 | 208.4213 | 136.9 | 481 | 971 | 1078.6 | 5.54 | 186.2 |
| 1820 B . | 3283253.92 | -49 | 125.0198 | 137.9 | 847 | 1337 | 1444.6 | 371.54 | 65.9 |
| $18: 1$ | 1932023.58 | 47 | 40.6182 | 138.9 | 1212 | 1702 | 354.6 | 152.6: | 187.7 |
| 18:2 | 538503.24 | 46 | 180.9174 | 139.9 | 1577 | 2067 | 719.6 | 517.62 | 66.4 |
| 18:3 | $2825.52: 20$ | 41 | 96.5159 | 140.9 | 1942 | 243: | 1084.6 | 298.70 | 188.2 |
| 18:1 $B$. | $149 \quad 19 \quad 0.37$ | 42 | 13.1143 | 141.9 | 2308 | 2798 | 1450.6 | 80.78 | 67.9 |
| 1825 | 14630.03 | -41 | 153.4135 | 142.9 | 2673 | 204 | 360.7 | 445.78 | 189.7 |
| 18:2 6 | 2385359.69 | 39 | 69.0119 | 143.9 | 3038 | 569 | 725.7 | 226.86 | 68.4 |
| $18: 7$ | 1034129.36 | 38 | 209.3112 | 14.9 | 3103 | 931 | 1090.7 | 7.94 | 190.2 |
| 18:8B. | $330 \quad 5 \quad 6.82$ | 36 | 125.9096 | 145.9 | 3769 | 1300 | 1.8 | 373.94 | 69.9 |
| $18: 9$ | 1945230.49 | 31 | 41.5080 | 146.9 | 4134 | 1665 | 366.8 | 155.02 | 191.7 |
| 1830 | 5940 6.15 | -33 | 181.8073 | 147.9 | 4199 | 2030 | 731.8 | 520.02 | 70.4 |
| 1831 | 2842735.81 | 31 | 97.4057 | 148.9 | 4861 | 2395 | 1096.8 | 301.09 | 192.2 |
| 1832 B. | 1505113.28 | 29 | 14.0041 | 149.9 | 5230 | 2761 | 7.8 | 83.17 | 71.9 |
| 1833 | 153842.91 | 28 | 151.3031 | 150.9 | 5595 | 167 | 372.8 | 448.17 | 193.8 |
| 1831 | 2402612.60 | 26 | 69.9018 | 151.9 | 5960 | 532 | 737.8 | 229.25 | 72.4 |
| 1835 | 1051349.27 | -25 | 210.2010 | 152.9 | 6325 | 897 | 1109.8 | 10.33 | 194.3 |
| 183613. | 3313719.73 | 23 | 126.7995 | 153.9 | 6691 | 1263 | 13.9 | 376.33 | 73.9 |
| 1837 | 1962449.40 | 21 | 42.3979 | 151.9 | 7056 | 1628 | 378.9 | 157.41 | 195.8 |
| 1838 | 611219.06 | 20 | 182.6971 | 155.9 | 7421 | 1993 | 743.9 | 522.41 | 74.1 |
| 1839 | 2855948.72 | 18 | 98.2956 | 156.9 | 7786 | 2358 | 1108.9 | 303.49 | 196.3 |
| 1810 B . | 1522326.19 | -16 | 14.8940 | 157.9 | 8152 | 2724 | 19.9 | 85.57 | 75.9 |
| 1811 | 171055.86 | 15 | 15.1932 | 158.9 | 8517 | 129 | 384.9 | 450.57 | 197.8 |
| 1812 | 2415825.52 | 13 | 70.7917 | 159.9 | 8882 | 494 | 749.9 | 231.64 | 76.4 |
| 1813 | 1064555.18 | 12 | 211.0909 | 160.9 | 92.17 | 859 | 1114.9 | 12.72 | 198.3 |
| 181433. | 3331832.65 | 10 | 127.6893 | 161.9 | 9613 | 1225 | 26.0 | 378.72 | 77.9 |
| 1845 | $197 \quad 57 \quad 2.32$ | $-8$ | 43.2878 | 162.9 | 9978 | 1590 | 391.0 | 159.80 | 199.8 |
| 1816 | 624431.98 | 7 | 183.5870 | 163.9 | 10343 | 1955 | 756.0 | 524.80 | 78.5 |
| 1817 | 287321.65 | 5 | 99.1854 | 164.9 | 10708 | 2320 | 1121.0 | 305.88 | 200.3 |
| 181313. | 1535539.12 | 3 | 15.7839 | 165.9 | 11074 | 2686 | 32.1 | 87.96 | 80.0 |
| 1819 | 18438.78 | - 2 | 156.0831 | 166.9 | 11439 | 92 | 397.1 | 452.96 | 201.8 |

Mean Lontgitude, Arguments. de., for Trashington Mean Noon of Jan. 0 in common years, Jan. 1 in bissextile years.


Mean Longitude, Arguments, \&.c., for Washington Mean Noon of Jan. 0 in common years, Jan. 1 in bisscxtile ycars.

| Year. | $L$ | 13. | I. | II. | III. | IV. | V. | VI. | VII. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1850 | $2133^{30} 303$ | 0 | 71.6815 | 167.9 | $11801^{\text {a }}$ | $457{ }^{\text {d }}$ | 76.2 .1 | 234.04 | 80.5 |
| 1851 | 108188.11 | 1 | 211.9808 | 168.9 | 18: | 822 | 1127.1 | 15.12 | 20:.3 |
| $1852 B$. | 3314145.58 | 3 | 128.5792 | 169.9 | 518 | 1188 | 38.1 | 381.12 | 82.0 |
| 1853 | 1992915.25 | 5 | 44.1776 | 170.9 | 913 | 1553 | 40:3.1 | $16 \pm .19$ | 202.8 |
| 18.51 | $6 \pm 1641.92$ | 6 | 184.4769 | 171.9 | 1278 | 1918 | 768.1 | 527.19 | 82.5 |
| 1855 | $289-414.58$ | 8 | 100.0753 | 172.9 | 1613 | 2283 | 1133.1 | 308.27 | 201.3 |
| $1856 B$. | 1552750.05 | 10 | 16.6738 | 173.9 | 2009 | 26.19 | 41.2 | 90.35 | 81.0 |
| 1857 | 2015021.72 | 11 | 156.9730 | 171.9 | 2374 | 55 | 409.2 | 455.35 | 20.5 |
| 1858 | 245 : 51.39 | 13 | 72.5715 | 175.9 | 2739 | 420 | 774.2 | 2:36.43 | 84.5 |
| 1859 | 1095021.05 | 14 | 212.8707 | 176.9 | 3104 | 785 | 1139.2 | 17.51 | 206.3 |
| 1860 B . | :336 13 [58.53 | 16 | 129.4691 | 177.9 | 3450 | 1151 | 50.3 | 383.51 | 86.0 |
| 1861 | $201 \quad 128.19$ | 18 | 45.0675 | 178.9 | 3835 | 1516 | 415.3 | 164.59 | 207.8 |
| 1862 | $65 \quad 4857.86$ | 19 | 185.3668 | 179.9 | 4200 | 1881 | 780.3 | 529.59 | 86.5 |
| 1863 | 2903627.53 | 21 | $100.965^{\circ}$ | 180.9 | 4545 | 2246 | 1145.3 | 310.67 | 208.3 |
| $1861 B$. | $157 \quad 0 \quad 5.00$ | 23 | $17 \cdot 5937$ | 181.9 | 4931 | 2612 | 56.3 | 92.75 | 88.0 |
| 1865 | 214731.67 | 24 | 157.86:9 | 189.9 | 5296 | 18 | 421.3 | 457.75) | 209.8 |
| 1866 | 2163.54 .34 | 26 | 73.4613 | 183.9 | 5661 | 383 | 786.3 | 238.80 | 88.5 |
| 1867 | 1112231.00 | 27 | 213.7606 | 184.9 | 60:6 | 748 | 1151.3 | 19.90 | 210.3 |
| $1868 B$. | 33374611.48 | 29 | 130.3590 | 185.9 | 6392 | 1114 | 62.4 | 355.90 | 90.0 |
| 1869 | 20: 3341.15 | 31 | 45.9575 | 186.9 . | 6757 | 1479 | 427.4 | 166.98 | 211.8 |
| 1870 | 672110.82 | 32 | 186.2567 | 187.9 | 7122 | 1844 | 792.4 | 531.98 | 90.5 |
| 1871 | 29: 840.49 | 31 | 101.8551 | 188.9 | 7487 | 2209 | 1157.4 | 313.06 | 212.4 |
| 1872B. | 158 3: 17.96 | 36 | 18.4536 | 189.9 | 7853 | 2575 | 68.5 | 95.14 | 92.0 |
| 1873 | 231947.63 | 37 | 158.7528 | 190.9 | 8218 | 2910 | 433.5 | 460.14 | 213.9 |
| 1874 | $\begin{array}{lll}218 & 717.30\end{array}$ | 39 | 74.3513 | 191.9 | 8583 | 316 | 798.5 | 241.22 | 92.5 |
| 1875 | 1125446.97 | 40 | 214.6505 | 192.9 | 8948 | 711 | 1163.5 | 22.30 | 214.4 |
| 1876 B . | 3391824.45 | 42 | 131.2489 | 193.9 | 9314 | 1077 | 74.5 | 388.30 | 94.0 |
| 1877 | 2015 51.12 | 44 | 46.8474 | 194.9 | 9679 | 1442 | 439.5 | 169.37 | 215.9 |
| 1878 | $6853 \times 3.39$ | 45 | 187.1466 | 195.9 | 10044 | 1807 | 80.1 .5 | 534.37 | 91.5 |
| 1879 | 2934053.46 | 47 | 102.7451 | 196.9 | 10409 | 2172 | 1169.5 | 315.45 | 216.4 |
| 1880 B. | $160 \quad 430.94$ | 49 | 19.3135 | 197.9 | 10775 | 2538 | 80.6 | 97.53 | 96.0 |
| 1881 | 24520.61 | 50 | 159.6428 | 198.9 | 11140 | 2903 | 445.6 | 462.53 | 217.9 |
| 188: | 2493930.28 | 52 | 75.2412 | 199.9 | 11505 | 308 | 810.6 | 243.61 | 96.6 |
| 1883 | 1142659.95 | 53 | 215.5104 | 200.9 | 11870 | 673 | 1175.6 | 24.69 | 218.4 |
| $1884 B$. | $310 \quad 5037.43$ | 55 | 132.1389 | 201.9 | 249 | 1039 | 86.6 | 390.69 | 98.1 |
| 1885 | $20538 \quad 7.10$ | 57 | 47.7373 | 202.9 | 615 | 140.1 | 451.6 | 171.77 | 219.9 |
| 1886 | $70 \quad 2536.77$ | 58 | 188.0366 | 203.9 | 980 | 1769 | 816.6 | 536.77 | 98.6 |
| 1887 | 295136 | 60 | 103.63.50 | 204.9 | 1315) | 2131 | 1181.6 | 317.85 | 220.4 |
| 1888 B. | 1613643.93 | 62 | 20.2335 | 205.9 | 1711 | 2500 | 92.7 | 99.92 | 100.1 |
| 1889 | 262113.60 | 63 | 160.53:27 | 206.9 | 2076 | 2865 | 457.7 | 461.92 | 221.9 |
| 1890 | 2511143.27 | 65 | 76.1312 | 207.9 | 2141 | 271 | 82.27 | 246.00 | 100.6 |
| 1891 | 1155912.95 | 66 | 216.4301 | 208.9 | 2806 | 636 | 1187.7 | 27.08 | 202.1 |
| 189:B. | 3122250.43 | 68 | . 133.0289 | 209.9 | 3172 | 101\% | 98.8 | 393.08 | 102.1 |
| 1893 | 2071020.10 | 70 | 48.6273 | 210.9 | 3537 | 1367 | 463.8 | 174.16 | 223.9 |
| 1894 | 715749.78 | 71 | 188.9265 | 211.9 | 3902 | 1732 | 828.8 | 539.16 | 10:2.6 |
| 1895 | 2964519.45 | 73 | 104.5950 | 212.9 | 4267 | 2097 | 1193.8 | 320.24 | 221.4 |
| 189613. | $163 \quad 856.93$ | 75 | 21.1235 | 213.9 | 4633 | 2163 | 104.8 | 102.32 | 101.1 |
| 1897 | 275626.61 | 76 | 161.4227 | 214.9 | 4998 | 28:28 | 469.8 | 467.32 | 20.5 .9 |
| 1898 | 2524356.29 | 78 | 77.0211 | 215.9 | 5363 | 233 | 831.8 | 248.40 | 104.6 |
| 1899 | 1173125.96 | 79 | 217.3:0.1 | 216.9 | 57.28 | 599 | 1199.8 | 29.48 | 226.4 |

Mean Longitude, Arguments, \&•e, for Wrashington Mean Noon of Jan. 0 in common years, Jan. I in bissextile years.

$7 v$

Mean Longituck, Argunents, dec., for Wrashington Mean Noon of Jen. 0 in common years, Jan. 1 in bissextile years.

| Year. | $L$. | $n$. | 1. | II. | III. | IV. | V. | VI. | VII. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1900 | $24{ }^{2}$ | 81 | $13: 2.9188$ | 217.9 | $6093{ }^{\text {a }}$ | $964{ }^{\text {a }}$ | 109.9 | 391.48 | $10 \% .1$ |
| 1901 | 207625.31 | 83 | 48.5173 | 218.9 | 6458 | 1329 | 474.9 | 175.5.5 | 226.9 |
| 190: | 715351.99 | 81 | 188.8165 | 219.9 | 6823 | 1694 | 839.9 | 510.55 | 105.6 |
| 1003 | 2964121.67 | 86 | 104.4150 | $2 \because 0.9$ | 7188 | 2059 | 1201.9 | 321.63 | 227.4 |
| $1901 B$. | $163 \quad 5 \quad 2.15$ | 88 | 21.0134 | $2: 21.9$ | 7554 | 2425 | 116.0 | 103.71 | 107.1 |
| 1905 | 275231.83 | 89 | $161.31: 7$ | 22.9 | 7919 | 2790 | 481.0 | 468.71 | 228.9 |
| 1906 | $\begin{array}{llll}252 & 10 & 1.51\end{array}$ | 91 | 76.9111 | 223.9 | 8281 | 196 | 816.0 | 249.79 | 107.6 |
| 1907 | $117 \quad 27 \quad 31.19$ | 92 | 217.2104 | 221.9 | 86.19 | 561 | 1211.0 | 30.87 | 229.5 |
| $1908 B$. | 3438518.67 | 94 | 133.8058 | 225.9 | 9015 | 927 | 122.0 | 396.87 | 109.1 |
| 1909 | $208 \quad 3838.35$ | 96 | 49.40\%3 | $2 \geqslant 6.9$ | 9380 | 1:292 | 487.0 | 177.95 | 231.0 |
| 1910 | 73268.03 | 97 | 189.7065 | 227.9 | 9745 | 1657 | 852.0 | 51.95 | 109.6 |
| 1911 | 29813387.71 | 99 | 105.3050 | 228.9 | 10110 | 2022 | 1217.0 | 324.03 | 231.5 |
| 19128. | $161: 3715.20$ | 101 | 21.9031 | 229.9 | 10176 | 2388 | 128.1 | 106.10 | 111.1 |
| 1913 | 292141.88 | 102 | 16:.20:7 | 230.9 | 108.11 | 2753 | 493.1 | 471.10 | 233.0 |
| 1914 | 2511214.56 | 104 | 77.8011 | 231.9 | 11206 | 158 | 858.1 | 252.18 | 111.6 |
| 1915 | 1185941.21 | 105 | 218.1004 | 232.9 | 11571 | 523 | 1223.1 | 33.26 | 233.5 |
| 19168. | $345 \sim 2: 31.53$ | 107 | 134.6988 | 233.9 | 11937 | 889 | 134.2 | 399.26 | 113.1 |
| 1917 | 2101051.41 | 109 | 50.2973 | 234.9 | 315 | 1254 | 499.2 | 180.34 | 235.0 |
| 1918 | 1745821.09 | 110 | 190.5965 | 235.9 | 680 | 1619 | 864.2 | 515.34 | 113.6 |
| 1919 | 2994550.77 | $11:$ | 106.1950 | 236.9 | 1045 | 1981 | 12:29.2 | 326.42 | 235.5 |
| 1920 B . | $166 \quad 9 \quad 28.26$ | 114 | 22.7935 | 237.9 | 1411 | 2350 | 140.2 | 108.50 | 115.2 |
| 1921 | $30 \quad 5657.95$ | 115 | 163.0927 | 238.9 | 1776 | 2715 | 505.2 | 473.50 | 237.0 |
| 1922 | 2554427.63 | 117 | 78.6912 | 1.0 | 2141 | 121 | 870.2 | 251.58 | 115.7 |
| 1923 | 1:20 3157.31 | 118 | 218.9901 | 2.0 | 2506 | 486 | 1235.2 | 35.65 | 237.5 |
| $1924 B$. | 3165531.80 | 120 | 135.5889 | 3.0 | 2872 | 852 | 146.3 | 401.65 | 117.2 |
| 1925 | $\begin{array}{llll}211 & 43 & 4.49\end{array}$ | 122 | 51.1873 | 4.0 | 3237 | 1217 | 511.3 | 182.73 | 239.0 |
| 1926 | $7630 \quad 31.17$ | 123 | 191.4866 | 5.0 | 3602 | 1582 | 876.3 | 547.73 | 117.7 |
| 1927 | $30118 \quad 3.86$ | 125 | 107.0850 | 6.0 | 3967 | 1947 | 12.11 .3 | 328.81 | 239.5 |
| 1928 B. | 1674141.35 | 127 | 23.6835 | 7.0 | 4333 | 2313 | 15\%. 4 | 110.89 | 119.2 |
| 1929 | 322911.04 | 128 | 163.98:27 | 8.0 | 4698 | 2678 | 517.4 | 475.89 | 211.0 |
| 1930 | 2571640.72 | 130 | 79.5812 | 9.0 | 5063 | 84 | 882.4 | 256.97 | 119.7 |
| 1931 | 122410.41 | 131 | 219.8804 | 10.0 | 5428 | 449 | 1247.4 | 38.05 | 241.5 |
| $1932 B$. | 3182747.90 | 133 | 136.4789 | 11.0 | 5794 | 815 | 158.4 | 404.05 | 121.2 |
| 1983 | $\begin{array}{lllll}213 & 15 & 17.59\end{array}$ | 135 | 52.0774 | 12.0 | 6159 | 1180 | 523.4 | 185.13 | 213.0 |
| 1934 | $78 \quad 247.27$ | 136 | 192.3766 | 13.0 | 6524 | 1545 | 888.4 | 550.13 | 121.7 |
| 1935 | 3025016.96 | 138 | 107.9751 | 14.0 | 6889 | 1910 | 1253.4 | 331.20 | 0.4 |
| $1936 B$. | 1691351.46 | 140 | 24.5735 | 15.0 | 7255 | 2276 | 164.5 | 113.28 | 123.2 |
| 1937 | $\begin{array}{llll}31 & 1 & 21.15\end{array}$ | 141 | 164.8728 | 16.0 | 7620 | 2641 | 529.5 | 478.28 | 1.9 |
| 1938 | $258.48 \quad 53.83$ | 143 | 80.4712 | 17.0 | 7985 | 47 | 894.5 | 259.36 | 123.7 |
| 1939 | 1233623.52 | 144 | 220.7705 | 18.0 | 8350 | 412 | 1259.5 | 40.44 | 2.4 |
| 1940 B . | $\begin{array}{llll}350 & 0 & 1.02\end{array}$ | 146 | 137.3630 | 19.0 | 8716 | 778 | 170.5 | 406.44 | 125.2 |
| 1941 | 2144730.71 | 148 | 52.9674 | 20.0 | 9081 | 1143 | 535.5 | 187.52 | 3.9 |
| 1912 | 79350.40 | 149 | 193.2667 | 21.0 | 9446 | 1508 | 900.5 | 552.52 | 125.7 |
| 19.13 | 3012230.09 | 151 | 108.8651 | 22.0 | 9811 | 1873 | 1265.5 | 333.60 | 4.4 |
| $1944 B$. | $17046 \quad 7.59$ | 153 | 25.4636 | 23.0 | 10177 | 2239 | 176.6 | 115.68 | 127.2 |
| 1915 | 353337.28 | 154 | 165.7628 | 24.0 | 10542 | 2604 | 541.6 | 480.68 | 5.9 |
| 1916 | 260216.97 | 156 | 81.3613 | 25.0 | 10907 | 10 | 906.6 | 261.76 | 127.7 |
| 19.47 | $\begin{array}{llll}125 & 8 & 36.66\end{array}$ | 157 | 221.6606 | 26.0 | 11272 | 375 | 1271.6 | 42.83 | 6.4 |
| $19.18 B$. | 351 <br> 216 <br> 10 | 159 | 138.2590 | 27.0 | 11638 | 741 | 182.7 | 408.83 | 129.2 |
| 1949 | 2161943.85 | 161 | 53.8575 | 28.0 | 15 | 1106 | 547.7 | 189.91 | 7.9 |


| Mecen Lemgitule, Argments. de., for Washington Meren Noon of Jen, 0 in common yects, Jen. 1 in bissertile yeurs. |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| lear. | VIII. | IX. | ズ. | XI. | XII. | XIII. | XIV. | Log. sin i. | $360^{\circ}$ | - 8 |
| 1900 | 111.5 | 69.15 | 0.9 .07 | 218.80 | 37.2 | 37.7: | 26.1 | 8.772.882 | 281 | 13 \% 0.8 |
| 1901 | 65.3 | 197.16 | 5.58 | 31.09 | 16.5 | 43.91 | 27.6 | 28:37 |  | 12.28 .3 |
| 190: | 009.8 | 88.17 | 38.81 | 181.73 | 36.1 | 47.06 | 28.4 | 28.51 |  | 1155.8 |
| 1903 | 1333.6 | 216.18 | 15.36 | 2:37.0: | 15.4 | 53, 2.28 | 29.9 | 2861 |  | 1123.3 .3 |
| 190183. | 58.5 | 108.20 | 51.88 | 52.31 | 51.6 | 59.50 | 31.1 | 2878 |  | 10) 50.7 |
| 1905 | 202.9 | 2:36.21 | 25.13 | 199.9G | 11.3 | 2.69 | 33.2 | 8.77 20s91 | 281 | 1018.2 |
| 1906 | 1:26.8 | 127.2. | 31.65 | 15.25 | 533.5 | 8.81 | :33.7 | - 0.5 |  | 9) 45.7 |
| $190 \%$ | 50.7 | 18.21 | 4.91 | 162.89 | 13.1 | 11.9 .5 | :31.1 | 2918 |  | () 13:3 |
| $190 \sim B$. | 196.1 | 117.25 | 11.13 | 218.18 | 52.1 | 18.17 | 33.9 | 293: |  | 840.6 |
| 1909 | 1:0.0 | 38.26 | 17.95 | 33.47 | 31.6 | 21.40 | 1.5 | 29.15 |  | $8 \quad 8.1$ |
| 1910 | 43.5 | 166.27 | 51.20 | 181.12 | 51.3 | 27.51 | 2.2 | 8.77229 .9 | 281 | 735.6 |
| 1911 | 188.3 | 57.29 | 57.72 | 236.41 | 30.5 | 333.73 | 3.7 | 297: |  | $7 \quad 3.0$ |
| $1912 B$. | 113.1 | 186.29 | 4.21 | 51.70 | 9.8 | 39.96 | 5.2 | 2986 |  | (6)30.1 |
| 1913 | 37.0 | 77.31 | 37.50 | 199.31 | 29.1 | 43.07 | 5.9 | 2999 |  | 557.9 |
| 1911 | 181.4 | 205.32 | 41.01 | 14.63 | 8.6 | 49.29 | 7.1 | 3012 |  | 525.1 |
| 1915 | 10:. 3 | 96.33 | 17.27 | 16.2.87 | 28.3 | 59.40 | 8.2 | 8.77230e6 | 28.1 | 452.9 |
| $1916 B$. | 30.2 | 225.31 | 233.79 | 217.56 | 7.5 | 58.633 | 9.7 | 30339 |  | 420.3 |
| 1917 | 17.6 | 116.36 | 30.31 | 32.85 | 46.8 | 4.85 | 11.2 | 3053 |  | 347.8 |
| 1918 | 98.5 | 7.38 | 3.57 | 180.50 | 6.1 | 7.96 | 11.9 | 3066 |  | 315.3 |
| 1919 | 23.3 | 135.38 | 10.08 | 235.79 | 45.6 | 14.19 | 13.4 | 3080 |  | 242.8 |
| 19003. | 167.8 | 27.40 | 16.60 | 51.08 | 24.9 | 20.41 | 15.0 | 8.7723093 | 28.1 | 210.2 |
| 1921 | 91.6 | 155.41 | 49.86 | 198.72 | 41.5 | 23.53 | 15.7 | 3107 |  | 137.6 |
| 192: | 15.5 | 46.12 | 56.38 | 14.01 | 23.8 | 29.75 | 17.2 | 3120 |  | 15.1 |
| 1923 | 159.9 | 174.43 | 29.63 | 161.66 | 43.4 | 32.86 | 18.0 | $31: 31$ |  | 033.6 |
| 19:13. | 81.8 | 66.45 | 36.15 | 216.95 | 22.6 | 39.08 | 19.5 | 3147 | 281 | $0 \quad 0.0$ |
| 1925 | 8.7 | 191.46 | 42.67 | 32.24 | 1.9 | 45.30 | 21.0 | 8.7723160 | 283 | 5927.5 |
| 192\% | 153.1 | 85.47 | 15.93 | 179.88 | 21.5 | 48.42 | 21.7 | 3174 |  | 5855.0 |
| 1927 | 77.0 | 213.48 | 20.45 | 235.17 | 0.8 | 54.64 | 23.2 | 3187 |  | 5820.5 |
| $1928 B$. | 1.9 | 105.50 | 28.96 | 50.46 | 40.0 | 0.86 | 24.7 | $3: 01$ |  | 5749.9 |
| 1929 | 1:6.3 | 233.50 | 2.22 | 198.10 | 59.6 | 3.97 | 25.5 | 3214 |  | 5717.3 |
| 1930 | 70.2 | 121.52 | 8.74 | 13.39 | 38.9 | 10.20 | 27.0 | 8.7728228 | 283 |  |
| 1931 | 214.6 | 15.51 | 42.00 | 161.01 | 58.5 | 13.31 | 27.7 | 3211 |  | 5612.3 |
| $193: 2$. | 139.5 | 141.55 | 48.51 | 216.33 | 37.8 | 19.53 | 29.2 | 3825 |  | 5539.7 |
| 1933 | 63.3 | 35.56 | 55.03 | 31.62 | 17.0 | 25.76 | 30.7 | 3268 |  | $55 \quad 7.2$ |
| 1931 | 207.8 | 163.57 | 28.29 | 179.26 | 36.6 | 28.87 | 31.5 | 3282 |  | 5134.7 |
| 193.) | 131.6 | 51.59 | 31.81 | 231.55 | 15.9 | 35.09 | 33.0 | 8.7723:95 | 283 | 51.2 .1 |
| $1936 B$. | 56.5 | 183.59 | 41.32 | 49.81 | 55.1 | 41.32 | 31.5 | 83309 |  | 5329.5 |
| 1937 | 200.9 | 74.61 | 14.58 | 197.19 | 14.8 | 41.43 | 35.3 | 3322 |  | 5257.0 |
| 1938 | 121.8 | 202.62 | 21.10 | 12.78 | 51.0 | 50.65 | 0.8 | 3333 |  | 5224.5 |
| 1939 | 48.7 | 93.63 | 54.36 | 160.42 | 13.6 | 53.76 | 1.5 | 3349 |  | 5152.0 |
| 1910 B . | 191.1 | 22.64 | 0.88 | 215.71 | 52.9 | 59.99 | 3.0 | 8.7723362 |  |  |
| 1911 | 118.0 | 113.66 | 7.39 | 31.00 | 32.1 | 6.21 | 4.5 | 3376 |  | 5046.9 |
| 1912 | 41.8 | 4.67 | 40.65 | 178.64 | 51.8 | 9.32 | 5.3 | 3389 |  | 50.11 .3 |
| 1913 | 186.3 | 13:.68 | 47.17 | 233.9:3 | 31.0 | 15.55 | 6.8 | 3103 |  | 4941.8 |
| $1944 B$. | 111.1 | 24.70 | 53.69 | 49.22 | 10.3 | 21.77 | 8.3 | 3116 |  | 49 9.2 |
| 1945 | 35.0 | 15.2 .71 | 26.95 | 196.57 | 29.9 | 21.88 | 9.0 | 8.7723430 | 283 | 4836.7 |
| 1916 | 179.4 | 43.72 | 33.46 | 12.16 | 9.1 | 31.10 | 10.5 | 3.413 |  | 484.2 |
| 1917 | 103.3 | 171.73 | 6.72 | 159.80 | 28.8 | 31.20 | 11.3 | 3157 |  | 4731.6 |
| $1918 D$. | 28.2 | 63.75 | 13.21 | 215.09 | 8.0 | 40.44 | 12.8 | 3170 |  | 4659.0 |
| 1919 | 172.6 | 191.76 | 19.76 | 30.38 | 47.3 | 46.66 | 14.3 | 8.7723184 | 283 | 4626.5 |

Motion of mean Longitude and of $-\Omega$; and Fraction of Year.

| $\begin{gathered} \text { Common } \\ \text { Year. } \end{gathered}$ | Bissextile Year. | Mution of Alean Longitude. | Motion of $360^{\circ}-8$ | Fract. of Year | Year. | Motion of Mean Longitude. | Motion of $360^{\circ}-8$ | Fract. of Year. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Jan. 0 | Jan. $\begin{array}{ll} \\ & 1 \\ & 2 \\ & 3 \\ & 1\end{array}$ | - 111 | $-0.0$ | 0.000 | Mar. | $96 \quad 7 \quad 43.44$ | $-5.3$ | 0.164 |
|  |  | $\begin{array}{llll}0 & 0 & 0.00\end{array}$ |  |  |  |  |  |  |
|  |  | $136 \quad 7.81$ | 0.1 | 0.003 |  | 1774356.25 | -5.3 | 0.167 |
|  |  | 31915.61 | 0.2 | $0.00 \%$ |  | 99204.05 | 5.5 | $0.1 \% 0$ |
|  |  | 44823.42 | $0.3$ | $0.00{ }^{\circ}$ |  | 1005611.86 | 5.6 | 0.173 |
| 4 | 5 | 62431.23 | $-0.4$ | 0.011 | 5 | 1023219.67 | $-5.7$ | 0.175 |
| 5 | 6 | $8 \quad 0 \quad 39.04$ | 0.4 | 0.014 | 6 | 1048397.48 | 5.8 | 0.178 |
| 6 | 7 | 93646.84 | 0.5 | 0.016 | 7 | 1054435.23 | 5.9 | 0.181 |
| 7 | 8 | 111254.6 J | 0.6-0.7 | $0.01!$ | 8 | 1072043.09 | 6.0 | 0.183 |
| 8 | 9 | 12492.46 |  | 0.022 | 9 | 1035650.90 | $-6.1$ | 0.186 |
| 9 | 10 | 14.2510 .97 | 0.8 | 0.02 .5 | 10 | 1103258.70 | 6.1 | 0.189 |
| 10 | 11 | $\begin{array}{llllllllll}16 & 1 & 18.07\end{array}$ | 0.8 | 0.047 | 11 | $11: 36.51$ | 6.2 | 0.199 |
| 11 | 12 | 173795.88 | 1.0 | 0.030 | 12 | 11345 14.3? | 6.3 | 0.194 |
| 12 | 13 | 191333.69 | - 1.1 | 0.033 | 13 | 1152129.13 | $-6.4$ | 0.197 |
| 13 | 14 | 204941.50 | 1.2 | 0.036 | 14 | 1165729.93 | 6.5 | 0.200 |
| 14 | 15 | 22.2549 .30 | 1.2 | 0.038 | 15 | 1183337.74 | 6.6 | $0.203$ |
| 15 | 16 | 241857.11 | 1.3 | 0.041 | 16 | $120 \quad 945.55$ | $6.7$ |  |
| 16 | 17 | 25.334 .92 | $-1.4$ | 0.044 | 17 | 1214553.36 | -6.8-6.96.97.0 | $\begin{aligned} & 0.206 \\ & 0.211 \\ & 0.214 \\ & 0.216 \end{aligned}$ |
| 17 | 18 | 271412.72 | 1.5 | 0.047 | 18 | 123221.16 |  |  |
| 18 | 19 | 285020.53 | 1.6 | 0.049 | 19 | 124588.97 |  |  |
| 19 | 20 | 302698.34 | 1.7 | 0.052 | 20 | 1263416.78 |  |  |
| 20 | 21 | $39 \quad 236.15$ | -1.81.92.02.0 | 0.055 | 91 | 1281024.59 | $-7.1$ | $\begin{aligned} & 0.219 \\ & 0.222 \end{aligned}$ |
| 21 | 212 | 3338438.95 |  | 0.057 | 29 | 1294632.39 | 7.27.3 |  |
| 29 | 23 | 351451.76 |  | 0.0600.063 |  | 1312240.20 |  | $\begin{aligned} & 0.222 \\ & 0.225 \end{aligned}$ |
| 23 | 24 | 365059.57 |  |  | 24 | 1325848.01 | $7.4$ | $0.2: 7$ |
| 24 | 25 | $3827 \quad 7.38$ | $-2.1$ | 0.066 | 25 | 1343455.81 | $-7.5$ | 0.2300.233 |
| 25 | 26 | $40 \begin{array}{llll}40 & 15.18\end{array}$ | 2.2 | 0.068 | 26 | $13611 \quad 3.62$ | 7.67.7 |  |
| 26 | 27 | 413922.99 | 2.3 | 0.071 | 27 | 1374711.43 |  | 0.233 0.236 |
| 27 | 23 | 431530.80 | 9.4 | 0.074 | 28 | 1392319.24 | 7.7 | 0.238 |
| 28 | 29 | 445138.60 | $-2.5$ | 0.077 | 29 | 1405927.04 | - 78 | 0.241 |
| 98 30 | 30 | 469746.41 | 2.6 | 0.079 | 30 | 1423534.85 | 7.9 | 0.244 |
| 30 31 | Feb. ${ }^{31}$ | $48 \quad 354.24$ | 2.7 | 0.082 | 31 | 1441149.66 | 8.0 | 0.246 |
| 31 | Feb. 1 | $4940 \quad 2.03$ | 2.8 | 0.085 | Apr. 1 | 1454750.47 | 8.1 | 0.249 |
| Feb. $\begin{array}{r}1 \\ 2 \\ 3 \\ 4 \\ \\ \\ 5 \\ 6 \\ 7 \\ 8\end{array}$ | 2345 | $\begin{array}{lll} 51 & 16 & 9.83 \\ 52 & 52 & 17.64 \\ 54 & 23 & 25.45 \\ 56 & 4 & 33.26 \end{array}$ | $\begin{array}{r} -2.8 \\ 2.9 \\ 3.0 \\ 3.1 \end{array}$ | $\begin{aligned} & 0.088 \\ & 0.090 \\ & 0.093 \\ & 0.096 \end{aligned}$ | $\begin{aligned} & 2 \\ & 3 \\ & 4 \\ & 5 \end{aligned}$ | $\begin{array}{lrr} 147 & 2.3 & 58.27 \\ 149 & 0 & 6.08 \\ 150 & 36 & 13.89 \\ 152 & 12 & 21.69 \end{array}$ | -8.9 | $\begin{aligned} & 0.2 .2 \\ & 0.2 .5 \\ & 0.2 .77 \\ & 0.260 \end{aligned}$ |
|  |  |  |  |  |  |  | 8.3 |  |
|  |  |  |  |  |  |  | 8.4 |  |
|  |  |  |  |  |  |  | 8.5 |  |
|  | 6789 | $\begin{array}{llll}57 & 40 & 41.06 \\ 59 & 16 & 48.87 \\ 60 & 52 & 56.68 \\ 69 & 29 & 4.49\end{array}$ | $\begin{array}{r} -3.2 \\ 3.3 \\ 3.4 \\ 3.5 \end{array}$ | $\begin{aligned} & 0.099 \\ & 0.101 \\ & 0.104 \\ & 0.107 \end{aligned}$ | $\begin{aligned} & 6 \\ & 7 \\ & 8 \\ & 9 \end{aligned}$ | $\begin{array}{rrr} 153 & 48 & 29.50 \\ 155 & 24 & 37.31 \\ 157 & 0 & 45.12 \\ 158 & 36 & 52.92 \end{array}$ | $\begin{array}{r} -8.5 \\ 8.6 \\ 8.7 \\ 8.8 \end{array}$ | $\begin{aligned} & 0.263 \\ & 0.266 \\ & 0.268 \\ & 0277 \end{aligned}$ |
|  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
| 9 | $\begin{aligned} & 10 \\ & 11 \\ & 12 \\ & 13 \end{aligned}$ | $\begin{array}{ccc} 64 & 5 & 19.29 \\ 65 & 41 & 20.10 \\ 67 & 17 & 27.91 \\ 68 & 53 & 35.71 \end{array}$ | $\begin{array}{r} -3.6 \\ 3.6 \\ 3.7 \\ 3.8 \end{array}$ | $\begin{aligned} & 0.110 \\ & 0.112 \\ & 0.115 \\ & 0.118 \end{aligned}$ | $\begin{aligned} & 10 \\ & 11 \\ & 12 \\ & 13 \end{aligned}$ | $\begin{array}{rrr}160 & 13 & 0.73 \\ 161 & 49 & 8.54 \\ 163 & 2.5 & 16.35 \\ 16.5 & 1 & 24.15\end{array}$ | $-8.9$ | $\begin{aligned} & 0.274 \\ & 0.277 \\ & 0.278 \\ & 0.282 \end{aligned}$ |
| 10 |  |  |  |  |  |  | 9.0 |  |
| 11 |  |  |  |  |  |  | 9.1 |  |
| 12 |  |  |  |  |  |  | 9.2 |  |
| 13 | $\begin{aligned} & 14 \\ & 15 \\ & 16 \\ & 17 \end{aligned}$ | $\begin{array}{llll}70 & 29 & 43.52 \\ 72 & 5 & 51.33 \\ 73 & 41 & 59.14 \\ 75 & 18 & 6.94\end{array}$ | $\begin{array}{r} -3.9 \\ 4.0 \\ 4.1 \\ 4.9 \end{array}$ | $\begin{aligned} & 0.120 \\ & 0.123 \\ & 0.126 \\ & 0.129 \end{aligned}$ | 14151617 | 1663731.96 <br> 1681339.77 <br> 169 <br> 49 <br> 171 <br> 15 | $-93$ | $\begin{aligned} & 0.28 .5 \\ & 0.283 \\ & 0.990 \\ & 0.293 \end{aligned}$ |
| 14 |  |  |  |  |  |  | - 9.3 |  |
| 15 |  |  |  |  |  |  | 9.4 |  |
| 16 |  |  |  |  |  |  | 9.5 |  |
| 17 | 18 | 765414.75 | $-4.3$ | 0.131 | 18 | $\begin{array}{llll}173 & 2 & 3.19\end{array}$ | $-9.6$ | 0.296 |
| 18 | 19 | 753023.56 | 4.4 | 0.134 | 19 | 174.3811 .00 | 9.7 | 0.2938 |
| 19 | 2021 | $\begin{array}{rrrr}80 & 6 & 30.37 \\ 81 & 42 & 38.17\end{array}$ | 4.54.5 | $\begin{aligned} & 0.137 \\ & 0.140 \end{aligned}$ | 20 | $\begin{array}{lll}176 & 14 & 18.80 \\ 177 & 50 & 26.61\end{array}$ | 0.9 |  |
| $\mathfrak{2 0}$ |  |  |  |  | 21 |  |  | $0.304$ |
| 21 | 22 | 831845.98 | -4.64.74.84.9 | $\begin{aligned} & 0.142 \\ & 0.145 \\ & 0.148 \\ & 0.151 \end{aligned}$ | $\begin{aligned} & 22 \\ & 23 \\ & 94 \\ & 25 \end{aligned}$ | $\begin{array}{lrr}179 & 26 & 34.42 \\ 181 & 2 & 42.23 \\ 180 & 33 & 50.03 \\ 184 & 14 & 57.84\end{array}$ | $\begin{array}{r} -10.0 \\ 10.1 \\ 10.1 \\ 10.2 \end{array}$ | $\begin{aligned} & 0.307 \\ & 0.309 \\ & 0.312 \\ & 0.315 \end{aligned}$ |
| 22 | 23 | 845453.79 |  |  |  |  |  |  |
| 93 | 24 | 8631.60 |  |  |  |  |  |  |
| 24 | 25 | $83 \% 9.40$ |  |  |  |  |  |  |
| 25 | 26 | 894317.21 | $\begin{array}{r} -5.0 \\ 5.1 \\ 5.2 \\ -5.3 \end{array}$ | $\begin{aligned} & 0.153 \\ & 0.150 \\ & 0.159 \\ & 0.161 \end{aligned}$ |  | 185515.65 | -10.3 | 0.318 |
| 96 | 97 | 011985.02 |  |  | $27$ | 1879713.46 | 10.4 | 0.329 |
| 27 | 28 | 925.532 .82 |  |  | $25$ | 189) 321.26 | 10.5 | 0.323 |
| 28 | \% | 943140.63 |  |  | 29 | 1903929.0 i | -10.6 | 0.326 |

Motion of Mean Longitude and of $-\Omega$; and Fraction of Year.


Motion of Mean Longitude and of $-\delta$; and Fraction of Year.

| lear. | Motion of <br> Mean Longitude. | Motion of $363^{\circ}-8$ | Fruction of lear. | Year. | Motion of <br> Mean Longitude | Motion of $360^{\circ}-\Omega$ | $\begin{aligned} & \text { Praction of } \\ & \quad \text { Year. } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{array}{r} \text { Aug. } 23 \\ 29 \\ 30 \\ 31 \end{array}$ |  | $\begin{array}{r} -21.1 \\ 21.5 \\ 21.5 \\ 21.6 \end{array}$ | $\begin{aligned} & 0.657 \\ & 0.669 \\ & 0.669 \\ & 0.663 \\ & 0.665 \end{aligned}$ | Nov. $\begin{array}{r}4 \\ 5 \\ 6 \\ 7 \\ 7\end{array}$ | $\begin{array}{ll} 133^{\prime} & : 8 \\ 13 & 4.67 \\ 135 & 4 \\ 130.46 \\ 136 & 40 \\ 138 & 20.27 \\ 165.07 \end{array}$ | $\begin{array}{r} -27.4 \\ -27.4 \\ 27.6 \\ 27.7 \end{array}$ | $\begin{aligned} & 0.843 \\ & 0.8 .16 \\ & 0.849 \\ & 0.852 \end{aligned}$ |
| Sept. $\begin{aligned} & 2 \\ & 3 \\ & 4 \end{aligned}$ | $\begin{array}{cccc}30 & 5.5 & 44.08 \\ 32 & 31 \\ 34 & 81 & 5.79 \\ 3 & 0.60 \\ 35 & 44 & 8.41\end{array}$ | $\begin{array}{r} -21.7 \\ 21.8 \\ 21.9 \\ 2.9 \\ 22.0 \end{array}$ | $\begin{aligned} & 0.668 \\ & 0.671 \\ & 0.674 \\ & 0.676 \end{aligned}$ | $\begin{array}{r} 8 \\ 9 \\ 10 \\ 11 \end{array}$ | 1395235.88 <br> $1412 \checkmark 43.69$ <br> 143451.50 <br> 1444059.30 | $\begin{array}{r} -97.8 \\ 27.9 \\ 28.0 \\ 28.0 \end{array}$ | $\begin{aligned} & 0.854 \\ & 0.857 \\ & 0.860 \\ & 0.86 \% \end{aligned}$ |
| $\begin{aligned} & 5 \\ & 6 \\ & 7 \\ & 8 \end{aligned}$ | $\begin{aligned} & 37 \quad 9016.21 \\ & 3856.4 .02 \\ & 403231.83 \\ & 4.28 \\ & 4.29 .64 \end{aligned}$ | $\begin{array}{r} -22.1 \\ -22.2 \\ 2.23 \\ 2.2 .3 \\ 2.3 \end{array}$ | $\begin{aligned} & 0.679 \\ & 0.6 \times 2 \\ & 0.685 \\ & 0.687 \end{aligned}$ | 112 13 14 15 | $14617 \quad 7.11$ 1475314.92 149 2.9 2e.7.3 <br> $151 \quad 5 \quad 30.5$ : | $\begin{array}{r} -28.1 \\ 28.2 \\ 28.3 \\ 28.4 \end{array}$ | $\begin{aligned} & 0.865 \\ & 0.868 \\ & 0.871 \\ & 0.873 \end{aligned}$ |
| $\begin{array}{r} 9 \\ 10 \\ 11 \\ 12 \end{array}$ | $\begin{array}{lll} 43 & 44 & 47.44 \\ 45 & 20 & 5.42 \\ 46 & 57 & 3.26 \\ 48 & 33 & 10.87 \end{array}$ | $\begin{array}{r} -9.4 \\ 20.5 \\ 29.6 \\ 22.7 \end{array}$ | $\begin{aligned} & 0.690 \\ & 0.693 \\ & 0.695 \\ & 0.6!98 \end{aligned}$ | 16 17 18 19 | $\begin{array}{llll} 152 & 41 & 3 \times .34 \\ 154 & 17 & 46.15 \\ 155 & 53 & 53.96 \\ 157 & 30 & 1.76 \end{array}$ | $\begin{array}{r} -28.5 \\ 28.6 \\ 28.7 \\ 23.8 \end{array}$ | $\begin{aligned} & 0.876 \\ & 0.879 \\ & 0.879 \\ & 0.854 \end{aligned}$ |
| $\begin{aligned} & 13 \\ & 14 \\ & 15 \\ & 16 \end{aligned}$ | $\begin{array}{lll}50 & 9 & 18.67 \\ 51 & 45 & 26.48 \\ 53 & 21 & 34.5 \% \\ 54 & 57 & 42.09\end{array}$ | $\begin{array}{r} -22.8 \\ 23.9 \\ 23.0 \\ 23.0 \end{array}$ | $\begin{aligned} & 0.701 \\ & 0.704 \\ & 0.7106 \\ & 0.709 \end{aligned}$ | 20 21 21 22 23 | $159 \quad 6 \quad 9.57$ <br> 1604217.38 <br> 1621825.18 <br> 1635432.99 | $\begin{array}{r} 23.8 \\ 28.9 \\ 29.0 \\ 29.0 \\ 20.1 \end{array}$ | $\begin{aligned} & 0.887 \\ & 0.890 \\ & 0.893 \\ & 0.895 \end{aligned}$ |
| $\begin{aligned} & 17 \\ & 18 \\ & 19 \\ & 20 \end{aligned}$ | 563349.90 $58 \quad 9 \quad 57.71$ $5946 \quad 5.52$ 612213.32 | $\begin{array}{r} -23.1 \\ 23.1 \\ 2: 1.1 \\ 23.4 \end{array}$ | $\begin{aligned} & 0.712 \\ & 0.715 \\ & 0.717 \\ & 0.720 \end{aligned}$ | 24 24 20 26 27 | $\begin{array}{lll} 165 & 30 & 40.80 \\ 167 & 6 & 48.61 \\ 168 & 42 & 56.41 \\ 170 & 19 & 4.22 \end{array}$ | $\begin{array}{r} -29.2 \\ 29.3 \\ 29.4 \\ 29.5 \end{array}$ | $\begin{aligned} & 0.898 \\ & 0.901 \\ & 0.904 \\ & 0.906 \end{aligned}$ |
| $\begin{aligned} & 21 \\ & 20 \\ & 23 \\ & 23 \\ & 24 \end{aligned}$ | $6258 \quad 21.13$ 643428.94 661036.75 674644.55 | -23.5 -23.6 23.7 23.8 | $\begin{aligned} & 0.723 \\ & 0.726 \\ & 0.728 \\ & 0.731 \end{aligned}$ |  | 171551203 <br> 1733119.84 <br> $175 \quad 767.64$ <br> 1764335.45 | $\begin{array}{r} -29.6 \\ -29.6 \\ 29.7 \\ 29.8 \end{array}$ | $\begin{aligned} & 0.999 \\ & 0.912 \\ & 0.914 \\ & 0.917 \end{aligned}$ |
| $\begin{aligned} & 25 \\ & 26 \\ & 27 \\ & 27 \end{aligned}$ | 69 22 52.36 <br> 70   <br> 70 59 0.17 <br> 72 35 $7 . .98$ <br> 74 11 15.78 | $\begin{array}{r} -23.9 \\ 23.9 \\ 24.0 \\ 24.1 \end{array}$ | $\begin{aligned} & 0.734 \\ & 0.737 \\ & 0.739 \\ & 0.742 \end{aligned}$ | 1 3 4 4 5 | 1781943.26 1795551.07 <br> 1 181 3158.87 <br> $183 \quad 8 \quad 6.68$ | $\begin{array}{r} -29.9 \\ 30.0 \\ 30.1 \\ 30.2 \end{array}$ | $\begin{aligned} & 0.920 \\ & 0.923 \\ & 0.925 \\ & 0.925 \end{aligned}$ |
|  | $\begin{aligned} & 7547 \quad 43.59 \\ & 772331.40 \\ & 785939.20 \\ & 80 \quad 3547.01 \end{aligned}$ | $\begin{array}{r} -94.2 \\ 24.3 \\ 24.4 \\ 24.5 \\ 24.5 \end{array}$ | $\begin{aligned} & 0.745 \\ & 0.747 \\ & 0.750 \\ & 0.753 \end{aligned}$ | 6 7 8 8 9 | 1844414.49 <br> 1862029.29 <br> 1875630.10 <br> $18!3237.91$ | $\begin{array}{r} -30.3 \\ 30.4 \\ 30.4 \\ 30.5 \end{array}$ | $\begin{aligned} & 0.931 \\ & 0.934 \\ & 0.936 \\ & 0.939 \end{aligned}$ |
| $\begin{aligned} & 3 \\ & 4 \\ & 5 \\ & 6 \end{aligned}$ | 821154.82 <br> 83482.63 <br> 8.52410 .43 <br> 87 018.24 | $\begin{array}{r} -94.6 \\ 24.7 \\ 24.7 \\ 24.8 \end{array}$ | $\begin{aligned} & 0.756 \\ & 0.758 \\ & 0.761 \\ & 0.764 \end{aligned}$ | 10 11 12 13 | $\begin{array}{lr} 191 & 845.72 \\ 192 & 44 \\ 193.52 \\ 194 & 21 \\ 195 & 1.33 \\ 1.14 \end{array}$ | $\begin{array}{r} -30.6 \\ 30.7 \\ 30.8 \\ 30.9 \end{array}$ | $\begin{aligned} & 0.942 \\ & 0.945 \\ & 0.947 \\ & 0.950 \end{aligned}$ |
| $\begin{array}{r} 7 \\ 8 \\ 9 \\ 10 \end{array}$ | 883626.05 901233.86 914841.66 1132449.47 | $\begin{array}{r} -24.9 \\ -25.0 \\ 25.1 \\ 25.1 \\ 25.2 \end{array}$ | $\begin{aligned} & 0.767 \\ & 0.769 \\ & 0.772 \\ & 0.775 \end{aligned}$ | 14 15 16 17 | $\begin{array}{lll} 197 & 3 & 16.95 \\ 190 & 9 & 2.475 \\ 000 & 4.5 & 32.56 \\ 202 & 21 & 40.33 \end{array}$ | $\begin{array}{r} -31.0 \\ 31.1 \\ 31.2 \\ 31.2 \end{array}$ | $\begin{aligned} & 0.953 \\ & 0.956 \\ & 0.958 \\ & 0.961 \end{aligned}$ |
| $\begin{aligned} & 11 \\ & 12 \\ & 13 \\ & 14 \end{aligned}$ | $95 \quad 0 \quad 57 .!8$ $\begin{array}{lll}96 & 37 & 5.08\end{array}$ $98 \quad 1312.89$ 954920.70 | $\begin{array}{r} -25.3 \\ -25.4 \\ 25.5 \\ 25.6 \end{array}$ | $\begin{aligned} & 0.778 \\ & 0.780 \\ & 0.783 \\ & 0.786 \end{aligned}$ | 18 18 19 20 21 | 2035748.17 <br> 2053355.98 <br> $207 \quad 10 \quad 3.79$ <br> 2084611.60 | $\begin{array}{r} -31.3 \\ 31.4 \\ 31.5 \\ 31.6 \end{array}$ | $\begin{aligned} & 0.964 \\ & 0.967 \\ & 0.969 \\ & 0.972 \end{aligned}$ |
| $\begin{aligned} & 15 \\ & 16 \\ & 17 \\ & 18 \end{aligned}$ | 1012528.51 <br> $103 \quad 136: 31$ <br> 1043744.12 <br> 1061351.93 | $\begin{array}{r} -95.6 \\ -2.7 \\ 25.8 \\ 25.8 \\ 25.9 \end{array}$ | $\begin{aligned} & 0.789 \\ & 0.791 \\ & 0.794 \\ & 0.797 \end{aligned}$ | 29 23 23 24 25 | 2102219.40 2115897.21 2133435.04 2151042.83 | $\begin{array}{r} -31.7 \\ 31.7 \\ 31.5 \\ 32.0 \end{array}$ | $\begin{aligned} & 0.975 \\ & 0.977 \\ & 0.980 \\ & 0.183 \end{aligned}$ |
| $\begin{aligned} & 19 \\ & 20 \\ & 21 \\ & 22 \end{aligned}$ | 1074959.74 <br> $10926 \quad 7.54$ <br> 111215.35 1123823.16 | $\begin{array}{r} -26.0 \\ 26.1 \\ 26.2 \\ 26.3 \\ \hline \end{array}$ | $\begin{aligned} & 0.800 \\ & 0.802 \\ & 0805 \\ & 0.808 \end{aligned}$ | 26 28 28 28 20 | 2164650.63 <br> 218 ! 58.44 <br> $\begin{array}{lll}219 & 59 & 6.25 \\ 221 & 35 & 14.06\end{array}$ | $\begin{array}{r} -32.0 \\ -32.1 \\ 32.2 \\ 32.3 \end{array}$ | $\begin{aligned} & 0.986 \\ & 0.1188 \\ & 0.991 \\ & 0.994 \end{aligned}$ |
| $\begin{aligned} & 23 \\ & 24 \\ & 24 \\ & 20 \\ & 26 \end{aligned}$ | 1141430.97 1155038.77 1172646.58 119254.39 | $\begin{array}{r} -26.4 \\ -26.4 \\ 26.5 \\ 26.6 \end{array}$ | $\begin{aligned} & 0.810 \\ & 0.813 \\ & 0.816 \\ & 0.819 \end{aligned}$ | 30 31 32 33 | 2231121.86 2244720.67 2262337.48 2275945.28 | $\begin{array}{r} -32.4 \\ 32.5 \\ 32.6 \\ 32.7 \end{array}$ | $\begin{aligned} & 0.997 \\ & 0.999 \\ & 1.009 \\ & 1.005 \end{aligned}$ |
| $\begin{aligned} & 127 \\ & 28 \\ & 239 \\ & 30 \end{aligned}$ | $\begin{array}{lll} 120 & 39 & 2.19 \\ 1929 & 15 & 10.00 \\ 123 & 51 & 178 \\ 145 & 27 & 25.62 \end{array}$ | $\begin{array}{r} -26.7 \\ -26.8 \\ 26.9 \\ 27.0 \end{array}$ | $\begin{aligned} & 0.821 \\ & 0.824 \\ & 0.827 \\ & 0.830 \\ & 0.830 \end{aligned}$ | $\begin{aligned} & 34 \\ & 39 \\ & 36 \\ & 34 \end{aligned}$ |  | $\begin{array}{r} -32.8 \\ 32.8 \\ 32.9 \\ -33.0 \end{array}$ | $\begin{aligned} & 1.008 \\ & 1.010 \\ & 1.013 \\ & 1.016 \end{aligned}$ |
| Nov. | $\begin{array}{ll} 127 & 3 \\ 123.42 \\ 12 y & 39 \\ 1: 10 & 41.23 \\ 130 & 49.04 \\ 131 & 51 \\ \hline \end{array}$ | $\begin{array}{r} -27.1 \\ 27.1 \\ 27.2 \\ -27.3 \end{array}$ | $\begin{aligned} & 0.832 \\ & 0.83 .3 \\ & 0.8: 38 \\ & 0.841 \\ & \hline \end{aligned}$ |  |  |  |  |


| Motion of Mean Longitude. |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hours. | For Hours. |  | Minutes or Seconds. | For Minutes. | For Seconds. | Minutes or Seconds. | For Minutes. | For Seconds. |
| 1 | $\begin{array}{llll}0 & 4 & 4 \\ 0\end{array}$ |  | 1 | $\begin{array}{ll}0 & \prime \prime \\ 0 & 4.005\end{array}$ | ${ }^{\prime \prime} 0.067$ | 31 | ${ }_{2}{ }^{\prime} \quad 4.168$ | 2.069 |
| 2 |  |  | 2 | $0 \quad 8.011$ | 0.134 | 32 | $\begin{array}{lll}2 & 8.173\end{array}$ | 2.136 |
| 3 | $\begin{array}{rrrr}0 & 8 & 0.651 \\ 0 & 12 & 0.976\end{array}$ |  | 3 | 012.016 | 0.200 | 33 | 212.179 | 2.203 |
| 4 | 0161.301 |  | 4 | $0 \quad 16.022$ | 0.267 | 34 | 216.184 | 2.270 |
| 5 |  |  | 5 | 020.027 | 0.334 | 35 | 220.190 | 2.336 |
| 6 | $\begin{array}{llll}0 & 20 & 1.627 \\ 0 & 24 & 1.952 \\ 0 & 2 & 2.27\end{array}$ |  | 6 | 024.033 | 0.401 | 36 | 224.195 | 2.403 |
| 7 | $\begin{array}{llll}0 & 24 & 1.952 \\ 0 & 28 & 2.277\end{array}$ |  | 7 | 028.038 | 0.467 | 37 | 228.201 | 2.470 |
| 8 | $\begin{array}{llll}0 & 28 \\ 0 & 32.277 \\ 0 & 2.602\end{array}$ |  | 8 | 032.043 | 0.534 | 38 | 232.206 | 2.537 |
| 9 | 00 322.602 |  | 9 | 036.049 | 0.601 | 39 | 236.211 | 2.604 |
| 10 | 00 03.253 |  | 10 | 040.054 | 0.668 | 40 | 240.217 | 2.670 |
| 11 | $0 \begin{aligned} & 0 \\ & 0\end{aligned} 43.578$ |  | 11 | 044.060 | 0.734 | 41 | 244.222 | 2.737 |
| 12 | $\begin{array}{llll}0 & 44 & 3.578 \\ 0 & 48 & 3.904 \\ 0 & 5 & 4 .\end{array}$ |  | 12 | 048.065 | 0.801 | 42 | 248.228 | 2.804 |
| 13 | 0524.229 |  | 13 | 052.070 | 0.868 | 43 | 252.233 | 2.871 |
| 14 | 0564.554 |  | 14 | 056.076 | 0.935 | 44 | 256.239 | 2.937 |
| 15 | 104.880 |  | 15 | 10.081 | 1.001 | 45 | 30.244 | 3.004 |
| 16 | 145.205 |  | 16 | 14.087 | 1.068 | 46 | 34.249 | 3.071 |
| 17 | 185.530 |  | 17 | 18.092 | 1.135 | 47 | $\begin{array}{ll}3 & 8.255\end{array}$ | 3.138 |
| 18 | 1 <br> 1 <br> 1 <br> 125 |  | 18 | 112.098 | 1.202 | 48 | 312.260 | 3.204 |
| 19 | $\begin{array}{ll}1 & 166.181\end{array}$ |  | 19 | 116.103 | 1.268 | 49 | 316.266 | 3.271 |
| 20 | 1206.506 |  | 20 | 120.108 | 1.335 | 50 | 320.271 | 3.338 |
| 21 | 1246.831 |  | 21 | 124.114 | 1.402 | 51 | 324.277 | 3.405 |
| 22 | 1287.157 |  | 22 | 128.119 | 1.469 | 52 | 328.282 | 3.471 |
| 23 | 1327.482 |  | 23 | 132.125 | 1.535 | 53 | 332.287 | 3.533 |
| 24 | 1367.807 |  | 24 | 136.130 | 1.602 | 54 | 336.293 | 3.605 |
|  |  |  | 25 | 140.136 | 1.669 | 55 | 340.298 | 3.672 |
|  |  |  | 26 | 144.141 | 1.736 | 56 | 344.304 | 3.738 |
|  |  |  | 27 | 148.146 | 1.802 | 57 | 348.309 | 3.805 |
|  |  |  | 28 | 152.152 | 1.869 | 58 | 352.314 | 3.872 |
|  |  |  | 29 | 156.157 | 1.936 | 59 | 356.320 | 3.939 |
|  |  |  | 30 | 20.163 | 2.003 | 60 | $4 \quad 0.325$ | 4.005 |
| Days. | Motion of M. L. |  |  | Days. | Motion of M. $\mathbf{I}$. |  | Days. | Motion of M. L. |
|  |  |  |  |  |  |  |  |  |
| 0.1 | [ $\begin{array}{llll}0 & 9 & 9 & 36.781\end{array}$ |  |  | 0.01 | 0 57.678 |  | 0.001 | 5.768 |
| 0.2 | [ $\begin{aligned} & 01913.561 \\ & 0 \\ & 0\end{aligned}$ |  |  | 0.02 | 155.356 |  | 0.002 | 11.536 |
| 0.3 0.4 | 02850.342 |  |  | 0.04 | 253.034 | 350.712 | 0.003 | 17.303 |
| 0.5 | 0483.904 | 03827.123 |  | 0.05 | 448.390 |  | 0.005 | 28.839 |
| 0.6 | $\begin{array}{rrrr}0 & 57 & 40.684 \\ 1 & 7 & 17.465\end{array}$ |  |  | 0.060.07 | 546.068 |  | 0.006 | 34.607 |
| 0.7 |  |  |  | $\begin{array}{ll}6 & 43.746 \\ 7 & 41.425\end{array}$ |  | 0.007 | 40.375 |  |
| 0.8 | 11654.246 |  |  |  |  | 0.08 | 0.008 | 46.142 |
| 0.9 | 12631.027 |  |  | 0.090.10 | 839.103 |  | 0.009 | 51.910 |
| 1.0 |  |  | $6 \quad 7.807$ |  | 936.781 |  | 0.010 | 57.678 |

## TABLC IX.

Factor of a small Correction to be multiplied by the fraction of the year and then added to $L$.

| Year. | Factor. | Year. | Factor. | Year. | Factor. | Year. | Factor. |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  |  |  |  |  |  |  |
| 1750 | -0.018 | 1800 | -0.011 | 1850 | $-0^{\prime \prime}$ |  | 1900 |
| 1760 | 0.016 | 1810 | 0.010 | 1860 | 0.003 | 1910 | +0.007 |
| 1770 | 0.015 | 1820 | 0.009 | 1870 | -0.001 | 1920 | 0.010 |
| 1780 | 0.014 | 1830 | 0.007 | 1880 | +0.001 | 1930 | 0.013 |
| 1790 | 0.012 | 1840 | 0.006 | 1890 | 0.004 | 1940 | 0.020 |
| 1800 | -0.011 | 1850 | -0.005 | 1900 | +0.007 | 1950 | +0.023 |

EQUATION OF TILE CENTRE, FOR $\mathrm{m}=0$.
Constant added $47^{\prime} 3^{\prime \prime} .5$. Period $=294.7003$.

| Arg. I. | ${ }_{0}^{d}$ | $\begin{gathered} \text { Diff. } \\ \text { for } 0.1 \end{gathered}$ | $\stackrel{d}{\mathrm{~d}} .1$ | $\begin{gathered} \text { Diff. } \\ \text { for } 0 \mathrm{~d} .1 \end{gathered}$ | $\begin{gathered} \mathrm{d} \\ 0.2 \end{gathered}$ | $\begin{gathered} \text { Viff. } \\ \text { for } 0^{d} .1 \end{gathered}$ | ${ }_{0}^{\mathrm{d}} .3$ | $\left\|\begin{array}{c} \text { Diff. } \\ \text { for } 0 \mathrm{~d} .1 \end{array}\right\|$ | $\begin{aligned} & d \\ & 0.4 \end{aligned}$ | $\underset{\substack{\text { Diff. } \\ \text { for } 0 \mathrm{~d} .1}}{\text {. }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }_{0}^{\text {d }}$ | O 4783.150 | +7.96 | 4 ${ }^{1} 11.146$ | +7.96 | $47^{1} 19.42$ | +7.93 | $4{ }^{\frac{1}{4}}{ }^{2} 7^{\prime \prime} 138$ | +7.96 | 47\% 3íl 35 | +7.96 |
| 1 | 04823.11 | 7.96 | 4831.07 | 7.96 | 48 39.03 | +7.96 | 4846.98 | ${ }^{7.96}$ | 48 54.94 | 7.05 |
| 2 | 049 42. (\%) | 7.95 | 4950.60 | 7.95 | 4958.55 | 7.05 | $50 \quad 6.50$ | 7.94 | 5014.44 | 7.94 |
| 3 | 0512.07 | 7.93 | 5110.00 | 7.93 | 5117.93 | 7.93 | 5125.86 | 7.33 | 51 33.79) | 7.92 |
| 4 | 05221.30 | 7.01 | 52.29 .21 | 7.91 | 5237.11 | 7.91 | 5245.02 | . 90 | 5953.92 | . 20 |
| 5 | 05340.27 | 7.88 | 53848.15 | 7.88 | 5356.02 | 7.88 | it 3.90 | 7.87 | 5411.7 | 7.87 |
| i | 0.5458 .92 | 7.85 | 5.518 .77 | 7.84 | 5514.61 | 7.84 | 55 2\%.4 | 7.84 | 55130.28 | 7.83 |
| 7 | 05617.19 | 7.81 | 5025.00 | 7.80 | 5632.70 | 7.80 | 5640.59 | 7.79 | 5648.38 | 7.is |
| 8 | 05735.02 | 7.76 | 5742.78 | 7.75 | 5750.53 | 7.75 | 5758.27 | 7.74 | $58 \quad 6.01$ | 7.74 |
| 9 | $058 \cdot 5.234$ | 7.70 | 59 | 7.70 | 597.74 | 7.63 | 5915.43 | 7.69 | 59 23.11 | 7.68 |
| 10 | 100.09 | 7.64 | 016.74 | 7.64 | 024.37 | 7.63 | 033.00 | 7.63 | 039.69 | 7.69 |
| 11 | 1125.22 | 7.58 | 133.79 | 7.57 | 140.36 | 7.56 | 147.92 | 7.56 | 155.48 | 7.55 |
| 12 | 1240.65 | 7.51 | 248.15 | 7.50 | 255.65 | 7.49 | $3 \quad 3.14$ | 7.48 | 310.62 | 7.48 |
| 13 | $1 \begin{array}{llll}1 & 3 & 55.33\end{array}$ | 7.43 | 42.76 | 7.42 | 410.17 | 7.41 | 417.58 | 7.40 | 424.98 | 7.40 |
| 14 | 1500 | 7.31 | 516.54 | 7.34 | 523.88 | 7.33 | 531.20 | 7.32 | 538.51 | 7.31 |
| 15 | 1622.21 | 7.25 | 620.46 | 7.24 | 630.50 | 7.24 | 643.03 | 7.23 | 651.15 | 7.29 |
| 16 | 1784.28 | 7.16 | 741.44 | 7.15 | 748.58 | \%. 14 | 75.5 .71 | 7.13 | $8 \quad 2.8 .1$ | 7.12 |
| 17 | 1845.37 | 7.06 | 852.43 | 7.05 | 859.47 | 7.04 | $9 \quad 6.50$ | 7.93 | 913.52 | 7.01 |
| 18 | 1 9) 55.4.2 | 6.95 | $\begin{array}{ll}10 & 2.37\end{array}$ | 6.94 | 109.30 | 6.93 | 10 16:22 | 6.92 | 1023.14 | 6.91 |
| 19 | 1114.37 | 6.81 | 1111.20 | 6.83 | 1118.03 | 6.82 | 1124.83 | 6.80 | 1131.63 | 6.79 |
| 20 | 11212.17 | 6.72 | 1218.89 | 6.71 | 1225.59 | 6.70 | 1232.28 | 6.6 | 1238.96 | 6.67 |
| 21 | 11318.77 | 6.60 | 13 25.36 | 6.58 | 1331.94 | 6.5 | 1338.50 | 6.56 | 1345.06 | 6.55 |
| 22 | 11424.10 | 6.17 | 1430.57 | 6.46 | 1437.02 | 6.44 | 1443.45 | 6.43 | 1449.87 | 6.1 |
| 23 | 11528.13 | 6.34 | 1534.46 | 6.32 | 1540.78 | 6.31 | 1547.08 | 6.29 | 1553.36 | 6.98 |
| 24 | 11630.80 | 6.20 | 1636.99 | 6.19 | 1643.16 | 6.17 | 1649.32 | 6.16 | 1655.47 | 6.14 |
| 2.5 | 11733.05 | 6.05 | 1738.10 | 6.04 | 1744.13 | 6.02 | 1750.15 | 6.01 | 1756.15 | 6.00 |
| 26 | 11831.85 | 5.90 | 1837.75 | 5.89 | 1843.63 | 5.87 | 18 49,50 | 5.86 | 1855.35 | 5.84 |
| 27 | 11930.15 | 5.75 | 1935.89 | 5.74 | 1941.62 | 5.72 | 1947.33 | 5.71 | 1953.03 | 5.69 |
| 28 | 12026.89 | 5.59 | 2032.47 | 5.58 | 2033.05 | 5.56 | 2043.60 | 5.55 | 2049.14 | 5.53 |
| 29 | 12122.04 | 5.43 | 2127.46 | 5.42 | 2132.87 | 5.40 | 2138.26 | 5.38 | 2143.64 | 5.37 |
| 30 | 12215.55 | 5.27 | 2220.81 | 5.25 | 2226.05 | 5.23 | 2231.27 | 5.21 | 2236.48 | 5.20 |
| 31 | 1237.38 | 5.10 | 2312.47 | 5.08 | 2317.54 | 5.06 | 2322.59 | 5.05 | 23.27 .63 | 5.03 |
| 32 | 12357.49 | 4.92 | 242.40 | 4.90 | 247.30 | 4.89 | 2412.18 | 4.87 | 2417.04 | 4.85 |
| 33 | 12445.84 | 4.75 | 2450.58 | 4.73 | 2455.29 | 4.71 | 2.50 .00 | 4.63 | 254.68 | 4.67 |
| 34 | 12.539 .39 | 4.56 | 25364.95 | 4.35 | 2541.49 | 4.33 | 2546.00 | 4.51 | 2.550 .50 | 4.49 |
| 35 | 12617.12 | 4.38 | 2621.49 | 4.36 | 2625.84 | 4.34 | 2630.17 | 4.32 | 2634.49 | 4.30 |
| 36 | 12659.97 | 4.19 | $\begin{array}{lll}27 & 4.15\end{array}$ | 4.17 | $27 \quad 8.32$ | 4.15 | 2712.46 | 4.13 | 2716.59 | 4.11 |
| 37 | 12740.93 | 4.00 | 2744.92 | 3.98 | 2748.89 | 3.96 | 2752.84 | 3.94 | 2756.77 | 3.92 |
| 38 | 12819.96 | 3.80 | 28 23.75 | 3.78 | 28.27 .53 | 3.77 | 2831.28 | 3.75 | 28 35.02 | 3.73 |
| 31 | 12857.02 | 3.61 | 29 0.62 | 3.59 | $29 \quad 4.20$ | 3.57 | 297.76 | 3.55 | 2911.29 | 3.53 |
| 40 | 12932.10 | 3.41 | 2935.50 | 3.39 | 2938.87 | 3.37 | 29.42 .23 | 3.35 | 29 45.57 | 3.33 |
| 41 | $130 \quad 5.16$ | 3.20 | $30 \quad 8.36$ | 3.18 | 3011.53 | 3.16 | 3014.69 | 3.14 | 3017.82 | 3.12 |
| 42 | 13036.19 | 3.00 | 3039.18 | 2.98 | 3048.14 | 2.96 | 3045.09 | 2.94 | 3048.02 | 2.32 |
| 43 | 1315.15 | 2.79 | 317.93 | 2.77 | 3110.69 | 2.75 | 3113.43 | 2.73 | 3116.15 | 2.71 |
| 44 | 13132.02 | 2.58 | 3131.59 | 2.56 | 3137.15 | 2.54 | 3139.68 | 2.52 | 31 42.18 | 2.50 |
| 4.5 | 13156.80 | 2.377 | 3159.16 | 2.35 | 321.50 | 2.33 | 323.81 | 2.31 | 3.26 .11 | 2.22 |
| 46 | 13219.45 | 2.16 | 32.21 .59 | 9.14 | 32 23.72 | 2.12 | 32 25.83 | 2.03 | 3.2 27.91 | 2.07 |
| 47 | 13239.96 | 1.91 | 3.41 .89 | 1.92 | 3243.80 | 1.90 | 3245.69 | 1.67 | 3947.56 | 1.85 |
| 48 | 13258.32 | 1.73 | 3830.04 | 1.71 | 331.73 | 1.68 | $33 \quad 3.40$ | 1.66 | $33 \quad 5.015$ | 1.64 |
| 49 | 133314.51 | 1.51 | 3:3 16.01 | 1.49 | 3317.49 | 1.47 | 3318.95 | 1.44 | $33320: 38$ | 1.42 |
| 50 | 133328.53 | 1.29 | :333 29.81 | 1.97 | 3331.07 | 1.25 | 33.39 .30 | 1.23 | 333 33.5. | 1.20 |
| 51 | 133440.36 | 1.08 | 3341.42 | 1.05 | 3342.46 | 1.03 | 3343.48 | 1.01 | 3344.47 . | 0.93 |
| 52 | 13345999 | 0.85 | 3350.83 | 0.83 | 3351.95 | 0.81 | 33.59 .45 | 0.79 | 33 53.23 | 0.76 |
| 53 | 133357.43 | 0.63 | 33.58 .05 | 0.61 | 3:3 58.6.3 | 0.59 | 3359.23 | , | 33359.78 | 0.54 |
| 51 | 1342.66 | 0. 41 | $31 \quad 3.06$ | 0.30 | 313.41 | 0.37 | $34 \quad 3380$ | 0.35 | $34^{2} 4.13$ | 0.32 |
| 55 | 1345.18 | +0.19 | $31 \quad 5.86$ | +0.17 | $31 \quad 6.02$ | +0.15 | 316 | +0.13 | 346.27 | +0.10 |

EQUATION OF THE CENTRE, FOR $\mathrm{m}=0$.
Constant added 4r'3 $3^{\prime \prime} 5 . \quad$ Period $=224 . \% 008$.


8 V

EQUATION OF THE CENTRE, FOR RE $=0$.
Constant added $47^{\prime} 3 \prime \prime .5$. Period $=29.4 .7008$.

| Arg. 1. | $\frac{d}{0.0}$ | $\begin{gathered} \text { Diff. } \\ \text { for } 00^{d}, 1 \end{gathered}$ | $\begin{gathered} \mathrm{d} \\ 0.1 \end{gathered}$ | $\begin{gathered} \text { Diff. } \\ \text { for } 8.1 \end{gathered}$ | $0.2$ | $\begin{gathered} \text { Wiff. } \\ \text { for } 0^{d} .1 \end{gathered}$ | $\frac{d}{0.3}$ | $\left\lvert\, \begin{gathered} \text { Diff: } \\ \text { for } 0 \mathrm{~d} .1 \end{gathered}\right.$ | $\frac{d}{0.4}$ | $\begin{gathered} \text { Dill: } \\ \text { for } 04.1 \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 56 | i 311 ¢1. 19 | ${ }_{-0.03}$ | 310.15 | -0.05 | 318 | -0.07 | $3{ }^{3} \quad 60.31$ | -0.09 | 34 6.20 | -0.12 |
| 57 | $1: 315.10$ | 0.25 | $34 \quad 4.84$ | 0.37 | 314.50 | 0.29 | 34 4.25, | 0.32 | $34 \quad 3.93$ | , |
| 53 | $1: 311.50$ | 0.47 | 3.1 .02 | 0.19 | 31.0 .5 | 0.51 | 33359.99 | 0.54 | :333 59.45 | 0.56 |
| 59 | $1: 3355.71$ | 0.63 | 3355.01 | 0.71 | 3354.28 | 0.73 | 3353.54 | 0.75 | 3352.77 | 0.78 |
| (i0) | 133347.72 | 0.91 | 33346.80 | 0.93 | 3345.86 | 0.95 | 3344.89 | 0.97 | 3343.91 | 1.00 |
| (i1 | 133337.51 | 1.13 | 33.36 .10 | 1.15 | 33335.24 | 1.17 | 33334.06 | 1.19 | 333 32.86 | 1.21 |
| 69 | 1 1:3 2.5 .19 | 1.34 | 33323.383 | 1.37 | : 23 22.4. | 1.39 | 3321.06 | 1.41 | 33 19.64 | 1.43 |
| 63 | $1: 3310.67$ | 1.56 | 339.10 | 1.58 | $33 \quad 7.51$ | 1.60 | $33 \quad 5.89$ | 1.62 | $33 \quad 4.20$ | 1.65 |
| 61 | 132 54.00 | 1.77 | 3252.21 | 1.80 | 3250.41 | 1.82 | 3248.58 | 1.84 | 3246.73 | 1.86 |
| 6.5 | 13.3 3.3.19 | 1.98 | 3.33 .19 | 2.01 | 3231.17 | 2.03 | 32 29.13 | 2.05 | 3927.07 | 2.07 |
| $6{ }^{6}$ | $\begin{array}{llll}1 & 3 & 1.14 .96 \\ 1 & 1 & 51.2\end{array}$ | 2.20 | 3312.05 | 2.22 | 3398.89 | 2.24 | 327.57 | 2.26 | 32 5.29 | 2.28 |
| 67 | 13151.2 | 2.11 | 3148.80 | 2.43 | 3140.37 | 2.4 | 3143.91 | 2.47 | 3141.42 | 2.49 |
| 68 | 13126.10 | 2.62 | 3123.48 | 2.64 | 3120.83 | 2.66 | 3118.16 | 2.68 | 3115.47 | $2 . \%$ |
| 69 | 13058.92 | 2.63 | 3056.09 | 2.84 | 30 5:3.23 | 2.86 | 30 50.36 | 2.88 | 3047.47 | 2.90 |
| 70 | 13029.69 | 3.02 | 3026.66 | 3.04 | 3023.60 | 3.06 | 3020.53 | 3.08 | 3017.43 | 3.10 |
| 71 | 1 123 58.45 | 3.22 | 2155.21 | 3.24 | 2951.96 | 3.26 | 2948.68 | 3.28 | 2345.39 | 3.30 |
| 72 | 1 29) 2.5 .21 | 3.42 | 2921.78 | 3.44 | 2918.33 | 3.46 | 2914.86 | 3.48 | 2.911 .37 | 3.50 |
| 73 | 128.00 .01 | 3.62 | 2846.38 | 3.64 | 28 42.74 | 3.66 | 2839.07 | 3.68 | 2835.39 | 3.69 |
| 74 | 12819.88 | 3.81 | 28 9.0.5 | 3.83 | 28.5 .22 | 3,85 | 281.36 | 3.87 | 2757.48 | 3.89 |
| 75 | 12833.36 | 4.00 | 2729.82 | 4.02 | 27 25.7! | 4.04 | 2721.75 | 4.05 | 2717.68 | 4.07 |
| 76 | 12659.91 | 4.18 | 2648.71 | 4.20 | 2644.50 | 4.22 | 2640.27 | 4.24 | 2635.02 | 4.26 |
| 77 | 12610.14 | 4.37 | 26.5 .77 | 4.38 | 261.37 | 4.40 | 25 56.96 | 4.42 | 25.52 .53 | 5.44 |
| 78 | 12.523 .57 | 4.55 | 2521.02 | 4.56 | 2.516 .44 | 4.58 | 2511.85 | 4.60 | 2.57 .24 | 4.62 |
| 79 | 12439.23 | 4.72 | 2431.50 | 4.74 | 24 20.\% | 4.76 | 2424.18 | 4.97 | 2420.20 | 4.79 |
| 80 | 12351.14 | 4.89 | 2346.24 | 4.91 | 2341.32 | 4.93 | 2336.39 | 4.94 | 2331.43 | 4.96 |
| 81 | 1231.35 | 5.06 | 22 56.29 | 5.08 | 2251.21 | 5.09 | 2246.10 | 5.11 | 2240.98 | 5.13 |
| $8:$ | 1229.92 | 5.23 | 22 4.63 | 5.24 | 2159.44 | 5.56 | 2154.17 | 5.27 | 2148.89 | 5.29 |
| 83 | 12116.86 | 5.39 | 2111.47 | 5.40 | 21.6 .06 | 5.42 | 210.63 | 5.43 | 2055.19 | 5.45 |
| 81 | 12022.23 | 5.54 | $20 \cdot 16.68$ | 5.56 | 2011.12 | 5.57 | $\begin{array}{ll}20 & 5.54\end{array}$ | 5.59 | 1950.94 | 5.60 |
| 85 | 119 26.06 | 5.69 | 1920.36 | 5.71 | 1914.64 | 5.72 | 198.91 | 5.74 | 19. 3.17 | 5.75 |
| 86 | 11828.39 | 5.84 | 1822.55 | 5.85 | 1816.69 | 5.87 | 1810.81 | 5.88 | 184.92 | 5.90 |
| 87 | 11723.29 | 5.98 | 1723.30 | 5.99 | 1717.30 | 6.01 | 1711.28 | 6.02 | $17 \quad 5.25$ | 6.0 |
| 88 | 11628.78 | 6.12 | 1622.65 | 6.13 | 1616.51 | 6.15 | 1610.36 | 6.16 | 164.19 | 6.18 |
| 89 | 11526.92 | 6.25 | 1520.66 | 6.26 | 1514.39 | 6.28 | 158.10 | 6.29 | 15.1 .81 | 6.30 |
| 90 | 11423.75 | 6.38 | 14 17.37 | 6.39 | 1410.97 | 6.40 | $14 \quad 4.56$ | 6.42 | 1358.13 | 6.43 |
| 91 | 11319.33 | 6.50 | 1312.82 | 6.51 | 136.30 | 6.53 | 1259.77 | 6.54 | 1253.22 | 6.545 |
| 92 | 11213.70 | 6.63 | 127.08 | 6.63 | 120.44 | 6.64 | 1153.79 | 6.66 | 1147.13 | 6.67 |
| 93 | 1116.92 | 6.73 | 11.0 .18 | 6.75 | 1053.43 | 6.76 | 1046.67 | 6.77 | 1039.89 | 6.78 |
| 94 | 1959.03 | 6.84 | 952.19 | 6.85 | 945.33 | 6.86 | 938.46 | 6.87 | 931.58 | 6.88 |
| 95 | 1850.09 | 6.94 | 843.14 | 6.95 | 836.18 | 6.96 | 829.22 | 6.97 | 822.24 | 6.98 |
| 96 | 1740.16 | 7.04 | 733.11 | 7.05 | 726.05 | 7.06 | 718.09 | 7.07 | 7.11 .91 | 7.08 |
| 97 | 1629.27 | 7.13 | 622.14 | 7.14 | 614.99 | 7.15 | 67.83 | 7.16 | 60.67 | 7.17 |
| 98 | 1517.50 | 7.22 | 510.28 | 7.23 | $5 \quad 3.05$ | 7.24 | 455.80 | 7.24 | 448.56 | 7.25 |
| 99 | $\begin{array}{llll}1 & 4 & 4.89\end{array}$ | 7.30 | 357.59 | 7.31 | 350.28 | 7.32 | 342.96 | 7.32 | 335.63 | 7.33 |
| 100 | 1251.51 | 7.38 | 244.13 | 7.38 | 236.74 | 7.39 | 220.35 | 7.40 | 221.94 | 7.40 |
| 101 | $1 \begin{array}{llll}1 & 1 & 37.39\end{array}$ | 7.45 | 129.95 | 7.45 | 122.49 | 7.46 | 115.03 | \%.46 | 17.56 | 7.47 |
| 102 | 06022.62 | 7.51 | 60 15. 11 | 7.51 | 607.59 | 7.52 | $\mathrm{c}_{5} 0.06$ | 7.53 | 5952.53 | 7.53 |
| 103 | 0597.23 | 7.57 | 5859.66 | 7.57 | 5852.08 | 7.58 | 5844.50 | 7.58 | 5836.91 | 7.59 |
| 104 | 05751.29 | 7.62 | 5743.67 | 7.62 | 57.36 .04 | 7.63 | 5728.41 | 7.63 | 5720.77 | 7.64 |
| 105 | 05634.86 | 7.67 | 5627.19 | 7.67 | 5619.52 | 7.67 | 5611.84 | 7.68 | $56 \quad 4.16$ | 7.68 |
| 106 | $\begin{array}{lll}0 & 5.517 .99\end{array}$ | 7.71 | 5510.28 | 7.71 | 55.2 .56 | 7.71 | 5454.85 | 7.82 | 5147.13 | 7.72 |
| 107 | $054 \quad 0.74$ | 7.,44 | 5353.00 | 7.74 | 5345.25 | 7.75 | 5337.50 | 7.85 | 5329.75 | 7.75 |
| 108 | 05243.18. | 7.77 | 5235.40 | 7.97 | 52.27 .63 | 7.77 | 5219.85 | 7.78 | 5212.07 | 7.7 |
| 109 | 05125.35 | 7.79 | 5117.56 | 7.79 | 51.9 .76 | 7.80 | 51.96 | 7.80 | 5054.16 | 7.80 |
| 110 | 0507.33 | 7.81 | 4953.52 | . 81 | 4951.71 | 7.81 | 4943.89 | \%.81 | 4936.08 | 7.82 |
| 111 | 04849.17 | -7.82 | 4841.34 | -i.82 | 4833.52 | -7.82 | 4825.70 | -7.82 | 4817.87 | -7.82 |

RQUATION OF THE CENTRE，FOR $\mathrm{m}=0$ ．


| Arg． 1 | $0.5$ | $\left\|\begin{array}{c} 1 \text { itli: } \\ \text { far } 0 \text { d } \end{array}\right\|$ | ${ }^{11} .6$ |  | $0.7$ | Dill： for $\mathrm{int}_{\mathrm{t}} 1$ | $0.8$ | $\left\lvert\, \begin{gathered} \text { Mifl: } \\ \text { for }()^{2}, i \end{gathered}\right.$ | $0.0$ | $\begin{gathered} \text { Bitl: } \\ \text { for (0d. } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sid | 1 ：11 6́． 0 \％ | －0．11 | 31 \％\％in | －0．16 | 3．6 5．5．5 | ${ }_{-0.1 \times}$ | 315 | －0．21 | ：14 5．1．31 | ${ }_{-0.23}^{11}$ |
| 57 | 13113.5 \％ | 0.36 | 3.43 .21 | 0.38 | il 2.81 | 0.40 | 3112.10 | 0.43 | 341.16 | $0 . \%$ |
| 58 | $1: 51588.58$ | 0.58 | ：31 5x．ent | 0.60 | ： 3 37．18 | 0.62 | 33 57.04 | 0．c5 | ：33 54， 518 | 0.67 |
| 59 | $1: 35$ 51．．！${ }^{1}$ | 0.50 | 23351.18 | 0.82 | 3：3 50.31 | 0.81 | 2514！．49 | 0.10 | 3：3 48．6il | 0.88 |
| 16 | 12314390 | 1．02 | 233 11.87 | 1.01 | ：3 40.8 ？ | 1.06 | $3: 13007$ | 1.08 | ：4］ 38.6 | 1.10 |
| （i） | $1: 33$ 31．13 | 1.21 | ：33 310.13 | 1.96 | ：33 20．1．13 | 1.28 | i31 27.58 | 1.50 | ：3） 210.5 | 1.33 |
| 1：3 | $1: 3118.20$ | 1.15 | 3：1111．78 | 1.17 | ：5315．95 | 1.49 | 23）1：1．74 | 1．ris | ：33 13， 23 | 1.54 |
| 131 | $13: 32.60$ | 1.67 | 33 0．5） | 1.69 | 3259．22 | 1.71 | 32.57 .50 | 1.63 | 3：2 55.76 | 1．\％5 |
| 6 | 1 53 44．2： | 1.88 | 129 4． 4.17 | 1.90 | 3241.05 | 1.92 | 13 3！ 319 | 1.91 | 3：3 37.17 | 1.97 |
| （i） | $1: 5221.519$ | 2.09 | 32）20． 88 | 2.11 | 35 $20 . ⿱ 亠 乂 口$ | 2.14 | ［12 18．6il | 4.16 | ［52 16.45 | 2.18 |
| （i） | $1: 138.00$ | 2.30 | 32.30 .6 | 2.39 | ：11 58．0\％ | 2.35 | ：11 51i．00 | 2.17 | ：31 5is．tie | 2.15 |
| bĩ | $13138 . .12$ | 2.51 | 3136.40 | 2.53 | $313: 3.86$ | 2.35 | ：11 31．26） | 2.57 | ：31 21． 11 | 2.59 |
| 628 | 13119.77 | 2.62 | 31110.04 | 2.74 | 31789 | 2.76 | 3114.59 | 2.78 | 311.73 | 2.80 |
| 6： | 13044.56 | 2.92 | 30.41 .121 | 2.94 | ：30 28． 67 | 2.96 | ：10 3．5． 0 | 2.98 | $30.3 \cdot 2.71$ | 3.00 |
| 70 | $13014.3:$ | 3.12 | 30 11．19 | 3.14 | $30 \quad 80.03$ | 3.16 | $30 \quad 4.86$ | 3.18 | i0 l． 36 | 3.30 |
| 71 | 12944.08 | 3.32 | 20138.74 | 3.31 | 2935.39 | 3.36 | 2．） 32.02 | 3.38 | ge） 28.63 | 3.10 |
| 72 | 120786 | 352 | 29） 4.33 | 3.54 | 290.78 | 3.56 | 28.57 .21 | 3.58 | 28 5．3．62 | 3.60 |
| 73 | 12831.68 | 3.71 | 9827.16 | 3.73 | 28.21 .29 | 3．75 | 28.20 .46 | 3.77 | 2816.68 | 3.59 |
| 71 | 197853.59 | 3.90 | 27 49， 67 | 8.92 | 2745.7 .4 | 3.94 | $27+1.7!$ | 3.96 | 27.37 .82 | 3.98 |
| 75 | 12713.60 | 4.03 | $27 \quad 9.50$ | 4.11 | $27 \quad 5.33$ | 4.13 | $27 \quad 1.24$ | 4.15 | 31） 57.08 | 4.17 |
| 76 | 12031.75 | 4.28 | $21 ; 27.47$ | 4.29 | 26.23 .16 | 4.31 | 2618.84 | 4.33 | 2614.50 | 4.35 |
| 78 | 1 25 48．08 | 4.46 | 2．7 4：3．62 | 4.47 | 25.39 .13 | 4.19 | 2.53 .1 .6 | 4.51 | 2.730 .11 | 4 4 －13 |
| 78 |  | 4.63 | 2.157 .18 | 4.65 | 24533.31 | 4.67 | 2148.16 | 4.69 | 24.43 .94 | 4.70 |
| $7: 1$ | 12415.40 | 4.81 | 2410.58 | 4.83 | 245.75 | 4.84 | $24 \quad 0.30$ | 4．66 | 2356.03 | 4.88 |
| 80 | 12326.46 | 4.98 | 2321.48 | 4.93 | 2316.47 | 5.61 | 2311.45 | 5.03 | $23 \quad 6.42$ | 5.04 |
| 81 | $122: 35.85$ | 5.14 | 23：30．70 | 5.16 | 2925.53 | 5.18 | 22.20 .34 | 5.19 | 21 15．14 | 5.21 |
| R2 | 121483.55 | 5.31 | 2138.28 | 5.32 | 2132.95 | 5.34 | 2127.60 | 5.35 | 2123.21 | 5.37 |
| ¢3 | 12049.5 | 5.47 | 20.44 .27 | 5.48 | 2038.78 | 5.50 | 2033.28 | 5.51 | 2027.76 | 5.53 |
| 81 | 119 ：4．333 | 5.61 | 1948.71 | 5.63 | 1943.07 | 5.64 | 1937.41 | 5.66 | 1931.74 | 5.687 |
| 85 | 118.77 .41 | 5.77 | 18.51 .63 | 5.78 | 1845.85 | 5.80 | 1840.04 | 5.81 | 18.31 .23 | 5.82 |
| 86 | 11759.09 | 5.91 | 17.53 .10 | 5.93 | 1747.17 | 5.91 | 1741.22 | 5.95 | 17 3．5． 46 | 5.97 |
| 87 | 11659.20 | 6.05 | 1653.15 | 6.06 | 1647.07 | 6.08 | 16 40．95） | 6.09 | 1 （ 31.6 ） | 6.10 |
| 88 | 11558.01 | 6.19 | 1．5） 51.82 | 6.20 | 154.5 .62 | 6.21 | 15139．40 | 6.23 | $15.34 \% 16$ | 6.24 |
| $8!$ | 114585.50 | 6.32 | 1449.17 | 6.33 | 14.42 .84 | 6.34 | $14: 36.49$ | 6.35 | 1430.13 | 6.37 |
| 90 | $11: 3: 11.70$ | 6.44 | 1345.25 | 6.45 | 1338.79 | 6.16 | $133: 3.3 .31$ | 6.48 | 1：3 25.23 | 6.49 |
| 91. | 11246.65 | 6.56 | 1240.10 | 6.57 | 1233.52 | 6.59 | 1220.92 | 6.60 | 1220.3 ？ | 8.61 |
| 92 | 11140.45 | 6.68 | 1133.77 | 6.69 | 1127.07 | 6.70 | 1120.37 | 6.71 | 11 13．05 | 6.72 |
| 913 | $110: 333.11$ | 6.79 | 10 26．32 | 6.80 | 1019.51 | 6.82 | 1012.70 | 6.83 | $10 \quad 5.87$ | 6.84 |
| 9. | $1924.6 \%$ | 6.80 | 917.79 | 6.90 | ！ 10.88 | 6.91 | $9 \quad 33.97$ | 6.92 | 857.04 | 0.93 |
| 95 | 1815.25 | 6.99 | $8 \quad 8.25$ | 7.60 | $8 \quad 1.24$ | 7.01 | 754.22 | 7.02 | 747.19 | 7.03 |
| 96 | 174.83 | 7.09 | 657.7 .1 | 7.10 | 6.50 .64 | 7.11 | ${ }^{6} 483.52$ | 7.12 | 636.40 | 7.12 |
| 97 | 1 1 5 53．50 | 7.18 | 5 16．31 | 7.19 | 539.19 | 7.13 | 531.93 | 7.20 | 524.72 | 7.21 |
| $!8$ | 14 ＋1．30 | 7.26 | 431.03 | 7.27 | 4 26．76 | 7.28 | 419.48 | 7.99 | 412.19 |  |
| ！） | 1328.30 | \％ 3.34 | 320.95 | 7.35 | 313.60 | 7.35 | 36.24 | 7.36 | 258.88 | 7．3\％ |
| 100 | 1214.51 | 7.41 | $\begin{array}{ll}2 & 7.12\end{array}$ | 7.12 | 159.70 | 7.42 | 15.5 .97 | 7.43 | 144.84 | 7.44 |
| 101 | $\begin{array}{lll}1 & 1 & 0.09 \\ 0 & 50 & 4100\end{array}$ | 7.48 | 052.60 | 7.48 | 045.12 | 7.43 | 0 37.62 | 7.50 | 030．19 | 7.50 |
| 109 | 059941.99 | 754 | 5937.45 | 7.54 | 59.50 .91 | 7 T 5 | 59.92 .35 | 756 | 5914.79 | 7.36 |
| 103 | 05829.32 | 785 | 5821.73 | 7.60 | 5814.12 | 7.60 | $58 \quad 6.52$ | 7.61 | 5758.91 | 7.61 |
| 104 | 05713.13 | 7.64 | $57 \quad 5.49$ | 7.65 | 5057.83 | 7.65 | 5650.18 | 7.66 | 5642.52 | 7.66 |
| 10.5 | 0 5．5 50.6 .47 | 7.69 | 5．5） 48.78 | 7.69 | 5.541 .09 | 7.69 | 5.3 3：3．3！ | 7.70 | 5.520 .69 | 7.70 |
| $10 \%$ | 0 5 5139.41 | 7.72 | 5131.68 | 7.73 | 5.123 .95 | 7.73 | 5416.22 | 7.73 | 5488.18 | － 7.74 |
| 107 | 05321.45 | 7.6 | 5314.23 | 7.76 | $53 \quad 6.47$ | 7.78 | 5258.71 | －7．78 | 5250.94 | 7.77 |
| 108 | 0524.29 | 7.88 | 5150.51 | 7.88 | 5148.72 | 7.79 | it 40.93 | 7.79 | 5133.14 | 7.79 |
| 10， | 05046.36 | 7.80 | $50: 38.56$ | 7．80 | 50.30 .75 | 7.81 | 5022.95 | 7.81 | 5015.14 | 7.81 |
| 110 | $04!28.21 \%$ | 7.28 | 4920.45 | 7.83 | 49 19． 6.3 | 7．82 | 494.81 | 7．08 | 48 53．9．9 | 7.82 |
| 111 | $048 \quad 10.05$ | $-7.89$ | 48 2．2：1 | －i．82 | 475.4 .40 | $-7.83$ | 4746.57 | $-7.83$ | 4738.75 | $-7.83$ |

EQUATION OF TIIE CENTRE, FOR $\mathbf{m}=\mathbf{0}$.
Constint added $48^{\prime} 3 / 3.5 . \quad$ Period $=20.1 .0008$.

| Arg. 1. | $0.0$ | $\begin{gathered} \text { Ditld: } \\ \text { for } 0^{\mathrm{d}} .1 \end{gathered}$ | $\stackrel{11}{1}_{0.1}$ | $\begin{gathered} \text { Bill. } \\ \text { for } 0 \mathrm{~d} .1 \end{gathered}$ | ${ }_{0.2}^{d}$ | $\begin{aligned} & \text { Ditl: } \\ & \text { for } 0^{d} .1 \end{aligned}$ | $\begin{gathered} d \\ 0.3 \end{gathered}$ | $\begin{gathered} \text { Diff. } \\ \text { for } 0 \mathrm{~d} .1 \end{gathered}$ | $\stackrel{\mathrm{d}}{0.4}$ | $\begin{aligned} & \text { Diff: } \\ & \text { for } 0^{d} .1 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 112 | ¢ 0478 | $\stackrel{11}{\text {-7. } 83}$ | 47823.10 | -718 | $47^{\prime} 15.27$ | -7183 | $47 \quad 81.44$ | ${ }_{-11}^{1 / 83}$ | $4\left(\mathrm{j} 50{ }^{\prime \prime} 62\right.$ | -7.83 |
| 113 | 04619.66 | 7.82 | 46 4.83 | 7.82 | 45.57 .01 | 7.82 | 4549.19 | 7.82 | 4.541 .36 | 7.82 |
| 114 | 044 51.4:3 | 7.82 | 4446.61 | 7.82 | $44: 33.80$ | 7.82 | 4430.98 | 7.81 | 4123.17 | 7.81 |
| 115 | 04336.31 | 7.81 | 4328.50 | 7.80 | $4: 320.70$ | 7.80 | 4312.90 | 7.80 | $43 \quad 5.10$ | 7.80 |
| 116 | 04218.34 | 7.79 | 4210.55 | 7.88 | $42 \quad 2.77$ | 7.88 | 41.51 .09 | 7.78 | 4147.21 | 7.78 |
| 117 | 0410.59 | 7.76 | 40 \% 50.8 | 7.76 | 40 45.07 | 7.76 | 40.37 .31 | 7.75 | 4021.56 | 7.75 |
| 118 | 03943.11 | 7.73 | 3935.38 | 7.73 | 34927.65 | 7.12 | 39) 19.95 | 7.5 | 3912.21 | 7.72 |
| 119 | 03825.97 | 7.69 | 3818.28 | 7.69 | 3810.59 | 7.69 | $38 \quad 2.90$ | 7.68 | 3755.22 | 7.68 |
| 120 | 0.37 ! 1.23 | 7.65 | $37 \quad 1.58$ | 7.6. | 30.53 .93 | 7.64 | 3046.29 | 7.64 | 3638.65 | 7.f13 |
| 121 | $033.552 .0 \%$ | 7.60 | 3.745 .33 | 7.60 | 3.5137 .74 | 7.59 | 3530.14 | 7.59 | 35 2. 50 | 7.58 |
| 12: | 033137.15 | 7.55 | 3429.61 | 7.54 | 3422.06 | 7.54 | 3414.53 | 7.53 | 34 7.00 | 7.53 |
| 123 | 03321.94 | 7.49 | 3314.46 | 7.48 | 3336.97 | 7.48 | 3259.50 | 7.47 | 3252.03 | 7.46 |
| 124 | $032 \quad 7.36$ | 7.42 | 3159.94 | 7.42 | 31.52 .52 | 7.41 | 3145.12 | 7.40 | 3137.71 | 7.40 |
| 13.5 | 03053.46 | $7 \times 35$ | 3046.11 | 7.35 | 30 :38.77 | 7.34 | 30.31 .43 | 7.33 | 30.24 .11 | 7.32 |
| 126 | 0 O29 40.30 | \%.28 | 29) 33.03 | 7.27 | 2925.76 | 7.96 | 2918.51 | 7.95 | 2911.26 | 7.24 |
| 127 | 02827.94 | 7.19 | 28.20 .75 | 7.19 | $28 \quad 13.57$ | 7.18 | $28 \quad 6.39$ | 7.17 | 2759.23 | 7.16 |
| 128 | 02716.43 | 7.11 | $27 \quad 9.32$ | 7.10 | $27 \quad 2.23$ | 7.09 | 2655.15 | 7.08 | 2648.07 | 7.07 |
| 129) | 0265.82 | 7.01 | 2.588 .81 | 7.00 | 25.51 .81 | 6.99 | 2544.83 | 6.98 | 2537.85 | 6.97 |
| 130 | 02156.18 | 6.91 | 2449.27 | 6.90 | 2442.37 | 6.89 | 2435.48 | 6.88 | 2428.60 | 6.87 |
| 131 | 02347.55 | 6.81 | 2340.75 | 6.80 | 2333.95 | 6.79 | 2327.17 | 6.18 | 2320.39 | 6.77 |
| 132 | 02939.99 | 6.70 | 2933.29 | 6.69 | 2926.61 | 6.68 | 2219.94 | 6.67 | 2213.27 | 6.66 |
| 133 | 02133.55 | 6.59 | 2126.97 | 6.57 | 2120.40 | 6.56 | 2113.84 | 6.55 | 217.30 | 6.54 |
| 134 | 02028.28 | 6.47 | 2021.82 | 6.45 | 2015.37 | 6.44 | $20 \quad 8.93$ | 6.43 | $20 \quad 2.51$ | 6.42 |
| 135 | 01924.23 | 6.34 | 1917.89 | 6.33 | 1911.57 | 6.32 | $19 \quad 5.26$ | 6.30 | 1858.96 | 6.29 |
| 136 | 01821.45 | 6.21 | 1815.24 | 6.20 | $18 \quad 9.05$ | 6.19 | $18 \quad 2.87$ | 6.17 | 1756.70 | 6.16 |
| 137 | 01719.99 | 6.08 | 1713.92 | 6.06 | $17 \quad 7.86$ | 6.05 | $17 \quad 1.82$ | 6.0 .1 | 16 55.79 | 6.02 |
| 138 | 01619,90 | 5.94 | 1613.96 | 5.92 | 1688.05 | 5.91 | $16 \quad 2.14$ | 5.90 | 1550.25 | 5.88 |
| 139 | 01521.22 | 5.80 | 1515.43 | 5.78 | $15 \quad 9.66$ | 5.77 | $15 \quad 3.90$ | 5.75 | 1458.15 | 5.74 |
| 140 | 01424.00 | 5.65 | 1418.36 | 5.63 | 1412.73 | 5.62 | $14 \quad 7.12$ | 5.61 | $14 \quad 1.53$ | 5.59 |
| 141 | 01328.28 | 5.49 | 1:3 22.79 | 5.48 | 1317.32 | 5.46 | 1311.87 | 5.45 | $13 \quad 6.43$ | 5.43 |
| 142 | 0 12 34.12 | 5.34 | 1228.79 | 5.32 | 1223.47 | 5.31 | 1218.17 | 5.99 | 1212.89 | 5.27 |
| 143 | $\begin{array}{lllll}0 & 11 & 41.54\end{array}$ | 5.18 | $11: 36.37$ | 5.17 | 1131.22 | 5.15 | 1126.08 | 5.13 | 11.20 .96 | 5.11 |
| 144 | 01050.59 | 5.01 | 1045.59 | 5.00 | 1040.60 | 4.98 | 10 3.).03 | 4.96 | 1030.68 | 4.94 |
| 145 | $\begin{array}{llll}0 & 10 & 1.3\end{array}$ | 4.84 | 9) 56.48 | 4.83 | 951.66 | 4.81 | 946.86 | 4.79 | 942.08 | 4.77 |
| 146 | 0 0 013.75 | 4.67 | $9 \quad 9.09$ | 4.65 | 94.45 | 4.63 | 859.82 | 4.62 | 855.21 | 4.60 |
| 147 | $0 \quad 827.3$ | 4.43 | 823.45 | 4.47 | 818.98 | 4.46 | 814.54 | 4.41 | 810.11 | 4.42 |
| 148 | $\begin{array}{lll}0 & 7 & 43.90\end{array}$ | 4.31 | 739.60 | 4.29 | 735.31 | 4.28 | 731.04 | 4.26 | 726.80 | 4.24 |
| 149 | $\begin{array}{llll}0 & 7 & 1.69\end{array}$ | 4.13 | 657.57 | - 4.11 | 6 5:3.47 | 4.69 | 649.38 | 4.07 | 645.32 | 4.05 |
| 150 | 0 0 $\quad 121,33$ | 3.94 | 617.39 | 3.92 | 613.48 | 3.90 | 6 9.59 | 3.89 | $6 \quad 5.71$ | 3.87 |
| 151 | $\begin{array}{llll}0 & 5 & 42.85\end{array}$ | 3.75 | 539.11 | 3.73 | 535.38 | 3.71 | 531.68 | 3.69 | 528.00 | 3.68 |
| -152 | $\begin{array}{llll}0 & 5 & 6.29\end{array}$ | 3.50 | $5 \quad 2.74$ | 3,54 | 459.21 | 3,52 | 4 55.70 | 3.50 | 452.21 | 3.48 |
| 153 | 0431.68 | 3.36 | 428.32 | 3.34 | 424.99 | 3.32 | 421.68 | 3.30 | 418.38 | 3.28 |
| 154 | $\begin{array}{llll}0 & 3 & 59.04\end{array}$ | 3.16 | 35.5 .88 | 3.14 | 352.75 | 3.13 | 349.63 | 3.10 | 346.54 | 3.08 |
| 155 | $0 \quad 328.40$ | 2.96 | 325.44 | 2.94 | 322.51 | 2.92 | 319.60 | 2.90 | 316.70 | 2.88 |
| 156 | $\begin{array}{lll}0 & 2 & 59.78\end{array}$ | 2.70 | 2 5\%.03 | 2.74 | 254.30 | 2.72. | 251.59 | 2.70 | 248.90 | 2.68 |
| 157 | $\begin{array}{llll}0 & 2 & 33.21\end{array}$ | 2.55 | 230.67 | 2.53 | 228.14 | 2.51 | 2 2.7.64 | 2.49 | 223.16 | 2.47 |
| 158 | $\begin{array}{llll}0 & 2 & 8.71\end{array}$ | 2.35 | 26.38 | 2.32 | 24.06 | 2.30 | 21.77 | 2.28 | 159.50 | 2.26 |
| 159 | $0 \quad 146.31$ | 2.13 | 144.18 | 2.11 | 142.08 | 2.09 | 140.00 | 2.07 | 137.94 | 2.05 |
| 160 | $0 \quad 126.01$ | 1.92 | 124.10 | 1.90 | 122.21 | 1.88 | 120.34 | 1.86 | 118.49 | 1.84 |
| 161 | $\begin{array}{lll}0 & 1 & 7.84\end{array}$ | 1.71 | 16.14 | 1.69 | 14.47 | 1.67 | 12.81 | 1.65 | 11.17 | 1.62 |
| 162 | 00051.81 | 1.49 | 050.33 | 1.47 | 048.87 | 1.45 | 047.43 | 1.43 | 0 46.01 | 1.41 |
| 163 | $0 \quad 037.94$ | 1.28 | 036.68 | 1.26 | 035.43 | 1.23 | 034.21 | 1.21 | 033.00 | 1.19 |
| 164 | $\begin{array}{lll}0 & 0 & 26.24\end{array}$ | 1.06 | 0 2.5. 19 | 1.04 | 021.16 | 1.02 | 023.16 | 1.00 | 022.17 | 0.97 |
| 16.5 | 0 0 0 16.72 | 0.84 | 015.89 | 0.82 | 0 15.08 | 0.80 | 0 14,29 | 0.78 | 0 113.5.3 | 0.76 |
| 166 | $\begin{array}{llll}0 & 0 & 3.39\end{array}$ | 0.62 | 08.77 | 0.60 | $\begin{array}{ll}0 & 8.18\end{array}$ | 0.58 | 0 7.61 | 0.56 | $0 \quad 7.07$ | 0.54 |
| 167 | $\begin{array}{lll}0 & 0 & 4.25\end{array}$ | -0.40 | $\begin{array}{lll}0 & 3.86\end{array}$ | -0.38 | $\begin{array}{lll}0 & 3.49\end{array}$ | -0.36 | $0 \quad 3.14$ | -0.34 | $0 \quad 2.81$ | $-0.32$ |

EQUATION OF THE: CENTRE, FOR $\mathbf{m}=0$.


| Arg. 1. | $0 . \pi$ | $\left\|\begin{array}{c} \text { Difl: } \\ \text { for }(1) d i \end{array}\right\|$ | ${ }_{0.6}^{d i}$ | $\begin{aligned} & \text { Ditl: } \\ & \text { (wor }()^{d} .1 \end{aligned}$ | $0.7$ | $\begin{gathered} \text { Ditl: } \\ \operatorname{Tor} 00^{d} .1 \end{gathered}$ | ${ }_{0}^{11}$ | Diff: $\text { for }{ }^{1} .1$ | $0.9$ | $\left\lvert\, \begin{aligned} & \text { Uilf: } \\ & \text { fior } 0.1 \end{aligned}\right.$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 112 | © 110.51 .79 | -7.03 | 46: $4: 3.96$ | $\overbrace{-1.80}$ | Ati $33^{\prime \prime} 14$ | -7.83 |  | ${ }_{-7,83}^{1 / 8}$ | 41520.49 | -11.83 |
| 11:1 | 04.5353 .54 | 7.82 | 4.5 35.72 | 7,*3 | 4.517 .90 | 7.52 | 4.5 10.07 | 7.82 | 4.52 .23 | 7.82 |
| 111 | 041 15.35 | \%. 51 | 418.51 | 7.41 | 4:1 50, 273 | 7.51 | di 13.71 .58 | 7.81 | 4 43 44.11 | 7.81 |
| 11.5 | 04252.10 | 7.80 | 4.2.19.50 | 7.75 | d: 41.71 | 7.79 |  | 7.79 | 4282.13 | 7.79 |
| 116 | 04139.4 3 | 7.77 | 41 31.6it | 7.77 | 41 2:3.89 | 7.\%\% | 4116.12 | 2.77 | $41 \quad 8.35$ | 7.86 |
| 117 | 04021.81 | \%.\%5 | 40 11.0\%; | 7.74 | 40 (i.:3) | 7., 1 | 3.158 .15 | 7.i1 | \% 3 \% 6.24 | 7.91 |
| 118 | 0:198 4.80 | \%.71 | 33 3151.78 | 7.71 | 3849.08 | 7.71 | 13 11.37 | \%.70 | 3.431 .67 | 7.70 |
| 119 | 03747.55 | 7.67 | 37 339.87 | \%.67 | 3783.21 | 7.67 | $37 \% 1.51$ | 7.66 | 37 14.स्य3 | \%.\% |
| 120 | 03631.02 | 7.6 | 33: 23.39 | 7.62 | 361.5.77 | 7.63 | 3i; 8.15 | 8.61 | 3i; 0.51 | 7.61 |
| 121 | 0 (1.5) 14.98 | 7.38 | (3) 7.40 | 7.57 | 31.50 .80 | 7.57 | 3150.27 | 7.56 | :31 48.71 | isaj |
| $1 \because 2$ | 0 0333 59.47 | \%22 | 23] $51.9 \%$ | 7.51 | :33 41.41 | 7.51 | [53 315.914 | \%..n) | :3:1 2: 3 ! 1 | (30) |
| 123 | $0: 3241.57$ | 7.16 | 3: 37.11 | 7.4 | 32.20 .67 | 7.15 | 32 22.2 | 7.11 | 3214.75 | 7.13 |
| 124 | 03130.32 | 7.39 | 3120.94 | 7.38 | 3115.56 | 7.38 | 318.18 | 7.35 | $31 \quad 0.8$ ? | 7.36 |
| 12.5 | 03016.79 | ¢.32 | 30 ! 1.47 | 7.31 | :30 2.17 | 7.30 | 24) 34.87 | 7.29 | 20) 47.58 | 7.28 |
| 129 | 0 029 4.03 | 7.24 | 2856.78 | 7.23 | 28.19 .56 | 7.22 | 28 42.31 | 7.2] | 28 35. 11 | 7.20 |
| 127 | 0275207 | 7.15 | 2744.92 | 7.14 | 2737.79 | 7.13 | 2730.16 | 7.13 | 2723.51 | 7.12 |
| 123 | 02641.01 | 7.00 | 26333.95 | 7.05 | 26.26 .91 | 7.04 | 26 19.87 | 7.03 | 2 2 12.81 | 7.02 |
| 12, | 02.530 .88 | 6.96 | 2.) 23.45 | 6.93 | 2.) 16.07 | 6.94 | 2.) 10.03 | 6.93 | 2.) 3.10 | 6.92 |
| 1:30 | 02421.73 | 6.86 | 2114.88 | 6.85 | 218.003 | 6.88 | 24 1.19) | 0.83 | 2354.37 | 6.02 |
| 131 | 02313.63 | 6.76 | 236.83 | 6.75 | 2300.14 | 6.73 | 22.53 .41 | 6.72 | 2246 | 6.71 |
| 132 | 0926.62 | 6.64 | 2159.99 | 6.63 | 21.53 .36 | 6.62 | 21 46.74 | 0.61 | 2140.14 | 6.m9 |
| 1:33 | 0210.76 | 6.53 | 2051.24 | 6.51 | 2047.73 | 6.50 | 2041.24 | 6.49 | 20 :41.75 | 6.13 |
| 1:34 | 01956.10 | 6.10 | 19 4!.70 | 6.39 | 1943.31 | 6.38 | 19336.91 | 6.37 | 1!9:30.58 | 6.35 |
| 135 | 01852.68 | 6.28 | 1846.40 | 6.97 | 1840.14 | 6.25 | 1833.90 | 6.24 | 1827.17 | 6.23 |
| 136 | 01750.55 | 6.15 | 1744.41 | 6.13 | 1738.28 | 6.12 | 1732.17 | 0.11 | 1726.07 | 6.09 |
| 137 | 01649.78 | 6.01 | 1643.77 | 5.99 | 1637.78 | 5.98 | 1631.80 | 5.97 | 11685.81 | 5.93 |
| 1:38 | 0 1.5 50.38 | 5.57 | 1.) 41.5 | 5.85 | 1533.67 | 5.84 | $15: 32.84$ | 5.82 | 15) 27.02 | 5.81 |
| 139 | 01452.42 | 5.72 | 1446.81 | 5.71 | 1441.01 | 5.69 | 1435.32 | 5.68 | 1429.65 | 5.66 |
| 140 | 01355.95 | 5.57 | 1350.38 | 5.56 | 1344.84 | 5.54 | 1339.30 | 5,33 | 1333.78 | $55^{10}$ |
| 141 | 0131.00 | 5.42 | 1255.59 | 5.40 | 1250.20 | 5.38 | 1244.82 | 5.37 | 12 31.4i; | 5.3 |
| 142 | 012 \%.th | 5.26 | 12.2 .38 | 5.24 | 1157.14 | 5.23 | 11.51 .92 | 5.21 | 1146.72 | 5.19 |
| 143 | 01115.86 | 5.09 | 1110.77 | 5.08 | $11 \quad 5.70$ | 5.06 | 110.65 | 3.04 | 10 5. 5.61 | 5.03 |
| 144 | 01025.74 | 4.93 | 1020.82 | 4.91 | 1015.92 | 4.89 | 1011.04 | 4.88 | $10 \quad 6.17$ | 4.88 |
| 14.5 | $0 \quad 937.32$ | 4.76 | 938.57 | 4.74 | (1) 27.84 | 4.72 | 923.12 | 4.70 | 918.43 | 4.69 |
| 146 | $0 \quad 850.62$ | 4.38 | 8 4(i.05 | 4.56 | 841.49 | 4.35 | 836.96 | 4.53 | 833.44 | 4.35 |
| 147 | $\begin{array}{lllll}0 & 8 & 5.69\end{array}$ | 4.40 | 81.30 | 4.30 | 756.92 | 4.37 | 752.56 | 4.35 | 743.22 | 4.33 |
| 148 | 0 \% 22.56 | 4.22 | 718.35 | 4.20 | \% 14.16 | 4.18 | 70.98 | 4.17 | 75.83 | 4.15 |
| 149 | $\begin{array}{llll}0 & 6 & 41.27\end{array}$ | 4.01 | 6 37.25) | 4.02 | (i) 3:3.24 | 4.00 | (6) 23.2 .5 | 93 | 625.28 | 2.36 |
| 1.50 | $\begin{array}{llll}0 & 6 & 1.85\end{array}$ | 3.95 | 558.01 | 3.83 | 554.20 | 3.81 | 550.40 | 3.79 | 5 46,61 | 3.71 |
| 151 | $\begin{array}{llll}0 & 5 & 24.33\end{array}$ | 3.66 | 520.68 | 3.64 | 517.06 | 3.62 | 513.45 | 3.60 | 59.86 | 3 m 5 |
| 159 | $\begin{array}{llll}0 & 4 & 48.74\end{array}$ | 3.48 | 44.3 .29 | 3.41 | 441.85 | 3.42 |  | 3.40 |  | 3.35 3.18 |
| 103 | 0 O 415.11 | 3.26 | 411.85 | 3.21 | 48.82 | 3.22 | 4.5 .41 | 3.20 3.00 | $4{ }^{4} 2.21$ | 3.18 2.98 |
| 155 | $\begin{array}{llllll}0 & 3 & 13.83\end{array}$ | 2.88 | 310.98 | 2.84 | 38.15 | 2.82 |  | 2.80 |  |  |
| 1.6 | $0 \quad 246.21$ | 2.66 | 243.59 | 2.64 | 240.97 | 2.62 | 238.36 | 2.59 | 23.35 .78 | 2.57 |
| 158 | 0 2 20.70 | 2.45 | 218.26 | 2.43 | 215.81 | 2.41 | 2136.45 | 239 | 211.07 | 2.37 |
| 1.8 | 0 0 157.25 | 2.24 | 15.5 .02 | 2.22 | 1528 | 2.20 | 150.62 | 2.18 | 148.45 | 2.16 |
| 159 | 0 1 3 <br> S.   | 2.03 | 133.88 | 2.01 | 131.88 | 1.93 | 129.90 | 1.97 | 127.95 | 1.94 |
| 160 | 0 1116.66 | 1.83 | 114.8 .5 | 1.80 | 113.07 | 1.77 | 111.30 | 1.75 | 19.56 | 1.73 |
| 161 | $0 \quad 0 \quad 59.56$ | 1.60 | 057.97 | 1.58 | 055.40 | 1.56 | 054.85 | 1.51 | 053.32 | 1.52 |
| 162 | 0 0 0 44.61 | 1.39 | 0 4.3.23 | 1.37 | 041.88 | 1.34 | 040.51 | 1.22 | 0 3.9.23 | 1,30 |
| 163 | $\begin{array}{llll}0 & 0 & 31.82\end{array}$ | 1.17 | 030.66 | 1.15 | 029.53 | 1.13 | 023.41 | 1.10 | 027.32 | 1.03 |
| 164 | $\begin{array}{llll}0 & 0 & 21.21\end{array}$ | 0.95 | 020.97 | 0.93 | 0 19.3.5 | 0.91 | 018.45 | $0 . .9$ | 017.57 | 0.26 |
| 1(\%) | $0 \begin{array}{lllll}0 & 0 & 19.78\end{array}$ | 0.33 | 0 12.06 | 7 | 011.36 | 09 | 0 10.ç | 0.67 | 010.03 | 0.\% |
| 166 | 0 0 0 6.51 | 0.51 | $0 \quad 6.04$ | . 43 | 05.51 | . 47 | $0 \quad 5.10$ | 0.45 | 0 4.63 | 0.43 |
| 167 | $\begin{array}{llll}0 & 0 & 2.51\end{array}$ | -0.29 | 0 2.8. | -0.97 | 0 1.9\% | -0.25 | $\begin{array}{lll}0 & 1.7 \%\end{array}$ | -0.23 | $0 \quad 1.51$ | -0.91 |

EQUATION OF TUE CENTRE, FOR $\mathbf{m}=0$.
Constant added $47^{\prime} 33^{\prime \prime} .5$. Period $=924.7008$.

| Arg. I | ${ }^{d}$ | $\left\lvert\, \begin{gathered} \mathrm{B}_{\mathrm{iff}} \\ \text { for }(0 \mathrm{~d} .1 \end{gathered}\right.$ | ${ }_{0}^{\mathrm{d}} .1$ | $\left\|\begin{array}{c} \text { Diti: } \\ \text { for } 0 \text { d } .1 \end{array}\right\|$ |  | $\left\lvert\, \begin{gathered} \text { Ditl: } \\ \text { for } 00^{d} .1 \end{gathered}\right.$ | $0.13$ | $\begin{gathered} \text { Diff. } \\ \text { for } \mathrm{Cd} .1 \end{gathered}$ | $\begin{gathered} \mathrm{d} \\ 0.4 \end{gathered}$ | $\begin{gathered} \text { Diff: } \\ \text { for } 0 \mathrm{~d} .1 \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 168 | 80 | -0.18 | $0 \quad 1.14$ | -0.16 | $0 \quad 0.99$ | -0.14 | $0 \begin{array}{ll}0 & 0.86\end{array}$ | -0.12 | $\begin{array}{ll}0 & 0.16\end{array}$ | -0.10 |
| 169 | $\begin{array}{llll}0 & 0 & 0.58\end{array}$ | +0.04 | 0 0.63) | +0.06 | $0 \quad 0.70$ | +0.08 | 00.79 | +0.10 | $\begin{array}{lll}0 & 0.91\end{array}$ | $+0.13$ |
| 170 | 0 0 0 O 2.06 | 0.26 | $0 \quad 2.33$ | 0.28 | $0 \quad 2.62$ | 0.30 | 0 | 0.32 | $\begin{array}{ll}0 & 3.27\end{array}$ | 0.35 |
| 171 | $\begin{array}{llll}0 & 0 & 5.74\end{array}$ | 0.48 | 0 (6.23 | 0.50 | $0 \quad 6.75$ | 0.55 | 07.28 | 0.54 | 0 7.84 | 0.57 |
| 172 | $\begin{array}{lllll}0 & 0 & 11.64\end{array}$ | 0.70 | 012.35 | 0.72 | 013.08 | 0.74 | 013.83 | 0.76 | 014.61 | 0.79 |
| 17\% | 00019.73 | 0.92 | 020.66 | 0.94 | 021.61 | 0.96 | 022.59 | 0.98 | 023.58 | 1.0 |
| 174 | $\begin{array}{llll}0 & 0 & 30.02\end{array}$ | 1.14 | 0 031.17 | 1.16 | 032.34 | 1.18 | 0 333.51 | 1.20 | 0 31.75 | 1.22 |
| 17.5 | $\begin{array}{llll}0 & 0 & 42.51\end{array}$ | 1.36 | 043.88 | 1.38 | 045.27 | 1.40 | 046.68 | 1.42 | 048.11 | 1.44 |
| 176 | 057.18 | 1.58 | 058.76 | 1.60 | 1. 0.37 | 1.63 | $0 \quad 2.00$ | 1.64 | $\begin{array}{ll}0 & 3.65\end{array}$ | 1.66 |
| 177 | 0 0 1 14.03 | 1.79 | 115.82 | 1.81 | 117.65 | 1.44 | 119.50 | 1.66 | ] 21.36 | 1.88 |
| 178 | $\begin{array}{llll}0 & 1 & 33.03\end{array}$ | 2.01 | 1 135.04 | 2.03 | 137.08 | 2.05 | 139.15 | 2.07 | 141.23 | 2.99 |
| 179 | $\begin{array}{llll}0 & 1 & 54.18\end{array}$ | 2.28 | 156.41 | 2,24 | 158.67 | 2.26 | 20.94 | 2.29 | 23.24 | 2.31 |
| 180 | $0 \quad 217.47$ | . 43 | 219.91 | 2.46 | 229.38 | 2.48 | 224.87 | 2.50 | 227.38 | 2.53 |
| 181 | $0 \quad 242.87$ | 2.65 | 2 45.53 | 2.67 | 248.20 | 2.69 | 250.90 | 2.71 | 253.62 | 2.73 |
| 182 | $0 \quad 310.37$ | 2.8 | 313.24 | 2.87 | 316.12 | 2.90 | 3 19.03 | 2.92 | 321.96 | 2.94 |
| 183 | $\begin{array}{llll}0 & 3 & 39.95\end{array}$ | 3.06 | 343.02 | 3.08 | 346.12 | 3.10 | 349.23 | 3.12 | 352.36 | 3.14 |
| 184 | $\begin{array}{llll}0 & 4 & 11.59\end{array}$ | 3.27 | 414.87 | 3.29 | 418.16 | 3.31 | 421.48 | 3.33 | 424.82 | 3.35 |
| 185 | 44.26 | 3.47 | 448.74 | 3.49 | 452.23 | 3.51 | 455.75 | 3.53 | 4 5!.99 | 3.55 |
| 186 | $\begin{array}{llll}0 & 5 & 20.93\end{array}$ | 3.67 | 524.61 | 3.69 | 528.31 | 3.71 | 532.04 | 3.73 | 533.76 | 3.75 |
| 187 | 558.59 | 3.86 | 62.46 | 3.88 | $6 \quad 6.36$ | 3.90 | 610.27 | 3.92 | 614.20 | 3.94 |
| 188 | $0 \quad 638.20$ | 4.06 | 642.26 | 4.08 | 646.35 | 4.10 | 650.46 | 4.11 | 654.58 | 4.13 |
| 189 | 07819.73 | 4.25 | 723.98 | 4.27 | 728.26 | 4.28 | 732.55 | 4.30 | 736.87 | 4.32 |
| 190 | 0883.14 | 4.43 | $8 \quad 7.59$ | 4.45 | 813.05 | 4.47 | 816.53. | 4.49 | 821.03 | 4.51 |
| 191 | $\begin{array}{llll}0 & 8 & 48.42\end{array}$ | 4.62 | 853.05 | 4.6.1 | 857.69 | 4.65 | 92.36 | 4.67. | 97.04 | 4.69 |
| 192 | 0 9 3 | 4.50 | 940.32 | 4.82 | 945.15 | 4.83 | 949.99 | 4.85 | 954.85 | 4.87 |
| 103 | 01024.40 | 4.98 | 1029.38 | 4.99 | 10 34.38 | 5.01 | 1033.40 | 5.03 | 1044.4 .1 | 5.04 |
| $1: 4$ | 01115.02 | 5.13 | 1120.18 | 5.17 | 1125.35 | 5.18 | 1130.55 | 5.20 | 11 35.75 | 5.22 |
| $19 \%$ | 0127.36 | 5.32 | 1212.68 | 5.33 | 1218.03 | 5.35 | 1223.39 | 5.37 | 1228.76 | 5.38 |
| 196 | $\begin{array}{lll}0 & 13 \\ 1.36\end{array}$ | 5.48 | 136.85 | 5.50 | 1312.36 | 5.51 | 1317.88 | 5.53 | 1323.42 | 5.55 |
| 197 | 013856.99 | 5.64 | 14.2 .64 | 5.66 | 14.8 .31 | 5.68 | 1413.99 | 5.6 | 1419.69 | 5.7 |
| 198 | 01451.20 | 5.80 | 150.01 | 5.81 | 1.) $5: 83$ | 5.83 | 1511.67 | 5.84 | 1517.52 | 5.86 |
| 199 | 01552.95 | 5.95 | 1558.91 | 5.96 | 164.88 | 5.97 | 1610.87 | 5.99 | 1616.87 | 6.01 |
| 200 | 01653.19 | 6.10 | 1659.29 | 6.1 | $17 \quad 5.41$ | 6.13 | 1711.54 | 6.14 | 17 17.69 | 6.15 |
| 201 | 01754.87 | 6.24 | $18 \quad 1.12$ | 6.25 | 187.38 | 6.27 | 18 13.6.5 | 6.23 | 1819.94 | 6.29 |
| 202 | 01857.95 | 6.38 | 19 4.33) | 39 | 1910.72 | 6.40 | 1917.13 | 6.42 | 1923.56 | 6.43 |
| 203 | $\begin{array}{lll}0 & 20 & 2.37\end{array}$ | 6.51 | 208.88 | 6.52 | 2015.41 | 6.53 | 2021.95 | 6.55 | 2028.50 | 6.56 |
| 204 | 0218.09 | 6.63 | 2114.73 | 6.65 | 2121.38 | 6.66 | 21 28.05 | 6.67 | 2134.72 | 6.68 |
| 20.5 | 02215.04 | 6.76 | 2221.81 | 6.77 | 2228.58 | 6.78 | 2235.37 | 6.79 | 2242.16 | 6.80 |
| 206 | 02323.19 | 6.87 | 2330.07 | 6.88 | 23.36 .96 | 6.89 | 2343.86 | 6.91 | 2350.77 | 6.92 |
| 207 | 02432.48 | 6.98 | 2439.47 | 6.99 | 2446.46 | 7.00 | 2453.47 | 7.03 | $25 \quad 0.50$ | 7.03 |
| 208 | 0 25. 42.84 | 7.09 | 2.549 .93 | 7.10 | 25.57 .01 | 7.11 | 26.4 .15 | 7.12 | 2611.28 | 7.13 |
| 209 | 02654.23 | 7.19 | $27 \quad 1.42$ | 7.20 | 278.62 | 7.21 | 2715.84 | $7 . .29$ | 2723.06 | 7.23 |
| 210 | 0286.59 | 7.28 | 2813.87 | 7.29 | 2821.17 | 7.30 | 2828.47 | 7.31 | 28 35.79 | 7.39 |
| 211 | 02919.85 | 7.37 | 2927.23 | 7.38 | 2934.61 | 7.39 | 29 42.00 | 7.40 | 2) 49.40 | 7.40 |
| 212 | 03033.97 | 7.45 | 3041.43 | 7.46 | 3048.89 | 7.47 | 30.50 .36 | 7.48 | 313.84 | 7.48 |
| 213 | 03148.88 | 7.53 | 3156.41 | 7.54 | 32 3.95 | 7.54 | 3211.50 | $7 . .55$ | 3219.05 | 7.56 |
| 214 | 0334.92 | 7.60 | 3312.13 | 7.61 | 3319.74 | 7.61 | 33:3 27.35 | 7.62 | 3:3 34.97 | 7.63 |
| 215 | 03420.84 | 7.66 | 3428.51 | 7.67 | 3436.18 | 7.67 | 3443.86 | 7.68 | 3451.54 | 7.69 |
| 216 | 03.537 .77 | 7.72 | 3.545 .49 | 7.73 | 3553.22 | 7.73 | 36 | 7.74 | 36 8.f9 | 7.74 |
| 217 | 03655.24 | 7.77 | 3783.02 | 7.78 | 3710.80 | 7.78 | 3718.58 | 7.79 | 3726.37 | 7.79 |
| 218 | 03813121 | 7.82 | :38 21.03 | 7.82 | 38 28,85 | 7.83 | 38319.68 | 7.83 | 3844.51 | 7.83 |
| 219 | 03931.60 | 7.86 | 3939.46 | 7.86 | 3947.32 | 7.87 | 3) 55.19 | 7.87 | $40 \quad 3.06$ | 7.87 |
| 220 | 04050.35 | 7.89 | 4058.24 | 7.89 | 416.13 | 7.90 | 4114.03 | 7.90 | 4121.03 | 7.90 |
| 221 | 04.39 .40 | 7.92 | 4217.39 | 7.92 | 42.2 .24 | 7.92 | 4233.16 | 7.9 | 4241.09 | 7.93 |
| 22. | 0 4:3 28.68 | 7.94 | 43 37,62 | 7.94 | 4:3 44.56 | 7.94 | 4.352 .51 | 7.94 | $44 \quad 0.45$ | 7.94 |
| 92:3 | 04.148 .14 | \%.95 | 445 s .10 | 7.95 | 454.05 | 7.95 | 4.512 .00 | 7.96 | 4519.96 | 7.96 |
| 521 | 0467.71 | +7.96 | $46 \quad 15.67$ | +7.96 | 4623.63 | +7.86 | $46: 31.59$ | +7.96 | 4639.55 | +7.96 |


| EQUATION OF THE CENTRE, FOR $m=0$. Constant added 4it' $3^{n}$.5. Period $=$ 2.21.70) |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Arg | 0.5 | fir | $0_{0}^{1.6}$ | $\left.\right\|_{\operatorname{ting}} ^{\operatorname{ting}}$ | 0.7 |  | 0.8 | ${ }_{n i l}^{n}$ | d. ${ }^{\text {d }}$ | init |
| $\begin{aligned} & 118 \\ & 168 \\ & 1601 \\ & 1701 \end{aligned}$ |  |  | $\begin{aligned} & 0 \\ & 0 \end{aligned}$ |  |  |  |  | $\begin{gathered} -0.01010 \\ 0.0 .018 \\ 0.10 .0 .0 \\ 0.0 .0 \end{gathered}$ |  | $\begin{aligned} & \text { tuot } \\ & 0.01 \\ & 0.46 \\ & 0.04 \\ & 0.64 \end{aligned}$ |
|  |  |  |  |  |  |  |  |  |  | $\begin{aligned} & 0.00 \\ & 1.12 \\ & 1.34 \\ & 1.55 \end{aligned}$ |
| $\begin{aligned} & 176 \\ & 172 \\ & 172, \\ & 172, \end{aligned}$ |  |  | $\frac{1}{2} \frac{15.46}{7.150}$ |  |  |  |  |  |  | , |
| $\begin{aligned} & 180 \\ & 181 \\ & 182 \\ & 183 \\ & 183 \end{aligned}$ |  | $\begin{aligned} & 2.54 \\ & 2.75 \\ & 2.96 \\ & 3.16 \end{aligned}$ |  |  |  | $\begin{aligned} & 2.58 \\ & 2.79 \\ & 3.00 \\ & 3.20 \end{aligned}$ |  |  |  | , |
| $\begin{aligned} & 181 \\ & \hline 185 \\ & \hline 185 \\ & 187 \\ & 187 \end{aligned}$ |  |  |  |  |  | $\begin{aligned} & 3.11 \\ & \text { a.10 } \\ & 2.010 \\ & 4.00 \end{aligned}$ |  | $\begin{aligned} & 3,1 \times 3 \\ & \text { and } \\ & \text { and } \\ & 4020 \end{aligned}$ |  | cos |
| $\begin{aligned} & 183 \\ & 189 \\ & 190 \\ & 1901 \end{aligned}$ |  | $\begin{gathered} 4.15 \\ \text { and } \\ 4.00 \\ 4, i=1 \end{gathered}$ | 8 <br> 8 <br> 8 <br> 810.099 <br> 10.46 |  | $\begin{aligned} & 743.921 \\ & 8.4 .1 .1 \\ & 921.20 \end{aligned}$ | $\begin{aligned} & 4.10 \\ & 4.48 \\ & 4.85 \\ & 4.75 \\ & 4.76 \end{aligned}$ |  | $\begin{gathered} 4.90 \\ .4010 \\ 4.450 \\ 4.6 \end{gathered}$ |  | cose |
|  | $\begin{aligned} & 0 \\ & 0 \end{aligned}$ |  |  |  |  |  |  |  |  | cosis |
| $\begin{aligned} & 196 \\ & 197 \\ & 197 \\ & 1959 \\ & 199 \end{aligned}$ | $\begin{aligned} & 0.132 .298 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned} 1$ | $\begin{aligned} & 5.56 \\ & 5.72 \\ & 5.88 \\ & 6.02 \end{aligned}$ |  | $\begin{gathered} 5.58 \\ 5.87 \\ 5.9 .9 \\ 0.94 \\ \hline \end{gathered}$ |  |  |  |  |  | (tich |
| $\begin{aligned} & 200 \\ & \begin{array}{l} 201 \\ 201 \\ 2020 \end{array} \\ & \hline 203 \end{aligned}$ |  02035.02 | $\begin{aligned} & 6.17 \\ & .6 .12 \\ & .6 .41 \\ & 0.57 \end{aligned}$ |  | $\begin{aligned} & 8.18 \\ & 0.81 \\ & 0.018 \\ & 0.58 \end{aligned}$ |  |  | $\begin{aligned} & 18.4 .98 \\ & 19.9 .38 \\ & 20.51 .84 \end{aligned}$ | $\begin{gathered} 6.21 \\ 0.2021 \\ 6.618 \\ 6.01 \end{gathered}$ |  | (e.en |
| $\begin{aligned} & 201 \\ & 2005 \\ & 2006 \\ & 2007 \end{aligned}$ |  |  |  |  | $2411.57$ |  |  |  |  | , |
| $\begin{aligned} & 200 \\ & 2001 \\ & 2090 \\ & 290 \\ & 211 \end{aligned}$ |  |  |  | $\begin{gathered} 7,1.51 \\ 7,-9.4 \\ 7,-12 \end{gathered}$ |  |  |  | $\begin{aligned} & 7.17 \\ & 7.26 \\ & 7.35 \\ & 7.41 \end{aligned}$ |  |  |
| $\begin{aligned} & 219 \\ & 213 \\ & 213 \\ & 214 \end{aligned}$ |  |  |  |  |  |  |  | $\begin{aligned} & 7.51 \\ & 7.59 \\ & 7.65 \\ & 7.71 \end{aligned}$ |  |  |
| $\begin{aligned} & 216 \\ & 217 \\ & 218 \\ & 2189 \end{aligned}$ |  |  | $\begin{aligned} & 3621.19 \\ & 374.19 \\ & 39.19 .19 \\ & 4018.81 \end{aligned}$ | $\begin{aligned} & 7.75 \\ & 7.80 \\ & 7.84 \\ & 7.88 \end{aligned}$ |  |  |  | $\begin{aligned} & 7.76 \\ & 7, .61 \\ & 7.48 .48 \\ & 7.88 \end{aligned}$ |  |  |
|  |  |  |  |  |  |  |  |  |  |  |


| Factor to be multiplied by the integer man ; and its Logarithm. |  |  |  |  |  |  |  |  |  |  |  | Pcrt. of the Long. <br> Fact. to be $\times\left(\frac{\mathrm{BII}}{1 \mathrm{NiO}}\right)^{2}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Arg. 1. | liator. | Log. Fac. | Arg. 1. | Pactor. | Log. Tac | Arg. 1. | Factor. | griac | Arg. 1 | Factor. | Log. Pax. | Arg. 1. | Fact. | L. Fac. |
| $\stackrel{1}{1}$ | 0.0 no |  | (i) | -12.596 | $n 1.100$ | 120 | 2.649 | 0.4231 | 180 | +12.109 | 1.0831 | $0_{0}^{d}$ | +0.0n | $\infty$ |
| 1 | 0.361 | 9.5.575 | 61 | 12.547 | 1.098 | 121 | 2.990 | 0.47 .37 | 181 | 11.996 | 1.0790 | 4 | 0.22 | 9.343 |
| 2 | 0.721 | !1.8.3) | 63 | 12.488 | 1.0965 | 12. | 3.328 | 0.502 | $1 \pm 2$ | 11.875 | 1.0746 | 8 | 0.14 | 9.648 |
| 3 | 1.051 | 0.0335 | 63 | 12.4:1 | 1.0942 | 123 | 3.663 | 0.5638 | 133 | 11.744 | 1.069 | 12 | 0.66 | 9.820 |
| 4 | -1.411 | $n 0.15$ | 64 | -12:343 | $n 1.09$ | 124 | $+3.997$ | 0.6017 | 184 | +11.604 | 1.106 | 16 | $+9.87$ | 9.933 |
| 5 | 1.799 | 0.25, | 6.3 | 12.256 | $1.0<83$ | 125 | 4.326 | 0.6361 | 150 | 11.404 | 1.0590 | 29 | 1.06 | $0.12: 27$ |
| ${ }_{6}$ | 9.155 | 0.33331 | 66 | 12.159 | 1.084! | 126 | 4.65 | 0.6676 | 186 | 11.2:5 | 1.0529 | 21 | 1:2 | 0.096 |
| \% | 2.509 | 0.3995 | 67 | 12.053 | 1.0511 | 127 | 4.976 | $0.6016{ }^{3}$ | 187 | 11.124 | 1.0464 | 23 | 1.42 | 0.151 |
|  | 2.962 | $n 0.4567$ | 6.9 | -11.938 | $n 1.0763$ | 123 | + 5.29 | 0.7239 | 188 | +10.952 | 1.0395 | 32 | +1.56 | 0.1911 |
| 9 | 3.212 | 0.5063 | 6: | 11.813 | 1.0724 | 129) | 5.511 | 0.7400 | 189 | 10.266 | 1.10321 | 36 | 1.69 | 0.2!? |
| 11 | 3.563 | 0.5014 | 70 | 11.(i3) | 1.0674 | 1:30 | 5.122 | 0.729.5 | 193 | 10.571 | 1.12:41 | 40 | 1.80 | 0.256 |
| 11 | 3.904 | 0.5915 | 71 | 11.536 | 1.0631 | 131 | 6.233 | 0.7945 | 191 | 10.369 | 1.0157 | 44 | 1.8!) | 0.2\%\% |
| 12 | 4.246 | n? 6239 | 72 | -11.385 | $n 1.0 .763$ | 132 | $+6.532$ | 0.8150 | 122 | +10.158 | 1.0063 | 43 | +1.95 | 0.991 |
| $1: 1$ | $4.5 \times 4$ | 0.6612 | 73 | 11.226 | 1,050\% | $13: 3$ | 6.589 | 0.834 1 | $1!3$ | 9.939 | 0.91973 | 59 | 1.99 | 0.299 |
| 14 | 4.915 | 0.6918 | 74 | 11.0.56 | 1.0436 | 131 | 7.121 | 0.85\% | 1:14 | 9.712 | 0.9573 | 56 | 2.91 | 0.302 |
| 15 | 5.250 | 0.7202 | 75 | 10.874 | 1.0366 | 13.5 | 7.408 | $0.86^{\circ} 17$ | 195 | 9.478 | 0.9767 | 6 | 1.99 | 0.300 |
| 16 | 5.575 | $n 0.7462$ | 76 | -10.694 | $n 1.02 .91$ | 136 | + 7.630 | 0.8859 | 196 | + 9.235 | 0.96 .54 | 61 | +1.96 | 0.292 |
| 17 | 5.8196 | 0.7706 | 77 | 10.501 | 1.0212 | 1:37 | 7.116 | 0.9012 | 197 | $8.95{ }^{\text {8 }}$ | 0.953 .5 | 63 | 1.31) | $0.27 \times$ |
| 18 | 6.213 | 0.7933 | 78 | 10.299 | 1.0123 | 133 | 8.295 | 0.9157 | 193 | 8.297 | 0.9400 | 72 | $1 \times 1$ | 0.253 |
| 19 | 6.524. | 0.8145 | 79 | 10.090 | 1.0039 | 139 | 8.498 | 0.9293 | 199 | 8.463 | 0.925 | 76 | 1.71 | (1).2.2: |
| 20 | -6.830 | $n^{n}$ | 8.7 | - 9.873 | $n 0.0944$ | 140 | +8.7.76 | 0.9423 | 200 | +8.191 | 0.91 | 89 | +1.5\% | 0.193 |
| 21 | 7.131 | (1).5.531 | 81 | !1.613 | 0.9844 | 141 | 9.9016 | 0.954 .5 | 201 | 7.914 | 0.8934 | 84 | 1.43 | (1.1河 |
| 22 | 7.42 G | 0.8717 | 89 | 9.417 | 0.97819 | 142 | 9.249 | 0.9661 | 202 | 7.649 | 11.852 | 88 | 1.26 | 0.101 |
| 23 | 7.715 | 0.8573 | 83 | $9.17 \%$ | $0.96 \pm 7$ | 143 | 9.486 | 0.9771 | 203 | 7.338 | 0.8659 | 92 | 1.08 | 0.034 |
| 24 | 7.997 | n11.9029 | 8.1 | 8.932 | $n 9.9509$ | 144 | + 0.716 | $0.98 \%$ | 204 | + 7.042 | 81 | 96 | +0.8 | 947 |
| 95 | 8.273 | 0.9177 | 85 | 8.67!) | $0.938 \%$ | 14.5 | 9.933 | 0.9973 | 20.5 | 6.733 | 0.8286 | 101 | 0.6 | 9.832 |
| 26 | 8.542 | 0.11316 | 86 | 8.191 | 0.925 | 146 | 10.153 | 1.0066 | 206 | 6.431 | 0.81):3 | 104 | 0.46 | 0.667 |
| 97 | 8.805 | 0.9447 | 87 | 8.155 | 0.9114 | 147 | 10.360 | 1.0154 | 207 | 6.118 | 0.7666 | 108 | 0.21 | 9.386 |
| 23 | $-9.060$ | $n 0.9571$ | 88 | 7.883 | $n 0.8967$ | 148 | +10.5.9 | 1.0236 | 203 | $+5.801$ | 0.763 | 112 | +0 | 293 |
| 2!) | $9.300^{\circ}$ | 0.9659 | 89 | 7.6016 | 0.8812 | 149 | 10.7.5) | 1.0314 | 2, 19 | 5.478 | 0.7386 | 116 | -0.43 | $n 9.310$ |
| 30 | 9.548 | 0.9719 | 90 | 7.32:3 | 0.8647 | 150 | 10.933 | 1.0387 | 210 | 5.150 | 0.7118 | 120 | 0.42 | 969 |
| :31 | 9.781 | 0.9904 | 91 | 7.035 | 0.8473 | 151 | 11.108 | 1.0456 | 211 | 4.81!) | 0.6830 | 124 | 0.61 | 9.807 |
| 32 | -10.005 | $n 1.0003$ | 92 | 6.741 | $n 0.8297$ | 152 | +11.274 | 1.0521 | 212 | + 4.484 | 0.6517 | 123 | 0.8 | n9.929 |
| 33 | 10.2\%:3 | 1.0019 | $9: 3$ | 6.412 | 0.8090 | $15: 3$ | 11.432 | 1.0.i31 | 213 | 4.145 | 0.6175 | 132 | 1.n.: | 0.0.) |
| 34 | 10.431 | 1.01×3 | 9. | 6.138 | 0.7883 | 154 | 11.581 | 1.06:37 | 214 | 3.80:2 | 0.5300 | 136 | 1.2: | 0.091 |
| 3.5 | 10.6331 | 1.0266 | 95 | 5.830 | 0.6657 | 155 | 11.721 | 1.0690 | 215 | 3.457 | 0.5357 | 140 | 1.43 | 0.146 |
| 36 | -10.82:3 | n].03.13 | 96 | 5.517 | $n 0.7417$ | 156 | +11.8. 21 | 1.0733 | 216 | $+3.103$ | 0.4920 | 144 | -1.55 | n0.191 |
| 37 | 11.00 .7 | 1.0416 | ! | 5.209 | 0.2160 | 157 | 11.972 | $1.07 \times 2$ | 217 | 2.757 | 0.4404 | 143 |  | 0.29 c |
| 38 | 11.179 | 1.0454 | 98 | 4.579 | 0.6388 | 158 | 12.045 | 1.0822 | 218 | 2.404 | 0.3309 | 152 | 1.80 | 10.2. 1 |
| 39 | 11.344 | 1.0518 | 99 | 4.555 | 0.6585 | 159 | 12.18:) | 1.0560 | 14 | 2.049 | 0.3115 | 156 | 1.89 | 0.275 |
| 40 | -11.500 | $n 1.0607$ | 100 | 4.297 | $n 0.6260$ | 169 | +12.283 | 1.0893 | $2: 0$ | + $1.6!1$ | 0.9231 | 160 | 1.9 | 2.200 |
| 41 | 11.647 | 1.0662 | 101 | 3.8917 | 0.5907 | 161 | 12.367 | 1.0123 | 221 | 1.3333 | 0.1243 | 161 | 1.99 | 0.299 |
| 42 | 11.784 | - 1.0713 | 102 | 3.563 | 0.5518 | 162 | 12.44 | 1.0549 | 222 | 0.174 | 0.9836 | 168 | 2.01 | 1).30\% |
| 43 | 11.913 | 1.0760 | $10: 3$ | 3.527 | 0.5088 | 163 | 12.507 | 1.0972 | 2 3 | 0.613 | 9.8875 | 372 | 2.00 | 0.300 |
| 44 | -12.131 | $n 1.0893$ | 104 | - 2.888 | ${ }^{0} 0.4696$ | 164 | +12.563 | 1.0991 | 9, | +0.2.33 | p!.4031 | 176 | 1. | 00.293 |
| 45 | 12.140 | 1.084\% | 10.5 | 2.547 | 0.4060 | 165 | 19.609 | 1.1007 | 22 | 0.1118 | n0.0334 | 180 | 1.90 | 0.230 |
| 46 | 12.23! | 1.0-2\% | 109 | 2.20 .5 | 0.3434 | 166 | 12.615 | 1.1019 | 246 | 0.469 | 9.6712 | 1-1 | 1.82 | 0.293 |
| 47 | 12.329 | 1.090 | 107 | . 863 | 0.2695 | 167 | 12.671 | 1.1023 | 427 | 0.829 | $9.918{ }^{\circ}$ | 183 | 1.22 | 0.2.34 |
| 48 | -12.418 | $n 1.0037$ | 108 | $-1.514$ | $n 0.1801$ | 168 | +19.687 | 1.1034 | 293 | - 1.189 | $n 0.07 .52$ | 192 | -1.59 | n0.201 |
| 49 | 12.479 | 1.0369 | 119 | 1.167 | 0.0671 | 169 | 12.6933 | 1.11336 | 92:) | 1.518 | 0.1898 | 196 | 1.14 | 0.159 |
| 50 | 12.510 | 1.093:3 | 110 | 0.81!) | 0.12133 | 170 | 12.60 | 1.1035 | 2:30 | 1.906 | 0.2301 | 900 | 1.28 | 0.106 |
| 51 | 12.590 | J.1000 | 111 | 0.471 | 9.6830 | \%1 | 12.676 | 1.1030 | 231 | 2.262 | 0.3545 | 204 | 1.10 | 0.049 |
| 52 | -12.630 | $n 1.1011$ | 119 | -0.122 | $n 9.086 .1$ | 172 | +12.6.53 | 1.1092 | 292 | - 2.615 | $u^{0} 0.41 \%$ | 208 | , | n.9.956 |
| 53 | 12.660 | 1.1024 | 113 | $+0.227$ | $p$ 9.3560 | 173 | 12.619 | 1.1010 | $3: 3$ | 2.968 | 0.4723 | 214 | 0.70 | 9.843 |
| 54 | 12.631 | 1.10:32 | 114 | 0.575 | 9.7597 | 174 | 12.576 | 1.090 .5 | 294 | 3.317 | 0.5207 | 216 | 0.15 | 9 ), |
| 55 | 12.602 | 1.1035 | 115 | 0.9223 | 0.196 | 17\% | 12.522 | 1.0977 | 235 | 3.664 | 0.5610 | 220 | 26 | 9.420 |
| 56 | -19.692 | n1.103. | 116 | + 1.281 | 0.1041 | 176 | +10.459 | 1.0055 | 2:36 | $-4.007$ | $n 0.6093$ | 224 | -0.01 | n5.59.4 |
| 2 | 12.6*3 | $1.10: 3$ | 117 | 1.617 | 0.2087 | 177 | 12.886 | 1.092.) | 837 | 4.313 | $0.63,353$ | 224 | $+9.18$ | $p^{\prime} 9.268$ |
| 5.5 | 19661 | 1.1026 | 113 | 1.963 | 0.232) | 178 | 11.391 | 1.0909 | 2:33 | 4. 6 \% $\%$ | 0.67807 | 232 | 0.41 | 0.619 |
| , | 19, (6; 3 | . 1016 | 119 | 2.307 | 0.31530 | 179 | 12.211 | 1.1863 | 2:39 | 5.018 | 0.7005 | 2:36 | 0.62 | 0.895 |
| (i) | -12.5:6 | $41.100 \%$ | 120 | + 2.619 | 0.42:31 | 180 | +12.10? | $1.08: 31$ | 240 | - 5.319 | $n 0.723: 3$ | 210 | +0.83 | 9.920 |

'I'le perturbations are expressed in hundredths of a second of are.


Perturbation of the Langitude by the Earth.
Constant added $166^{\prime \prime}$. $\mathbf{( 5 5}$.
1'eriod of Argument VI., 583 d .92.

| Arg. V1. | Equa. | Arg. VJ. | Lqua. | Arg. V1. | Lqua. | Arg. V1. | Equa: | Arg. VI. | Equa. | Arg. V1. | Equa. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{\text {d }}$ | J668 | $104^{\text {d }}$ | 47 | 208 | 27:0 | 312 | $91 \%$ | $416^{\text {d }}$ | 2093 | 520 | 2456 |
| 2 | 16.1 | 106 | 31 | 210 | (37\% | 314 | 846 | 418 | 217: | 529 | 2405 |
| 4 | 1675 | 108 | 13 | 212 | 25:1 | 316 | 783 | 420) | 2249 | 521 | 2354 |
| 6 | $16 \hat{7}$ | 110 | 8 | 214 | 2866 | 318 | \%19\% | 429 | 9356 | 596 | 9303 |
| 8 | 1679 | 112 | 3 | 216 | 2908 | $3{ }^{2} 0$ | 664 | 424 | 2400 | 528 | 29.94 |
| 10 | 1680 | 114 | 0 | 2 i | 2046 | 322 | 609 | 426 | 2473 | $5: 30$ | 2205 |
| 12 | 1675 | 116 | ${ }_{2}$ | 220 | $29 \% 9$ | 39, | 5.57 | 428 | 2.44 | 532 | 2158 |
| 14 | 1676 | 118 | 7 | 22 | 3009 | 326 | 509 | 430 | 9613 | 534 | 2112 |
| 16 | $16 \% 1$ | 120 | 16 | 2.4 | 30:35 | 328 | 464 | 432 | 2680 | 536 | 2068 |
| 18 | 1664 | 122 | 28 | 226 | 3057 | :330 | 423 | 483 | 2744 | $5: 3$ | 295 |
| 20 | 165\% | 12. | 45 | 223 | 3074 | 3:9 | 385 | 4:36 | 280.5 | 5.10 | 1985 |
| :22 | 1643 | 126 | 65 | 230 | 3087 | 334 | 359 | 438 | $2 \checkmark 63$ | 5.12 | 1946 |
| 94 | 1693 | 123 | 90 | 232 | 3095 | 336 | 322 | 440 | 2913 | 5.41 | 1910 |
| 26 | 1611 | 130 | 113 | 234 | 3099 | 335 | $2!6$ | 442 | 2971 | 546 | 1875 |
| 23 | 1591 | 132 | 149 | 236 | 3099 | 340 | 275 | 44.4 | $30: 0$ | 548 | 184:1 |
| 30 | 1569 | 134 | 185 | 233 | 3095 | 342 | 253 | 446 | 3065 | 550 | 181:1 |
| 32 | 1544 | 136 | 224 | 240 | 3086 | 344 | 245 | 448 | 3108 | 559 | 1786 |
| 34 | 1517 | 138 | 266 | 242 | 3073 | 346 | 237 | 450 | 314 | 5 T 4 | 1762 |
| 36 | 1486 | 140 | 315 | 244 | 3055 | 348 | 233 | 452 | 3152 | 5.56 | 1740 |
| 33 | 1454 | 142 | 361 | 246 | 3033 | 350 | 233 | 454 | $3 \pm 14$ | 5 5 8 | 1721 |
| 40 | 1419 | 144 | 414 | 248 | 3007 | 352 | 937 | 456 | 3941 | 560 | 1704 |
| $4 \cdot$ | 1332 | 146 | 470 | 250 | 2977 | 354 | 246 | 4.38 | $: 1265$ | 562 | 1690 |
| 44 | 1343 | 148 | 523 | 252 | 2943 | 336 | 259 | 460 | 3255 | 564 | 1679) |
| 46 | 1302 | 150 | 590 | 254 | 2905 | 353 | 277 | 462 | 3302 | 566 | 1670 |
| 48 | 1259 | 152 | 654 | 256 | 2864 | 360 | 299 | 464 | 3314 | 568 | 1663 |
| 50 | $1 \times 14$ | 154 | 720 | 258 | 2818 | 362 | 325 | 466 | :3:393 | 570 | 1659 |
| 59 | 1168 | 156 | 789 | 260 | 970 | 36.4 | 35.3 | 468 | 1332 | 57: | 1956 |
| 51 | 1120 | 158 | 860 | 262 | 2717 | 366 | 389 | 470 | 3329 | 574 | 1655 |
| 56 | 107! | 160 | 933 | 264 | 2662 | 368 | 426 | 47.3 | 3337 | 576 | 16.96 |
| 58 | 102\% | 169 | 1008 | 266 | 2604 | 370 | 468 | 474 | 3320 | 578 | 16.58 |
| 60 | 971 | 164 | 1084 | 263 | 2542 | 372 | 514 | 476 | $3: 311$ | 580 | 1661 |
| 63 | 130 | 166 | 1169 | 270 | 2479 | 374 | 563 | 473 | 3:9\% | 582 | 1664 |
| 64 | 868 | 168 | 124] | 272 | 241: | 376 | 615 | 480 | 3230 | 584 | 1668 |
| 66 | 816 | 170 | 1321 | 274 | 2344 | 378 | 671 | 485 | 32(6) | 586 | 1671 |
| (i8) | 764 | 17: | 1402 | 276 | 2973 | 380 | 7 T! | 484 | 32:37 | 588 | 1675 |
| 70 | 712 | 174 | 1483 | 978 | $2: 31$ | 382 | 791 | 486 | 3211 | $5!9$ | 1677 |
| 72 | 660 | 176 | 1564 | 280 | 2127 | 384 | 85.5 | 488 | 3182 | 592 | 1679 |
| 74 | 609 | 178 | 1646 | 282 | 2051 | $3 \pm 6$ | $92 ?$ | 490 | 31.50 | 594 | 1680 |
| 76 | 5.59 | 180 | 1727 | 234 | 19\%5 | 388 | 091 | 419 | 3116 | 596 | 1678 |
| 78 | 510 | 182 | 1808 | 206 | 1897 | 390 | 106:3 | 494 | $30 \% 9$ | 598 | 1696 |
| 80 | $46 \%$ | 184 | 1898 | 233 | 1819 | 392 | $11: 17$ | 406 | 30.39 | 600 | 1671 |
| 82 | 415 | 186 | 1967 | 290 | 1740 | 394 | 1219 | 498 | 9! 919 | 602 | 1664 |
| 84 | 370 | 188 | 2046 | 202 | 1661 | 396 | 1:28! | 500 | 2954 | 604 | 1635 |
| 86 | 327 | 190 | 2123 | 294 | 1582 | 398 | 1367 | 502 | 2009 | 606 | 1642 |
| 88 | (25.5 | 192 | 2198 | 296 | 1504 | 400 | 1446 | 504 | 2863 | 608 | 1627 |
| 90 | 946 | 1194 | 2432 | 2498 | 1496 | 402 | 1527 | 506 | 2814 | 610 | 1610 |
| 99 | 210 | 196 | $2: 143$ | 300 | 1348 | 404 | 1607 | 508 | 2764 | 612 | 1590 |
| 94 | 175 | 1193 | 2413 | 302 | 1279 | 406 | 1681 | 510 | 2714 | 614 | 1568 |
| 96 | 144 | 200 | 2479 | 304 | 1197 | 403 | 170) | 512 | 2663 | 616 | 1543 |
| 18 | 115 | 209 | 2.44 | 306 | 1123 | 410 | 1851 | 514 | 2612 | 618 | 1516 |
| 100 | 89 | 204 | 2605 | 3018 | 1051 | 412 | 1939 | 516 | 2.660 | $6: 3$ | 1485 |
| 102 | 67 | 206 | 2661 | 310 | 980 | 414 | 2013 | 518 | 2508 | $6 \pm 1$ | 14.53 |
| 104 | 47 | 21)8 | 2720 | 312 | 912 | 416 | 2093 | 520 | 2456 | 624 | 1418 |

The perturbations are expressed in hundredths of a second of are.




Add 33.26 to Arg . X. when $224^{\mathrm{d}} .7$ is subtracted from Arg . I.

|  | Perturbations of the Longitude by the Earth. <br> Horizontal Argument $=1$. <br> onstant added J'". 40. <br> Period of Argument 1. 224.7. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Arg. $\mathbf{X 1}$. | $0^{d}$ | $\mathrm{s}^{d}$ | $16^{1}$ | $2{ }^{\text {d }}$ | $3 \pm$ | $40^{10}$ | $44^{4}$ | $56^{d}$ | $6 i^{\prime \prime}$ | $8 \stackrel{1}{2}$ | $80^{d}$ | $88$ | $96^{\prime \prime}$ | H0 ${ }^{1}$ | 1退 ${ }^{\text {a }}$ |
| 0 | 71 | 80 | 88 | 94 | 98 | 100 | 102 | 105 | 110 | 117 | 127 | 140 | 153 | 165 | 177 |
| 1 | 63 | 21 | 79 | 85 | 88 | 90 | 92 | 95 | 99 | 105 | 115 | 126 | 139 | 15\% | 161 |
| 2 | 55 | 63 | 71 | 76 | 79 | 81 | 82 | 85 | 88 | 94 | 102 | 113 | 126 | 138 | 151 |
| 3 | 49 | 56 | 63 | 63 | 71 | 72 | 73 | 75 | 77 | 89 | 91 | 101 | 11:3 | 126 | 138 |
| 4 | 4. | 50 | 56 | 60 | 63 | 64 | 65 | 66 | 68 | 72 | 80 | 90 | 101 | 114 | 126 |
| 5 | 40 | 45 | 50 | 54 | 56 | 57 | 57 | 58 | 59 | 63 | 70 | 79 | 00 | 102 | 115 |
| 6 | 33 | 42 | 47 | 50 | 51 | 52 | 51 | 51 | 52 | 55 | 61 | 70 | 81 | 92 | 10.5 |
| 7 | 32 | 4.2 | 45 | 47 | 43 | 48 | 47 | 47 | 47 | 49) | 54 | 62 | -i | 84 | 9.5 |
| 8 | 42 | 43 | 46 | 47 | 47 | 47 | 45 | 44 | 43 | 45 | 49 | 56 | 65 | 76 | 87 |
| 9 | 47 | 47 | 48 | 49 | 49 | 48 | 45 | 43 | 4: | 42 | 45 | 51 | 60 | 70 | 81 |
| 10 | 54 | 53 | 53 | 54 | 5.3 | 51 | 43 | 45 | 43 | 42 | 44 | 49 | 56 | 65 | 75 |
| 11 | 63 | 61 | 61 | 60 | 51 | 57 | 53 | 49 | 46 | 44 | 45 | 43 | 54 | 62 | 71 |
| 12 | 73 | 71 | 70 | 69 | 67 | 64 | 61 | 56 | 51 | 49 | 47 | 49 | 5.3 | (i) | 67 |
| 13 | 84 | 82 | 81 | 80 | 77 | 34 | 70 | 64 | 59 | 5 | 52 | 52 | 5.3 | 5.9 | 66 |
| 14 | 95 | 94 | 92 | 91 | 89 | 85 | 80 | 74 | 68 | 6: | 58 | 57 | 5 | 61 | 65 |
| 15 | 107 | 106 | 104 | 103 | 101 | 97 | 9 | 85 | 78 | 72 | 66 | 63 | 62 | 63 | 66 |
| 16 | 118 | 117 | 116 | 115 | 114 | 10.9 | 104 | !7 | 89 | 82 | 75 | 70 | 68 | 67 | 6!) |
| 17 | $1 \cdot 3$ | 123 | 123 | 127 | 125 | 121 | 116 | 103 | 100 | 92 | 84 | 78 | 7.1 | 73 | 73 |
| 18 | 1:38 | $1: 36$ | $1: 38$ | 137 | 136 | 13.2 | 127 | 119 | 111 | 112 | 94 | 87 | $8:$ | 79 | 78 |
| 19 | 146 | 146 | 146 | 146 | 145 | 141 | 136 | 129 | 121 | 112 | 103 | 95 | 90 | 86 | 83 |
| 20 | 1.53 | 1:3 | 153 | 153 | 152 | 148 | 144 | 137 | 129 | 120 | 111 | 103 | 97 | 93 | 90 |
| 21 | 158 | 108 | 158 | 158 | 157 | 154 | 150 | 144 | 136 | 127 | 118 | 110 | 104 | 100 | $9 \%$ |
| 22 | 163 | 162 | 162 | $15 \%$ | 161 | 158 | 154 | 148 | 140 | 133 | 124 | 116 | 111 | 106 | 103 |
| 23 | 166 | 160 | 164 | 163 | 162 | 160 | 156 | 150 | 1113 | 1336 | 128 | 121 | 115 | 112 | 109 |
| 24 | 168 | 166 | 165 | 164 | 163 | 160 | 156 | 151 | 145 | 138 | 130 | 124 | 119 | 116 | 114 |
| 6 | 170 | 167 | 165 | 164 | 169 | 160 | 156 | 151 | 144 | 133 | 131 | 125 | 121 | 119 | 117 |
| 26 | 172 | 168 | 16:3 | 163 | 161 | 158 | 154 | 149 | 143 | 136 | 130 | 124 | 121 | 119 | 11!) |
| 27 | 174 | 169 | 166 | 163 | 160 | 157 | 152 | 147 | 140 | $1: 14$ | 128 | 123 | 120 | 119 | 11!) |
| 23 | 176 | 171 | 167 | 164 | 160 | 156 | 151 | 144 | 138 | 131 | 125 | $1 \geqslant 0$ | 117 | 116 | 117 |
| 29 | 179 | 174 | 16!) | 165 | 161 | 156 | 150 | 143 | 136 | 123 | 122 | 116 | 113 | 11: | 114 |
| 30 | 183 | 17\% | 172 | 167 | 162 | 157 | 150 | 143 | 135 | 126 | 118 | 112 | 109 | 107 | 109 |
| 31 | 187 | 181 | 176 | 171 | 166 | 150 | 159 | 144 | 134 | 125 | 116 | 109 | 104 | 102 | 103 |
| 32 | 190 | 185 | 181 | 176 | 370 | 163 | 155 | 146 | 135 | 125 | 114 | 106 | 100 | 97 | ! 17 |
| 33 | 194 | 190 | 186 | 182 | 176 | 16.9 | 160 | 150 | 138 | 126 | 114 | 10.1 | 96 | 92 | !) |
| 34 | 198 | 195 | 192 | 188 | 183 | 176 | 166 | 156 | 143 | 129 | 115 | 104 | 0.1 | 83 | 86 |
| 35 | 201 | 200 | 198 | 195 | 190 | 183 | 174 | 169 | 149 | 134 | 119 | 10\% | 94 | 86 | 82 |
| 36 | 204 | 204 | 203 | 202 | 197 | 191 | 182 | 170 | 156 | 140 | 124 | 108 | 95 | 86 | 80 |
| 37 | 205 | 208 | 208 | 207 | 204 | 199 | 191 | 179 | 164 | 148 | 131 | 114 | 99 | 87 | 80 |
| 38 | 205 | 208 | 211 | 212 | 211 | 206 | 199 | 188 | 174 | 157 | 139) | 121 | 105 | 92 | 83 |
| 39 | 204 | 209 | 213 | 216 | 216 | 213 | 207 | 198 | 184 | 167 | 149 | 130 | 113 | 98 | 88 |
| 40 | 201 | 208 | 214 | 218 | $2 \%$ | 219 | 215 | 206 | 194 | 178 | 160 | 141 | '123 | 107 | 95 |
| 41 | 107 | 205 | 213 | 219 | 223 | 924 | 221 | 215 | 203 | 189 | 171 | 15:3 | 134 | 118 | 105 |
| 42 | 192 | 202 | 211 | 219 | 225 | 228 | 296 | 29 | 213 | 200 | 183 | 165 | 147 | 130 | 116 |
| 43 | 186 | 197 | 208 | 217 | 225 | 930 | 2311 | 299 | 291 | 211 | 196 | 178 | 161 | 143 | 12!) |
| 44 | 179 | 192 | 203 | 214 | 224 | 231 | 235 | 234 | 929 | 221 | 207 | 191 | 175 | 158 | 143 |
| 45 | 172 | 185 | 198 | 210 | 229 | 231 | 237 | 239 | 236 | 230 | 219 | 204 | 188 | 17\% | 157 |
| 46 | 167 | 178 | 192 | 206 | 218 | 230 | 2:38 | 242 | 2.13 | 238 | 2:29 | 216 | 201 | 186 | 171 |
| 47 | $15 \%$ | 171 | 186 | 200 | 214 | 297 | 2:38 | 245 | 217 | 245 | 2:38 | 237 | 213 | 199 | 184 |
| 48 | 150 | 163 | 178 | 19.1 | 209 | $2 \cdot 4$ | 236 | 246 | 250 | 250 | 246 | $2: 37$ | 224 | 211. | 196 |
| 49 | 14\% | 156 | 171 | 187 | 204 | 220 | 234 | 245 | 252 | 254 | 252 | 245 | 234 | 222 | 208 |
| 50 | 134 | 147 | 162 | 179 | 197 | 214 | 239 | 213 | 252 | 237 | 256 | 251 | 242 | 231 | 218 |
| 51 | 126 | 139 | 15.4 | 170 | 18! | 907 | $2 \cdot 5$ | 235 | 250 | 257 | 259 | 255 | 248 | 2:3 | 226 |
| 52 | 117 | 129 | 144 | 161 | 180 | 19\% | 218 | 234 | 246 | 2.56 | 2.9 | 258 | 252 | 243 | 23: |
| 53 | 108 | 119 | 133 | 150 | 169 | 189 | 209 | 226. | 241 | 959 | 9.5 | 2.88 | 254 | 947 | 9337 |
| 54 | 915 | 109 | 192 | 133 | 157 | 178 | 198 | $2177^{\circ}$ | 233 | 245 | 953 | 256 | 254 | 249 | 240 |
| 5 | 90 | 93 | 110 | 125 | 144 | 164 | 185 | 205 | 223 | 237 | 247 | 251 | 259 | 298 | 212 |
| 56 | 81 | 87 | 97 | 111 | 199 | 149 | 170 | 191 | 210 | 2326 | 2:38 | 24.5 | 2.18 | 246 | 241 |
| 57 | 72 | 76 | 84 | 96 | 113 | 133 | 154 | 175 | 196 | 213 | 297 | 236 | 211 | 242 | 239 |
| 58 | 63 | 64 | 70 | 81 | $!9$ | 115 | 136 | 158 | 179 | 198 | 214 | 4 | 2:33 | 236 | 235 |
| $59$ | 55 | 54 | 57 | 66 | 73 | 97 | 117 | 139 | 161 | 181 | 19\% | 212 |  | 223 | 2:30 |
| 60 | 49 | 45 | $4{ }^{\circ}$ | 51 | 63 | 79 | 98 | 11.9 | 141 | 16.3 | $10 \%$ | 198 | 210 | 218 | 2:3 |


| Perturbations of the：Lengitude by the Earth． Ilurizumtal $A$ rgument $=1$. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Constant added 1＇．10．Period of Argamemite 210 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | $120^{\prime \prime}$ | 12＊＊ | $136^{\prime \prime}$ | 111 | 15＊ | $160^{\prime \prime}$ | 168 | 176 | 181 | $19 \%$ | 200 | 208 | $216^{\prime \prime}$ | 221 | 238 |
| 0 | 158 | 195 | 201 | 214 | 20.3 | 206 | 406 | 2017 | 2）： | 211 | 21：1 | 214 | 21.1 | 211 | 2） 5 |
| 1 | 120 | 183 | $1 \leq 15$ | 193 | 19 | 1！\％ | 198 | 211 | 204 | 218 | 212 | 215 | 216 | 25 | 211 |
| \％ | $16 \pm$ | 170 | 176 | 102 | 18.5 | $1-7$ | $1: 10$ | 11：3 | $1: 13$ | 203 | 209 | 213 | 217 | 218 | 21.5 |
| 3 | 1．1！ | $1: 17$ | 166 | 171 | 17.1 | 1i＊ | 151 | 18.5 | $1: 19$ | 197 | 20.4 | 211 | 216 | 219 | 218 |
| 4 | $13 *$ | 117 | 15.5 | 160 | 161 | 16： | 172 | 177 | $1 \geq 3$ | 1：0 | 199 | 207 | 21.4 | 218 | 219 |
| 5 | 127 | 136 | 141 | 150 | 15.5 | 1.54 | 16：3 | 163 | 1\％ | 18：3 | 193 | 20） | 210 | 216 | 219 |
| 6 | 116 | 197 | 13.1 | 1.11 | 11.7 | 149 | 1.54 | 159 | 1616 | 176 | 1－6 | $1: 46$ | 211 | 214 | 213 |
| 7 | 110 | 117 | 12.5 | 13： | 137 | 140 | 14．： | 1，51 | 1.15 | 11 is | 179 | 191） | 2.1 | 211 | 217 |
| ， | （9） | 101 | 117 | $1: 1$ | 123 | 119 | 1：37 | 142 | 1.50 | 15．） | 171 | $1 \times 3$ | 196 | 2is | 21.5 |
| 1 | 12 | 101 | $10: 3$ | 116 | 120 | 121 | 128 | 134 | 141 | 1.15 | 16.4 | $1: 7$ | 191 | 20.1 | 24 |
| 10 | 8 | \％ | 102 | 3ns | 112 | 116 | 120 | 125 | 133 | 113 | $1: 96$ | 170 | 186 | 200 | 21： |
| 11 | 80 | 8 | 96 | 101 | 10．5 | 109 | 11：1 | 117 | 124 | 11.5 | 1．19 | 161 | $1 \times 3$ | 196 | 21 |
| 13 | 76 | 84 | 90 | 95 | 99 | 102 | 30.5 | 110 | 117 | 127 | 1.11 | 1.5 | 17．15 | 192 | $29!$ |
| 1：1 | 73 | 80 | $8 i$ | 91 | 93 | 9 | 93 | 102 | 109 | 119 | 1：31 | 1：50 | 16．） | 1s9 | 217 |
| 14 | 71 | 77 | 81 | 85 | 87 | 89 | 92 | 45 | 102 | 112 | 126 | 14：3 | 163 | 18.1 | 234 |
| 15 | 21 | 75 | 78 | 81 | $8: 3$ | 8.1 | 86 | 89 | 95 | 10.5 | 119 | 136 | 157 | 179 | 231 |
| 16 | 72 | 2 | 77 | 89 | 80 | 80 | 82 | 84 | $8!$ | \％ | 111 | 129 | 150 | 174 | 197 |
| 17 | 74 | 76 | 77 | 78 | 5 | 77 | 78 | 79 | $8: 3$ | 12 | 105 | 143 | 143 | 167 | $1!8$ |
| 13 | 78 | 78 | 79 | 79 | 78 | 76 | 76 | 76 | 7！ | 86 | ！8 | 11.5 | 136 | 163 | 18. |
| 19 | 83 | 83 | \％ | 81 | 79 | 77 | 75 | 7.4 | \％6 | 82 | 92 | 108 | 128 | 151 | 177 |
| $9)$ | 89 | 48 | 86 | 85 | 82 | 79 | 76 | 73 | 74 | 78 | 87 | 101 | 119 | 142 | 163 |
| 21 | 9.5 | 94 | 92 | 90 | 87 | $8: 3$ | 78 | 7.1 | 73 | 75 | 82 | 91 | 111 | 132 | $15 \%$ |
| ${ }^{2}$ | 102 | 101 | 99 | 96 | 9 | 87 | 89 | 78 | 7． 1 | \％ 4 | 78 | 98 | 10：1 | 192 | 146 |
| 23 | 108 | 107 | 115 | 103 | 99 | 93 | 87 | 81 | 75 | 7：3 | 7. | 83 | 35 | 112 | 131 |
| 24 | 114 | 113 | 11： | 110 | 105 | 100 | 93 | $8 \bar{\square}$ | 78 | 74 | 73 | 78 | 87 | 102 | 122 |
| 2 | 118 | 118 | 117 | 116 | 111 | 106 | 98 | 90 | 82 | 76 | 72 | 74 | 81 | 93 | 110 |
| 26 | 120 | 121 | 123 | 121 | 117 | 112 | 104 | 95 | 86 | 78 | $7: 1$ | 72 | 76 | 85 | 99 |
| 27 | 121 | 123 | 120 | 12.5 | 122 | 117 | 110 | 101 | 90 | 81 | 24 | 71 | 72 | 73 | 99 |
| 24 | 12： | 12：1 | 126 | 127 | 12， | 121 | 115 | 106 | 95 | 8.1 | 76 | 71 | 69 | $7: 1$ | 82 |
| 2．） | 117 | 121 | 125 | 127 | 127 | 124 | 118 | 110 | 99 | 88 | 78 | 72 | 63 | 69 | 76 |
| 30 | 113 | 117 | 129 | 126 | 127 | 126 | 121 | 113 | 103 | 99 | 81 | 4 | 69 | 67 | 71 |
| 31 | 107 | 112 | 118 | 123 | 12.5 | 125 | 121 | 115 | 106 | 96 | 85 | 77 | 70 | 67 | 69 |
| 32 | 100 | 106 | 112 | 118 | 122 | 121 | 121 | $11 \%$ | 103 | 99 | 88 | 80 | 72 | 69 | （is |
| 33 | 94 | 99 | 106 | 113 | 118 | 121 | 120 | 117 | 110 | 101 | 9 | 83 | 76 | 71 | 63 |
| 34 | 88 | $9 \%$ | 99 | 107 | 113 | 117 | 118 | 117 | 111 | 104 | 95 | 87 | 39 | 24 | 3 |
| 35 | 83 | 86 | 93 | 101 | 108 | 113 | 116 | 116 | 112 | 106 | 98 | 91 | 83 | \％ | 7 |
| 36 | 79 | 82 | 88 | 96 | 103 | 119 | 114 | 11.5 | 113 | 10.3 | 102 | 9 | 87 | 82 | 78 |
| 37 | 78 | 79 | 8.5 | $!2$ | 100 | 107 | 112 | 114 | 113 | 110 | 10. | 99 | 92 | 46 | $8!$ |
| 38 | 78 | $3!$ | 83 | 90 | 93 | 105 | 111 | 114 | 115 | 112 | 103 | 103 | 0 | 91 | 8 |
| 39 | 82 | 81 | 84 | 90 | 98 | 105 | 111 | 115 | 117 | 115 | 111 | 107 | 100 | 95 | 91 |
| 40 | 88 | 85 | 87 | 93 | 100 | 107 | 113 | 118 | 119 | 118 | 115 | 111 | 105 | 100 | 9.5 |
| 41 | 96 | 92 | 93 | 97 | 104 | 110 | 117 | 121 | 123 | 129 | 119 | 115 | 109 | 104 | 99 |
| 42 | 106 | 101 | 101 | 103 | 109 | 115 | 121 | 126 | 127 | 1197 | 124 | 120 | 114 | 109 | 104 |
| 43 | 118 | 111 | 110 | 112 | 116 | 122 | 127 | 131 | 133 | 133 | 12：） | 12 | 119 | 114 | 109） |
| 44 | 131 | 123 | 120 | 121 | 125 | 130 | 135 | 138 | 139 | 139 | 136 | 131 | 125 | 119 | 114 |
| 45 | 144 | 136 | 132 | 132 | 134 | $1: 18$ | 142 | 14.5 | 146 | 146 | 142 | 137 | 131 | 12.5 | 129 |
| 46 | 158 | 149 | 144 | 142 | 144 | 147 | 151 | 15.3 | 154 | 15.3 | 149 | 14.4 | 138 | 132 | 126 |
| 47 | 171 | 161 | 15.7 | 153 | 153 | 156 | 159 | 169 | 161 | 160 | 156 | 151 | 145 | $13: 4$ | 133 |
| 4.3 | 154 | 173 | 166 | 163 | 163 | 164 | 167 | 168 | 169 | 167 | 163 | 158 | 150 | 146 | 141） |
| 49 | 195 | 184 | 126 | 172 | 171 | 172 | 174 | 130 | 176 | 37.4 | 170 | 165 | 159 | 153 | 143 |
| 5 | 295 | 194 | 185 | 181 | 179 | 179 | 189 | 181 | 182 | 180 | 177 | 172 | 166 | 160 | 15.3 |
| 51 | 213 | 202 | 193 | 189 | 135 | 185 | 126 | 187 | 187 | 186 | 183 | 178 | 172 | 167 | 162 |
| 没 | 等 | 209 | 200 | 194 | 191 | 190 | 191 | 192 | $1!2$ | 191 | 188 | 184 | 178 | 1711 | 163 |
| 5 | 226 230 230 | 21.5 | 206 |  | 196 201 | 190 | ${ }_{1}^{1199}$ | 196 | 196 200 | 195 | 192 196 | 192 | 183 | 178 | 173 177 |
| 54 | 230 | 220 | 211 | 235 | 201 | 192 | 199 | 199 | 200 | 193 | 196 | 192 | 107 | 189 | 177 |
|  | 233 | 24 | 215 | 203 | 205 | 202 | 202 | 203 | 202 | 201 | 103 | 195 | 190 | 184 | 179 |
| 56 | $2: 34$ | 226 | 218 | $21:$ | 208 | 20 | 20.4 | 20.3 | 205 | 203 | 230 | 197 | 191 | 146 | $1 \times 1$ |
| ：7 | 2：34 | 427 | 䐴 | 215 | 211 | 239 | 2107 | 208 | 207 | ${ }_{202} 2.8$ | 202 | 193 | 19 | 156 | 130 |
| 5 | － | 227 |  | 218 | 214 | 214 | 210 | 210 212 | 29！ | 2）7 | 293 <br> 20.1 | 1198 | 192 | 18.4 | 179 |
| $6)$ | 24 | 241 | 202 | 220 | 218 | 216 | 21．， | 215 | 213 | 210 | 20. | 198 | 191 | 153 | 171 |

Add 147.64 to Arg．XI．when 294.5 is subtracted from Arg． 1.


| たニテニゴ心 | こニご， |  | －후心夊心気 |  | 以忒ご边 | gractut | $x_{4}^{\text {¢ }}$ | －1がごごこ | 二发忒ご気 | 898\％ | 은읭 | $\underset{y y y y}{c}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | ご心忒忒 |  |  | cigctis | gacace | い気忥気島 |  | $\stackrel{6}{6}$ |  |
| － |  |  |  | 気忥志馬嵒 | ※ニデ怘合。 | 忥忥呺 |  | \％$\square^{5}$ | ¢ンがすご |  |  | 念 |  |
|  |  |  | 或呺気灾 |  |  | こsxax | $x=159$ | ¢88를 |  |  |  | \％ |  |
|  |  |  |  |  |  | $3^{-2} a^{-2}=\overrightarrow{3}$ | 二小心灾乐 | 8タミニ゙ | ¢○このごさ | 忥或気言突 |  | $\stackrel{m}{m}$ |  |
|  |  |  |  |  |  | 99크릐 | 긍9응 |  |  |  |  | $\begin{aligned} & \text { 思 } \\ & \text { 空ニ } \end{aligned}$ |  |
|  |  |  | 気気心忒 | 드ㅇㅡㄸํํㅇํㅇ | ¢cysigis | 989얭 | ダすごぐに | ※x ¢ ¢ |  |  |  | $\stackrel{y}{\delta}=$ |  |
|  |  | 或ごご突 |  |  | 㐫会会会感 | citg cis |  | 色念总に突 | 或忥忥詋区 |  |  | － |  |
|  |  | 忒矛或或总 |  | 或芽ご芯去 |  | 式ggit |  |  |  |  |  | $\begin{aligned} & \text { E } \\ & \text { ean } \end{aligned}$ |  |
|  | 忥気気匂灾 | す⿹勹口欠心ごす | 8－¢ ¢ ¢ |  |  |  |  |  |  |  |  | 年 |  |
|  |  |  | 준ํㅡㄹ |  |  |  | シここに笖苞 | 気気気ご湯 |  |  | ただきだった。 | $\begin{aligned} & m \\ & B=3 \\ & B= \end{aligned}$ |  |
| 或気気気灾 | બ゙ず¢ ¢ ¢ |  |  | 式 | $\underset{\sim}{\omega}$ | รษ์ ล์ |  |  | $\mathrm{cos}_{-1}^{10}$ |  | きたほきだす | 180 |  |
|  |  | 愛炎ここの | 可枵式合合 |  | 枈念忒咸发 |  | 或忥気氙 |  |  |  |  | ${ }_{0}^{10}$ |  |
|  |  |  | ごの訋き会 |  |  | ごごミ | 気忥忥ご気 |  |  |  | 忥忥宗宫 | ＊ |  |
| 式ご忒ごご気 | 忥氙玉忥灾 | 灾気忥ぎ |  |  | ¢ |  |  |  |  |  | 뚜cay | 伿 |  |
|  |  |  |  |  | 옹N心令 | 岩华氙玄突 | 或ご気気 |  |  | 可或こご気 | 可ごこここ | 迌 |  |



| Perturbations of the Lonnsitule liy the Earrth. <br> Horizontal Argunent $=1$. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| .rg.x1 | 120 | $12{ }^{18}$ | 18\% | $11^{11}$ | 1.32 | 190 | $14{ }^{\text {¢ }}$ | 176 | 181 | 192 | 203 | $208{ }^{8}$ | $216^{\text {d }}$ | ${ }^{1}$ | $233^{\frac{1}{2}}$ |
|  |  | $\begin{aligned} & 1010 \\ & \begin{array}{l} 168 \\ 1050 \\ 141 \end{array} \end{aligned}$ |  |  |  |  |  |  |  |  |  |  | ais |  |  |
|  |  |  |  |  | $\begin{aligned} & 170 \\ & \hline 1061 \\ & \hline 140 \\ & 130 \\ & 130 \end{aligned}$ |  | $\begin{aligned} & 196 \\ & 190 \\ & 170 \\ & 1750 \\ & 1.46 \end{aligned}$ |  |  |  |  |  |  |  |  |
|  | $\begin{aligned} & 83 \\ & 88 \\ & 80 \end{aligned}$ | $\begin{aligned} & 8.8 \\ & 87 \\ & 97 \\ & 97 \end{aligned}$ |  |  | $\begin{aligned} & 110 \\ & 100 \\ & 100 \\ & 100 \\ & 100 \end{aligned}$ | $\begin{aligned} & 193 \\ & \substack{193 \\ 110 \\ 106 \\ 1005} \end{aligned}$ | $\begin{gathered} 137 \\ 192 \\ 192 \\ 116 \\ 113 \end{gathered}$ |  | $\begin{aligned} & 161 \\ & 1.65 \\ & 1.10 \\ & 1134 \\ & 134 \end{aligned}$ |  | $\begin{gathered} 1-6 \\ \substack{179 \\ \text { and } \\ 165 \\ 1505} \end{gathered}$ | $\begin{aligned} & 198 \\ & 1810 \\ & 171 \\ & 177 \\ & 172 \end{aligned}$ |  |  |  |
| $\begin{aligned} & 113 \\ & 1.16 \\ & \text { and } \\ & 137 \\ & 1390 \end{aligned}$ |  | $\begin{aligned} & 1919 \\ & 119 \\ & \text { and } \\ & 1297 \\ & 139 \end{aligned}$ | $\begin{aligned} & 103 \\ & 110 \\ & 118 \\ & 1206 \\ & 135 \end{aligned}$ |  | $\begin{aligned} & 193 \\ & 107 \\ & 113 \\ & 1193 \\ & 125 \end{aligned}$ |  | $\begin{aligned} & 111 \\ & 112 \\ & 1126 \\ & 1119 \end{aligned}$ | $\begin{aligned} & 119 \\ & 117 \\ & 1116 \\ & 1117 \end{aligned}$ |  | $\begin{aligned} & 149 \\ & 139 \\ & 130 \\ & 130 \\ & 190 \\ & \hline 9 . \end{aligned}$ |  |  |  | $\begin{aligned} & 189 \\ & 171 \\ & 170 \\ & 160 \\ & 160 \end{aligned}$ |  |
|  | $\begin{aligned} & 136 \\ & \left.\begin{array}{l} 136 \\ \text { ar } \\ 137 \\ 137 \end{array}\right) \end{aligned}$ | $\begin{aligned} & 139 \\ & \substack{13 \\ 1.14 \\ 143 \\ 141} \end{aligned}$ |  | $\begin{aligned} & 135 \\ & 1.10 \\ & 1,13 \\ & 145 \\ & 145 \end{aligned}$ | $\begin{aligned} & 133 \\ & 135 \\ & 139 \\ & 1.41 \\ & 142 \end{aligned}$ | $\begin{aligned} & 1969 \\ & 139 \\ & 133 \\ & 139 \\ & 135 \end{aligned}$ |  | $\begin{aligned} & 118 \\ & 119 \\ & 190 \\ & 1201 \\ & 120 \end{aligned}$ | $\begin{aligned} & 117 \\ & 1116 \\ & 116 \\ & 116 \end{aligned}$ | $\begin{aligned} & 119 \\ & 119 \\ & 1114 \\ & 1109 \end{aligned}$ | $\begin{aligned} & 193 \\ & 119 \\ & 1115 \\ & 110 \\ & 106 \end{aligned}$ | $\begin{aligned} & 135 \\ & 125 \\ & 119 \\ & 119 \\ & 109 \end{aligned}$ | $\begin{aligned} & 110 \\ & \text { and } \\ & 133 \\ & 139 \\ & 1111 \end{aligned}$ |  | $\begin{aligned} & 16 . \\ & \begin{array}{l} 169 \\ 1.411 \\ 1111 \\ 1.123 \end{array} \end{aligned}$ |
| $\begin{aligned} & 146 \\ & 1.16 \\ & 1.17 \\ & 1.14 \\ & 149 \end{aligned}$ |  | $\begin{aligned} & 1373 \\ & 133 \\ & 1393 \\ & 123 \\ & 113 \end{aligned}$ | $\begin{aligned} & 1423 \\ & \text { and } \\ & 1353 \\ & 13505 \end{aligned}$ | $\begin{aligned} & 1131 \\ & 133 \\ & 133 \\ & 138 \\ & 130 \end{aligned}$ | $\begin{aligned} & 1414 \\ & 139 \\ & 137 \\ & 138 \\ & 139 \end{aligned}$ | $\begin{aligned} & 133 \\ & \text { and } \\ & 13,31 \\ & 1301 \end{aligned}$ | $\begin{aligned} & 1288 \\ & 128 \\ & 127 \\ & 1266 \end{aligned}$ | $\begin{aligned} & 129 \\ & 119 \\ & 1118 \\ & 117 \end{aligned}$ | $\begin{aligned} & 113 \\ & 111 \\ & 110 \\ & 109 \\ & 108 \end{aligned}$ | $\begin{gathered} 106 \\ 106 \\ 101 \\ 0101 \\ 0,0 \end{gathered}$ | $\begin{aligned} & 109 \\ & 9.9 \\ & 9 . \\ & 91 \\ & \hline 98 \end{aligned}$ |  |  |  | $\begin{aligned} & 129 \\ & 1101 \\ & 101 \\ & 9.19 \\ & 79 \end{aligned}$ |
|  |  |  | $\begin{aligned} & 191 \\ & 117 \\ & 111 \\ & 111 \end{aligned}$ | $\begin{aligned} & 126 \\ & 123 \\ & 129 \\ & 1118 \\ & 118 \end{aligned}$ |  |  |  | $\begin{aligned} & 116 \\ & 116 \\ & 117 \\ & 117 \end{aligned}$ | $\begin{aligned} & 107 \\ & 107 \\ & 109 \\ & 109 \\ & 110 \end{aligned}$ | $\begin{aligned} & 96 \\ & 96 \\ & 96 \\ & 979 \\ & 997 \end{aligned}$ | $\begin{aligned} & 85 \\ & 83 \\ & 83 \\ & 83 \\ & 83 \\ & 83 \end{aligned}$ | $\begin{aligned} & 76 \\ & 7.3 \\ & 71 \\ & 70 \\ & 71 \\ & 71 \end{aligned}$ | $\begin{aligned} & 69 \\ & 69 \\ & 50 \\ & 50 \\ & 507 \\ & 50 \end{aligned}$ |  |  |
| $\begin{aligned} & 186 \\ & \begin{array}{l} 107 \\ 150 \\ 150 \\ 159 \end{array} \end{aligned}$ | $\begin{aligned} & 102 \\ & 100 \\ & 100 \\ & 1113 \\ & 119 \end{aligned}$ | $\begin{aligned} & 107 \\ & \begin{array}{l} 107 \\ 109 \\ 109 \\ 1116 \end{array} \end{aligned}$ | $\begin{aligned} & 110 \\ & 111 \\ & 1113 \\ & 1116 \\ & 116 \end{aligned}$ | $\begin{aligned} & 1166 \\ & 1116 \\ & 118 \\ & 118 \end{aligned}$ | $\begin{gathered} 129 \\ 120 \\ 120 \\ 1290 \\ 1200 \end{gathered}$ | $\begin{aligned} & 193 \\ & 123 \\ & 193 \\ & 193 \\ & 193 \\ & 1 \times 3 \end{aligned}$ | $\begin{aligned} & 123 \\ & 193 \\ & 193 \\ & 1920 \\ & 190 \end{aligned}$ | $\begin{aligned} & 120 \\ & 192 \\ & 193 \\ & 1230 \\ & 120 \end{aligned}$ |  | $\begin{aligned} & 102 \\ & \text { jon } \\ & 1010 \\ & 1114 \\ & 118 \end{aligned}$ |  | $\begin{aligned} & 73 \\ & 78 \\ & 81 \\ & 80 \\ & 80 \\ & 80 \end{aligned}$ | $\begin{aligned} & 56 \\ & 59 \\ & 94 \\ & 79 \\ & 79 \end{aligned}$ |  |  |
|  |  |  | $\begin{aligned} & 119 \\ & 1,96 \\ & 1.196 \\ & 145 \end{aligned}$ | $\begin{aligned} & 11929 \\ & 1926 \\ & 1296 \\ & 138 \\ & 138 \end{aligned}$ |  |  |  | $\begin{aligned} & 1929 \\ & 1920 \\ & 130 \\ & 138 \\ & 134 \end{aligned}$ | $\begin{gathered} 126 \\ \substack{190 \\ 1.13 \\ 139 \\ 137} \\ \hline \end{gathered}$ |  | $\begin{aligned} & 1111 \\ & \substack{1112 \\ 1.18 \\ 133 \\ 139} \end{aligned}$ |  |  | ( |  |
|  |  |  |  | $\begin{aligned} & 146 \\ & 1,50 \\ & 1,505 \\ & 1990 \\ & 192 \end{aligned}$ | $\begin{aligned} & 149 \\ & 148 \\ & 1,168 \\ & 169 \\ & 189 \end{aligned}$ | $\begin{aligned} & 13 \pi \\ & 1,43 \\ & 1,50 \\ & 1 ; 61 \\ & 1=1 \end{aligned}$ | $\begin{gathered} 136 \\ 1.19 \\ 1,17 \\ 169 \end{gathered}$ | $\begin{aligned} & 137 \\ & 141 \\ & 4195 \\ & 1515 \\ & 153 \end{aligned}$ | $\begin{aligned} & 119 \\ & \hline 143 \\ & 4197 \\ & 1515 \\ & 156 \end{aligned}$ | $\begin{aligned} & 1464 \\ & \hline 146 \\ & \hline 143 \\ & 153 \\ & \hline 58 \end{aligned}$ | $\begin{gathered} 144 \\ \substack{148 \\ 5 \\ 5150 \\ 150 \\ 150} \end{gathered}$ |  | $\begin{aligned} & 131 \\ & 112 \\ & 154 \\ & 159 \\ & 163 \\ & \hline 163 \end{aligned}$ |  |  |
|  |  |  |  |  |  | $\begin{aligned} & 183 \\ & \hline 1051 \\ & 2027 \\ & 2139 \\ & \hline 130 \end{aligned}$ |  |  | $\begin{aligned} & 169 \\ & \hline 169 \\ & \hline 176 \\ & \hline 1819 \\ & 190 \end{aligned}$ | $\begin{aligned} & 161 \\ & 166 \\ & 176 \\ & 776 \\ & 762 \end{aligned}$ |  |  |  | $\underset{\substack{16 \pi \\ 170 \\ 171 \\ 171}}{\substack{12}}$ |  |
|  |  |  |  |  |  |  |  |  |  |  |  | $\begin{aligned} & 17 \% \\ & 170 \\ & 170 \\ & 1701 \\ & 183 \end{aligned}$ |  | (1701 |  |


| Constant added 1 1/40. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
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| Afg. $\mathrm{M1}$. | ¢ | ${ }_{8}^{8}$ | ${ }_{16} 16$ | din | $3^{2} 2$ | ic | A's | 56 | 62. | $\stackrel{4}{2}$ | sio | sis | ${ }_{96}$ | 108 | $11^{2} 2$ |
| $\begin{aligned} & 181 \\ & \begin{array}{l} 188 \\ 183 \\ 184 \end{array} \end{aligned}$ |  | $\begin{gathered} 68 \\ 70 \\ 70 \\ 78 \\ 70 \\ 70 \end{gathered}$ | $\begin{gathered} 7 . \\ 78 \\ 78 \\ 78 \end{gathered}$ |  | $\begin{aligned} & 79 \\ & 78 \\ & 78 \end{aligned}$ | $\begin{aligned} & 97 \\ & 90 \\ & 80 \\ & 85 \\ & 80 \\ & 80 \end{aligned}$ | $\begin{aligned} & 108 \\ & 90 \\ & 99 \\ & 89 \\ & 89 \end{aligned}$ | $\begin{aligned} & 19 \\ & 107 \\ & 90 \\ & 90 \\ & 80 \end{aligned}$ | $\begin{aligned} & 1266 \\ & 106 \\ & 105 \\ & 95 \\ & 97 \end{aligned}$ | $\begin{aligned} & 100 \\ & 110 \\ & 110 \\ & 190 \\ & 89 \end{aligned}$ | $\begin{aligned} & 150 \\ & 130 \\ & 1130 \\ & 104 \\ & 104 \end{aligned}$ |  | $\begin{aligned} & 1727 \\ & 176 \\ & 136 \\ & 109 \\ & 109 \end{aligned}$ | $\begin{aligned} & 186 \\ & 1.64 \\ & 1.129 \\ & 112 \end{aligned}$ | $\begin{aligned} & 1798 \\ & 170 \\ & 1601 \\ & 1.23 \\ & 120 \end{aligned}$ |
| $\begin{aligned} & 185 \\ & 1186 \\ & 187 \\ & 180 \\ & 189 \end{aligned}$ | $\begin{gathered} 87 \\ 97 \\ 90 \\ 90 \\ \hline 1010 \end{gathered}$ | $\begin{gathered} 83 \\ .87 \\ .97 \\ \hline 9 . \\ 100 \end{gathered}$ | $\begin{aligned} & 80 \\ & 80 \\ & 80 \\ & 93 \\ & 97 \\ & 97 \end{aligned}$ | $\begin{aligned} & 79 \\ & 89 \\ & 89 \\ & 89 \\ & 89 \\ & \hline 9 . \end{aligned}$ | 79 81 84 87 67 | $\begin{aligned} & 80 \\ & 80 \\ & 80 \\ & 805 \\ & 889 \end{aligned}$ | $\begin{aligned} & 80 \\ & 80 \\ & 80 \\ & 80 \\ & 80 \\ & 80 \end{aligned}$ | $\begin{aligned} & 81 \\ & 78 \\ & 78 \\ & 78 \\ & 80 \\ & 80 \end{aligned}$ |  | $\begin{aligned} & 82 \\ & 76 \\ & 78 \\ & 70 \\ & 70 \\ & \hline 0 . \end{aligned}$ |  | $\begin{aligned} & 85 \\ & \begin{array}{l} 85 \\ 68 \\ 63 \\ 60 \\ 60 \end{array} \end{aligned}$ |  | $\begin{aligned} & 973 \\ & 83 \\ & 83 \\ & 68 \\ & 58 \end{aligned}$ | 107 <br> 98 <br> 81 <br> 81 <br> 1 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1 | ${ }_{\text {H }}^{111}$ | ${ }_{\substack{105 \\ 100}}$ | ${ }_{\substack{101 \\ 106}}$ | ${ }^{193}$ | ${ }^{95}$ | ${ }_{96}$ | ${ }^{92}$ | ${ }_{87}^{83}$ | 81 | ${ }_{2}$ | ${ }_{66}^{64}$ | 59] | 5 | 5 | - 5 |
| $\begin{aligned} & 1999 \\ & 193 \\ & 193 \end{aligned}$ | $\begin{aligned} & 115 \\ & 1951 \\ & 1297 \end{aligned}$ | $\begin{aligned} & 11016 \\ & 1,262 \end{aligned}$ | 1 | $\begin{aligned} & 103 \\ & 1114 \\ & 114 \end{aligned}$ | cilio | $\begin{gathered} 969 \\ 102 \\ 102 \end{gathered}$ | $\begin{array}{r} 97 \\ \\ \hline 104 \end{array}$ | $\begin{aligned} & 87 \\ & 98 \\ & 98 \\ & 98 \end{aligned}$ | $\begin{aligned} & 81 \\ & 81 \\ & 91 \\ & 91 \end{aligned}$ | $\begin{aligned} & 74 \\ & 83 \\ & 83 \end{aligned}$ | $\begin{aligned} & 66 \\ & 70 \\ & 744 \\ & 74 \end{aligned}$ | $\left.\begin{array}{l} 59 \\ 689 \\ 60 \\ 60 \end{array}\right)$ | $\begin{aligned} & 54 \\ & 56 \\ & 58 \\ & 58 \end{aligned}$ | ¢ |  |
| 194 | 133 | 129 | 124 | 121 | 118 | 114 | 111 | 105 | ${ }^{98}$ | ${ }_{90}$ | 4 | \% | ${ }_{62}$ | ${ }_{56}^{54}$ | ${ }_{53}^{53}$ |
| ${ }_{\substack{195 \\ 196 \\ 1}}^{1}$ | 140 <br> 147 <br> 1 | 136 143 14 | 131 138 1 | ${ }^{1238}$ | ${ }^{125}$ | ${ }^{192}$ | 118 | ${ }^{113}$ | ${ }^{106}$ | 98 | 9 | , | 20 | d | 55 |
| linc |  | 143 <br> 150 <br> 157 <br> 1 | ${ }_{1}^{133} 1$ | 136 143 15 | ${ }_{\substack{133 \\ 140 \\ 148 \\ \hline \\ \\ \hline}}$ | ${ }_{\substack{130 \\ 138}}^{14}$ | 127 135 13 | ${ }_{\substack{121 \\ 131}}^{110}$ | 115 | cin | ciot | (84 | \% 78 | - 64 | ${ }^{581} 6$ |
| ${ }_{199}^{1,18}$ | $\begin{gathered} 1661 \\ \hline 168 \end{gathered}$ | 157 <br> 164 | ${ }_{150}^{153}$ | ${ }^{150} 15$ | 148 <br> 156 <br> 1 | ${ }_{154}^{146}$ | 144 <br> .152 | ${ }_{14}^{140}$ | 1 | ${ }_{134}^{194}$ | ${ }_{12}^{113}$ | ${ }_{109}^{100}$ | ${ }^{87}$ | 81 | ${ }_{6}^{65}$ |
| ${ }^{200}$ | 1738 | ${ }^{17}{ }^{174}$ | ${ }^{161}$ | ${ }^{164}$ | ${ }^{163}$ | ${ }_{161}^{167}$ | ${ }^{160}$ | ${ }^{157}$ | 151 | ${ }^{143}$ | 131 | ${ }_{117}^{127}$ | ${ }^{102}$ | 04 | \% |
| $\begin{aligned} & 2020 \\ & \hline 2020 \\ & 2020 \end{aligned}$ | $\begin{aligned} & 188 \\ & \hline 184 \\ & 184 \end{aligned}$ | $\substack{178 \\ 180}$ | ${ }_{\substack{174 \\ 176}}$ | - | 1168 <br> 174 <br> 174 <br> 1 | $\begin{aligned} & 1767 \\ & 1724 \\ & 1720 \end{aligned}$ | $\begin{aligned} & 1672 \\ & 1720 \\ & 1720 \end{aligned}$ | $\begin{gathered} 1601 \\ 1740 \\ 174 \end{gathered}$ | ${ }_{1} 171$ | $\begin{aligned} & 155 \\ & 158 \\ & 164 \end{aligned}$ | ${ }_{\substack{117 \\ 154}}$ | ${ }_{\substack{133 \\ 140}}^{14}$ | - | coid |  |
| 204 | 185 | 180 | 176 | 174 | 174 | 175 | ${ }_{176}^{172}$ | ${ }_{176}$ | 171 | ${ }^{168}$ | ${ }_{159}$ | ${ }_{146}^{140}$ | 130 | ${ }_{113}$ | ${ }^{90} 9$ |
| ${ }_{205}^{295}$ | ${ }_{184}^{184}$ | 180 <br> 178 <br> 18 | ${ }_{173}^{175}$ | ${ }^{173}$ | ${ }_{\substack{173 \\ 169}}$ |  | ${ }_{172}^{175}$ | ${ }_{1}^{174}$ | ${ }_{\substack{175 \\ 174}}^{175}$ | 171 | ${ }_{1}^{162}$ | ${ }_{\substack{151 \\ 155}}$ | ${ }_{\substack{136 \\ 1.41}}$ | $\xrightarrow{119} 1$ | ${ }_{\substack{101 \\ 107}}$ |
| $\substack{210 \\ 208 \\ 208}$ <br> 2 | $\begin{aligned} & 1888 \\ & \begin{array}{l} 182 \\ 181 \end{array} \end{aligned}$ | ${ }^{175}$ | 166 | ${ }_{160}^{165}$ | ${ }_{\substack{1 \\ 158}}^{\substack{164}}$ | ${ }_{\substack{165 \\ 160}}^{10}$ | $\begin{aligned} & 1720 \\ & 1620 \\ & 1620 \end{aligned}$ | $\begin{aligned} & 177 \\ & 1705 \\ & \hline 165 \end{aligned}$ | $\begin{aligned} & 174 \\ & 174 \\ & 167 \end{aligned}$ | $\begin{aligned} & 77170 \\ & 1707 \\ & 167 \end{aligned}$ | $\begin{aligned} & 165 \\ & 165 \\ & 364 \end{aligned}$ |  | ${ }_{\substack{144 \\ 148 \\ 148}}$ | cis | ${ }_{117}$ |
| ${ }_{209}$ | 179 | 170 | 163 | ${ }_{156}$ | ${ }_{153}$ | ${ }_{153}$ | ${ }_{155}^{150}$ | ${ }_{159}$ | 162 | 164 | ${ }_{162}$ | 157 | ${ }_{148}$ | ${ }_{136}^{133}$ | ${ }_{127}^{127}$ |
| ${ }_{211}^{210}$ | $\underset{\substack{178 \\ 178}}{ }$ | ${ }_{1}^{168}$ | $\underbrace{}_{\substack{159 \\ 1.78}}$ | ${ }_{149}^{159}$ | $1 \begin{aligned} & 148 \\ & 148 \\ & 1\end{aligned}$ |  | 1149 <br> 142 <br> 1 | ${ }_{\substack{153 \\ 146}}$ | ${ }_{\substack{156 \\ 150}}$ | $\xrightarrow{159}$ | ${ }_{1}^{155}$ |  | 148 <br> 148 |  | $\underset{\substack{124 \\ 126}}{\substack{2 \\ \hline}}$ |
| 2112 | (180 | $\underset{\substack{167 \\ 169}}{160}$ | ${ }_{\substack{156 \\ 157}}^{15}$ | 146 <br> 146 <br> 146 | $\begin{aligned} & 144 \\ & \hline 140 \\ & 140 \end{aligned}$ | $\begin{aligned} & 142 \\ & \left.\begin{array}{l} 132 \\ 130 \end{array}\right) \end{aligned}$ | $\begin{aligned} & 139 \\ & 348 \\ & 134 \end{aligned}$ | $\begin{gathered} 146 \\ 1414 \\ 136 \end{gathered}$ | $\begin{aligned} & 15050 \\ & 1405 \\ & 140 \end{aligned}$ | $\begin{aligned} & 1545 \\ & 1414 \\ & 143 \end{aligned}$ |  | $\begin{aligned} & 1530 \\ & 158 \\ & 148 \end{aligned}$ | $\substack{146 \\ 144 \\ 144}_{\substack{\text { a }}}$ | $\substack{\begin{subarray}{c}{138 \\ 135} }} \\{135} \end{subarray}$ |  |
| 214 | 186 | 172 | 163 | 148 | 13.9 | 134 | ${ }_{1}^{132}$ | ${ }_{133}$ | ${ }_{137}$ | 141 | 144 | 145 | 143 | 137 | 128 |
| 215 216 | ${ }_{\substack{199 \\ 196}}$ | ${ }_{\substack{177 \\ 183}}$ | $\substack{164 \\ 170}_{\substack{164}}$ | ${ }_{1}^{157}$ | 1142 <br> 148 <br> 1 | 136 <br> 139 |  | (133 |  |  |  |  |  |  | ${ }_{\text {ce }}^{\substack{29 \\ 29}}$ |
| 2.27 <br> 218 <br> 18 |  | $\xrightarrow{190} 1$ | ${ }_{1}^{187}$ | ${ }_{\substack{176 \\ 172}}^{\substack{19 \\ 1}}$ | , | (195 | $\begin{aligned} & 130 \\ & 146 \\ & 146 \end{aligned}$ | $\underset{\substack{134 \\ 143}}{\substack{143}}$ | (1438 | $\begin{aligned} & 138 \\ & 143 \\ & 143 \end{aligned}$ | ${ }_{145}^{142}$ | ${ }_{143}^{143}$ | ${ }_{1}^{141} 1$ | $\substack{1.137 \\ 139}$ | 131 |
| 219 | 213 | 204 | 193 | 131 | 170 | 163 | ${ }_{154}^{146}$ | ${ }_{150} 14$ | 149 | ${ }_{148}$ | ${ }_{140}$ | 149 | ${ }_{146}^{14}$ | 142 | ${ }_{135}$ |
| ${ }^{292}$ | $\substack{217 \\ 2020}^{21}$ | 210 215 | ${ }_{\substack{299 \\ 297}}$ | $1 \begin{aligned} & 189 \\ & 197\end{aligned}$ | ${ }_{187}^{173}$ | ${ }_{\substack{169 \\ 178}}$ | ${ }_{\substack{162 \\ 171}}$ | 158 166 1 |  | ${ }_{\substack{155 \\ 152}}^{1}$ |  |  |  | 147 | ${ }_{4}^{39}$ |
|  |  |  | ¢ 212 | 2274 | $\begin{aligned} & 1875 \\ & \begin{array}{l} 1825 \end{array}, ~ \end{aligned}$ | $\begin{gathered} 186 \\ 193 \\ 180 \end{gathered}$ | $\begin{aligned} & 1780 \\ & \hline 187 \\ & 187 \end{aligned}$ | ${ }^{1185}$ | $\xrightarrow[\substack{172 \\ 181}]{1}$ | $\begin{gathered} 1972 \\ 1727 \\ 172 \end{gathered}$ | ${ }_{\substack{17 \\ 178 \\ 170}}$ | $\begin{aligned} & 16169 \\ & 1880 \\ & 180 \end{aligned}$ | ${ }_{1}^{156}$ | $\underset{\substack{191 \\ 171}}{171}$ | ${ }_{163}$ |
| ${ }^{29} 4$ | 219 | 220 | 217 | 212 | 205 | ${ }_{1} 199$ | ${ }^{194}$ | 190 | 188 | 187 | 187 | 187 | 185 | 181 | 174 |
| ${ }_{2}^{208}$ | ${ }_{210}^{215}$ | ${ }_{218}^{218}$ | 217 218 | 213 211 | ${ }_{288}^{238}$ | ${ }_{204}^{202}$ | ${ }_{201}^{198}$ | ${ }_{199}^{195}$ |  |  |  |  |  |  | $\underbrace{\substack{\text { 2 }}}_{\substack{186 \\ 1 \% 8}}$ |
| $\xrightarrow{329}$ | 202 194 104 | cos | ${ }_{203}^{209}$ | $c208201$ | 206 | $\begin{aligned} & 20,30 \\ & 2020 \\ & 2001 \end{aligned}$ | $\begin{aligned} & 2010 \\ & 2010 \\ & 2001 \end{aligned}$ | ${ }_{201}^{201}$ | - | 220 213 |  | $\begin{aligned} & 201 \\ & 2011 \\ & 2017 \end{aligned}$ | 213 | 213 | ${ }_{\substack{209 \\ 202}}$ |
| 229 | 184 | 192 | 195 | 197 | 197 | 196 | 197 | 199 | 293 | 218 | 915 |  | ${ }^{236}$ | 230 | 329 |
| ${ }_{231}^{230}$ | ${ }_{1}^{174}$ | - | ${ }_{187}^{187}$ | 18 | ${ }_{182}^{190}$ | ${ }_{1}^{190}$ | ${ }_{1}^{196}$ | ${ }_{\substack{195 \\ 190}}^{19}$ | ${ }^{290}$ |  |  |  | ${ }_{231}^{231}$ | -333 | ${ }_{24}^{237}$ |
| - | $\underset{\substack{153 \\ 142}}{ }$ | ${ }_{\substack{161 \\ 151}}$ | $\begin{gathered} 1,67 \\ 1,62 \end{gathered}$ | (1720 | $\begin{aligned} & 1783 \\ & \hline 196 \\ & \hline 169 \end{aligned}$ | $\begin{aligned} & 1785 \\ & \hline 167 \\ & \hline 167 \end{aligned}$ | (178 | ${ }^{138}$ | cos | (192 | $\begin{aligned} & 214 \\ & 210 \\ & 204 \end{aligned}$ | 215 | ${ }^{207}$ | $\underset{\substack{239 \\ 239}}{\text { 23, }}$ | ${ }_{24}$ |
| 234 | 131 | 140 | ${ }^{44}$ | 152 | ${ }^{155}$ | 158 | 161 | 167 | 174 | 184 | 196 | 209 | 221 | 23.2 | 240 |
| $\underset{236}{238}$ | ${ }^{190}$ | ${ }^{130}$ | ${ }_{\substack{137 \\ 127}}^{18}$ | ctis |  | 148 139 | ${ }_{142}^{152}$ |  | ${ }_{\substack{165}}^{155}$ | ${ }_{\substack{175 \\ 163}}$ |  | 200 |  |  | ${ }^{2}$ |
|  | - $\begin{gathered}99 \\ 89 \\ 89\end{gathered}$ | (109 | ${ }_{\substack{117 \\ 107}}^{102}$ | 12913 |  | ${ }^{139}$ |  | ${ }_{\substack{137 \\ 127}}^{1}$ | (194 | ck | ${ }_{\substack{165 \\ 103}}^{163}$ | 178 166 168 | cin | cis |  |
|  | $\stackrel{80}{71}$ | ${ }_{8}^{89} 8$ | ${ }_{88}^{97}$ | (103 | ${ }_{107}^{107}$ | 110 100 |  |  |  |  | ci10 | (153 | ${ }_{\substack{166 \\ 153}}$ | ${ }_{165}^{173}$ | ${ }_{177}^{191}$ |


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$\therefore$ dd 19.6 to Arg. XII. when $224^{4} .7$ is subtracted from Arg. I.

|  |  | Perturbations of the Longilude by Jupiter. <br> Horizontal Argument $=1$. <br> onstant added $2^{\prime \prime} .35$. <br> P'eriod of Argument I. |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Arg. } \\ & \text { XIII. } \end{aligned}$ | ${ }^{\text {d }}$ | ${ }_{8}^{8}$ | $\stackrel{4}{16}$ | ${ }_{2}^{d}$ | $\mathbf{B}^{\mathrm{d}}$ | ${ }_{40}^{d}$ | $48$ | $\stackrel{d}{56}$ | $61$ | ${ }_{y}^{d}$ | ${ }_{80}^{d}$ | ${ }_{8}^{\mathrm{d}} 8$ | $\stackrel{d}{96}$ | $\stackrel{d}{101}$ | $119$ |
| 0 | 205 | 209 | 216 | 226 | 237 | 248 | 259 | 268 | 235 | 278 | 230 | 279 | $2 \%$ | 271 | 263 |
| 1 | 185 | 184 | 188 | 194 | 204 | 211 | 296 | 236 | 245 | 253 | 257 | $25!$ | 2.8 | 256 | 25.4 |
| 3 | 169 | 164 | 163 | 166 | 173 | 102 | 192 | 204 | 215 | 224 | 231 | 2.37 | 239 | 240 | 238 |
| 3 | 158 | 147 | 1.12 | 111 | 144 | 151 | 160 | 171 | 183 | 194 | 204 | $\stackrel{212}{12}$ | 218 | 221 | $2 \% 2$ |
| 4 | 150 | 136 | $1 \div 6$ | 121 | 120 | 193 | 130 | 140 | 1.51 | 163 | 175 | 186 | 195 | 201 | 204 |
| 5 | 145 | 108 | 115 | 105 | 100 | 100 | 104 | 111 | 121 | 133 | 146 | 155 | 1.0 | 179 | 18.5 |
| 6 | 143 | 125 | 108 | 95 | 86 | 82 | 8: | 86 | 94 | 104 | 117 | $1: 31$ | 144 | 156 | 161 |
| 7 | 143 | 123 | 105 | 89 | 77 | 63 | 6.1 | 65 | 70 | 79 | 90) | 10.1 | 118 | $13:$ | 143 |
| 8 | 143 | 194 | 105 | 87 | 72 | 61 | 53 | 50 | 52 | 57 | 67 | 79 | 93 | 108 | 121 |
| 9 | 143 | 126 | 108 | 89 | 72 | 58 | 47 | 40 | 38 | 40 | 47 | 58 | 71 | 85 | 100 |
| 10 | 142 | 123 | 111 | 93 | 75 | 59 | 46 | 36 | 30 | 29 | 32 | 40 | 51 | 65 | 79 |
| 11 | 140 | 129 | 115 | 99 | 81 | 65 | $4!$ | 37 | 28 | 23 | 23 | 2\% | 36 | 47 | 61 |
| 12 | 136 | 129 | 119 | 10.5 | 89 | 73 | 57 | 42 | 31 | 23 | 1!) | 20 | 25 | 34 | 45 |
| 13 | 1310 | 123 | 121 | 111 | 98 | 83 | 67 | 59 | 38 | 28 | 21 | 18 | 19 | 25 | 34 |
| 14 | 121 | 125 | 122 | 116 | 106 | 94 | 79 | 6.1 | 50 | 37 | $\underline{37}$ | 21 | 19 | 21 | 27 |
| 15 | 116 | 123 | 129 | 120 | 114 | 105 | 99 | 78 | 64 | 50 | 38 | 29 | 24 | 22 | 24 |
| 16 | 109 | 115 | 120 | 122 | 120 | 115 | 106 | 94 | 80 | 66 | 53 | 42 | 34 | 28 | 27 |
| 17 | 102 | 110 | 117 | 123 | 125 | 124 | 119 | 109 | 98 | 85 | 71 | 58 | 48 | 40 | 35 |
| 18 | 96 | 105 | 114 | 192 | 129 | 131 | 130 | 124 | 116 | 104 | 91 | 73 | 65 | 55 | 47 |
| 19 | 92 | 101 | 111 | 122 | 131 | 137 | 140 | 138 | 133 | 12.1 | 112 | 99 | 85 | 73 | 63 |
| 20 | 91 | 99 | 107 | 121 | 132 | 142 | 149 | 151 | 149 | 142 | 133 | 121 | 108 | 91 | 82 |
| 21 | 92 | 99 | 108 | 120) | 13:3 | 146 | 156 | 161 | 163 | 160 | $15: 3$ | 143 | 131 | 117 | 104 |
| 22 | 95 | 101 | 109 | 121 | 135 | 149 | 161 | 170 | 176 | 177 | 173 | 16.5 | 154 | 141 | 123 |
| 23 | 100 | 105 | 112 | $12!3$ | 136 | $1: 1$ | 166 | 178 | $18 \%$ | $1!1$ | 190 | 186 | 177 | 16 | 172 |
| 24 | 108 | 111 | 118 | 127 | 139 | 154 | 170 | 184 | 196 | 204 | 206 | 205 | 199 | 189 | 177 |
| 2.) | 117 | 120 | 125 | 133 | 144 | 158 | 1\%4 | 190 | 203 | 214 | 220 | 299 | 219 | 211 | 201 |
| 26 | 128 | 130 | 134 | 141 | 150 | 16.3 | 178 | 194 | 210 | 223 | 232 | 237 | 237 | 238 | 294 |
| 27 | 139 | 14: | 145 | 151 | 159 | 170 | 184 | 199 | 215 | 230 | 2.11 | 2919 | 259 | 251 | 24.5 |
| 23 | 151 | 155 | 158 | 16.3 | 16.) | 178 | 190 | 205 | 220 | 236 | 349 | 260 | 266 | 267 | 264 |
| 23 | 164 | 168 | 171 | 175 | 180 | 188 | 193 | 211 | 926 | 241 | 255 | 268 | 9\%7 | 291 | 281 |
| 30 | 177 | 181 | 185 | 189 | 194 | 199 | 207 | 218 | 231 | 246 | 261 | 974 | 285 | 292 | 296 |
| 31 | 190 | 196 | 200 | 204 | 203 | 21\% | 218 | 297 | 238 | 251 | 265 | 279 | 291 | 301 | 307 |
| 32 | 20.4 | 210 | 215 | $21!$ | 2022 | 220 | 230 | 237 | 245 | 256 | 269 | 283 | 296 | 307 | 316 |
| 33 | 219 | 2 2 1 | 299 | 234 | 237 | 210 | 243 | 248 | 204 | 263 | 273 | 286 | 299 | 311 | $3: 2$ |
| 3.1 | 235 | 239 | 214 | 249 | 259 | 255 | 2.7 | 260 | 264 | 270 | 278 | 289 | 301 | 314 | 3326 |
| 35 | 2.1 | 2.54 | 259 | 263 | 267 | 269) | 271 | 273 | 275 | 278 | 284 | 292 | 303 | 315 | 327 " |
| 36 | 26 | $2 \% 0$ | 274 | 278 | 281 | 234 | 286 | 286 | 237 | 288 | 291 | 297 | 305 | 315 | $3: 7$ |
| 37 | 287 | 238 | $\stackrel{39}{3}$ | 292 | 296 | 298 | 300 | 300 | 299 | 299 | 299 | 302 | 307 | \$16 | 396 |
| 38 | 306 | 304 | 305 | 306 | 309 | 311 | 313 | 313 | \$1 | 310 | 308 | 304 | 311 | 316 | 39.5. |
| 33 | 326 | 322 | 321 | 321 | 32\% | 324 | 395 | 325 | 324 | 321 | 318 | 316 | 316 | 318 | 324 |
| 40 | 346 | 341 | 3.37 | 395 | 335 | 336 | 337 | 337 | 336 | 333 | 328 | 324 | 321 | 321 | 32.1 |
| 41 | 366 | 3.5 | 354 | 350 | 348 | 347 | 348 | 348 | 346 | 343 | 339 | 3:33 | 329 | 3\% | 325 |
| 42 | $3 \geq 6$ | 378 | 370 | 36.5 | 361 | 338 | 358 | 3 3\% | 356 | $35 \%$ | 343 | 343 | 336 | 331 | 327 |
| 43 | 405 | 396 | 387 | 379 | 373 | 363 | 367 | 366 | 364 | 362 | 325 | 351 | 344 | 337 | 331 |
| 44 | 492 | 413 | 403 | 394 | $3 \div 6$ | 380 | 375 | 373 | 371 | 369 | 365 | 359 | 352 | 344 | 336 |
| 45 | 436 | 428 | 418 | 408 | 398 | 390 | 383 | 330 | 376 | $3{ }^{38}$ | 371 | 366 | 3.9 | 3.1 | 341 |
| 46 | 443 | 440 | 431 | 420 | 409 | $39 \%$ | 391 | 384 | 381 | 378 | 375 | 371 | 36.5 | 357 | 347 |
| 47 | 454 | 4.0 | 441 | $4: 31$ | 419 | 408 | 398 | 390 | 344 | 381 | 378 | 371 | 369 | 36 | 33.3 |
| 43 | 457 | 453 | 449 | $43!9$ | 423 | 41.5 | 404 | 39.4 | :387 | 382 | 378 | 37.5 | 371 | 365 | 3,\% |
| 49 | 455 | 456 | $45: 2$ | 4.14 | 433 | 421 | 409 | 398 | 388 | 38.2 | 378 | 374 | 371 | 367 | 369 |
| 50 | 448 | 409 | 451 | 446 | 436 | 425 | 412 | 400 | 389 | 351 | 376 | 3\%2 | 369 | 366 | 361 |
| 51 | 436 | 4.13 | 44.5 | 443 | 4:5 | 426 | $41: 1$ | 401 | 359 | 330 | 373 | 368 | 365 | 36:3 | 3-! |
| 59 | 419 | 429 | $4: 34$ | 434 | 430 | 42.3 | 412 | 400 | 393 | 377 | 369 | 363 | 360 | 358 | 3\% |
| 53 | 397 | 410 | 418 | 421 | 421 | 416 | 407 | $3!16$ | 384 | 373 | 36.4 | 3.7 | 353 | 350 | 319 |
| 54 | 372 | 386 | 397 | 404 | 406 | 404 | 398 | 389 | 378 | 368 | 358 | 350 | 34.5 | 349 | 341 |
| 55 | 344 | 369 | 372 | 381 | 386 | 323 | 385 | 379 | 370 | 360 | 351 | 312 | 336 | 332 | 331 |
| 56 | 31.5 | $3: 9$ | 31.3 | 354 | $30^{\circ} \mathrm{F}$ | 367 | 368 | 36.5 | 3.9 | 3.0 | 3.11 | 3:31 | 326 | $32 \%$ | 320 |
| 57 | 28. | 298 | 3115 | 134 | 335 | 312 | 346 | 346 | 343 | $3: 37$ | 330 | $3 \cup 3$ | 315 | 310 | 307 |
| 58 | 2006 | 267 | 27.9 |  | 304 | 31.3 | 320 | 324 | $3 \because 4$ | 321 | 316 | 310 | 304 | 298 | 29\% |
| 59 | 9! ${ }^{2}$ | $6: 37$ | 9.17 | 20,9 | 231 | 281 | 291 | 9.17 | 301 | 301 | 299 | 296 | 290 | 28.5 | 28.2 |
| 69 | 205 | 203 | 216 | 296 | 237 | 288 | 259 | 263 | $2 \%$ | 275 | 250 | $28!$ | 276 | 271 | 268 |



11 V

Perturbations of the Longitude by Saturn.
Ilorizontal Argument $=1$.
Constant added $0^{\prime \prime} .40$.
Period of Argument 1., $294^{\mathrm{d} .7}$.

| $\stackrel{\text { Arcr. }}{\mathrm{XiV}}$ | ${ }_{0}^{\text {d }}$ | $\begin{aligned} & \mathrm{d} \\ & 8 \end{aligned}$ | $16$ | $84$ | $3 \underset{8}{\mathbf{2}}$ | $40$ | $\begin{array}{r} 1 \\ 48 \\ 48 \end{array}$ | $56^{d}$ | $6{ }^{4}$ | ${ }^{\mathrm{d}}$ | $80$ | $88$ | $96$ | $10 d^{d}$ | $18{ }^{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 39 | 43 | 47 | 54 | 60 | 66 | 72 | 77 | 80 | 81 | 81 | 80 | 78 | 75 | \% |
| 1 | 37 | 39 | 43 | 48 | 5.1 | 61 | 67 | 79 | 77 | 79 | 80 | 80 | 79 | 76 | 74 |
| 2 | 36 | 36 | 39 | 43 | 48 | 54 | 61 | 67 | 72 | 76 | 78 | 79 | 78 | 77 | i4 |
| 3 | 36 | 35 | 35 | 38 | 42 | 47 | 54 | 60 | 66 | 71 | 75 | 77 | 77 | 76 | 74 |
| 4 | 36 | 34 | 33 | 34 | 36 | 40 | 46 | 52 | 59 | 6.1 | 69 | 73 | 34 | 75 | 73 |
| 5 | 37 | 34 | 31 | 30 | 31 | 34 | 39 | 44 | 51 | 57 | 63 | 67 | 70 | 71 | 71 |
| 6 | 38 | 34 | 31 | 28 | 28 | 29 | 32 | 37 | 42 | 49 | 55 | 60 | 65 | 67 | 68 |
| 7 | 38 | 34 | 31 | 27 | 25 | 25 | 97 | 30 | 34 | 40 | 46 | 52 | 58 | 62 | 64 |
| 8 | 38 | 34 | 31 | 27 | 2.1 | 22 | 22 | 24 | 27 | 33 | 38 | 44 | 50 | 55 | 59 |
| 9 | 37 | 34 | 31 | 27 | 23 | 21 | 19 | 19 | 21 | 25 | 30 | 35 | 42 | 47 | 52 |
| 10 | 35 | 33 | 30 | 26 | 23 | 19 | 17 | 16 | 16 | 18 | 22 | 27 | 33 | 39 | 45 |
| 11 | 33 | 31 | 29 | 26 | 22 | 19 | 16 | 14 | 13 | 14 | 16 | 20 | 95 | 31 | 37 |
| 12 | 30 | 29 | 27 | 25 | 22 | 19 | 15 | 12 | 11 | 10 | 11 | 14 | 18 | 24 | 29 |
| 13 | 27 | 9 | 25 | 23 | 21 | 18 | 15 | 12 | 9 | 8 | 8 | 3 | 12 | 17 | 22 |
| 14 | 25 | 94 | צ3 | 29 | 20 | 18 | 15 | 12 | 9 | 7 | 6 | 6 | 8 | 11 | 16 |
| 15 | 23 | 2: | 21 | 20 | 19 | 17 | 15 | 12 | 9 | 7 | 5 | 4 | 5 | 7 | 11 |
| 16 | 23:3 | 21 | 20 | 19 | 18 | 16 | 15 | 13 | 10 | 8 | 5 | 4 | 3 | 4 | 7 |
| 17 | 24 | 21 | 19 | 18 | 17 | 16 | 15 | 13 | 11 | 8 | 6 | 4 | 3 | 3 | 4 |
| 18 | 26 | 23 | 20 | 19 | 17 | 16 | 15 | 13 | 12 | 10 | 7 | 5 | 4 | 3 | 3 |
| 19 | 29 | 26 | 23 | 20 | 19 | 17 | 16 | 15 | 13 | 11 | 9 | 7 | 5 | 4 | 3 |
| 20 | 33 | 30 | 26 | 23 | 21 | 19 | 18 | 16 | 15 | 13 | 11 | 9 | 7 | 5 | 1 |
| 21 | 38 | 34 | 31 | 27 | 25 | 22 | 20 | 19 | 17 | 16 | 14 | 12 | 10 | 8 | 6 |
| 23 | 42 | 39 | 36 | 32 | 29 | 96 | 24 | 22 | $\because 0$ | 19 | 17 | 15 | 13 | 11 | 9 |
| 23 | 46 | 44 | 42 | 38 | 35 | 32 | 29 | 27 | 24 | 22 | 21 | 19 | 17 | 15 | 13 |
| 24 | 50 | 50 | 47 | 44 | 41 | 38 | 34 | 32 | 29 | 27 | 25 | 23 | 21 | 19 | 17 |
| 25 | 54 | 54 | 53 | 50 | 47 | 44 | 41 | 38 | 35 | 32 | 30 | 28 | 26 | 24 | 22 |
| 26 | 56 | 58 | 57 | 56 | 54 | 51 | 47 | 44 | 41 | 38 | 36 | 34 | 31 | 29 | 27 |
| 27 | 58 | 60 | 61 | 61 | 59 | 57 | 54 | 51 | 48 | 44 | 42 | 39 | 37 | 35 | 32 |
| 28 | 58 | 62 | 64 | 65 | 65 | 63 | 60 | 57 | 54 | 51 | 48 | 45 | 43 | 41 | 38 |
| 99 | 58 | 63 | 66 | 68 | 69 | 68 | 66 | 63 | 60 | 57 | 54 | 51 | 49 | 47 | 44 |
| 30 | 57 | 62 | 67 | 70 | 72 | 72 | 71 | 69 | 66 | 63 | 60 | 57 | 55 | 52 | 50 |
| 31 | 54 | 61 | 66 | 70 | 73 | 75 | 75 | 74 | 71 | 69 | 66 | 63 | 60 | 57 | 55 |
| 32 | 52 | 58 | 64 | 69 | 7.4 | 76 | 77 | 77 | 76 | 73 | 71 | 68 | 65 | 62 | 60 |
| 33 | 48 | 55 | 61 | 67 | 72 | 76 | 79 | 79 | 79 | 77 | 75 | 72 | 69 | 67 | 64 |
| 34 | 45 | 51 | 57 | 6.1 | 69 | 34 | 78 | 80 | 81 | 80 | 78 | 76 | 73 | 70 | 68 |
| 35 | 42 | 47 | 52 | 59 | 65 | 71 | 76 | 79 | 81 | 81 | 80 | 78 | 76 | 73 | 70 |
| 36 | 39 | 43 | 47 | 5.1 | 60 | 66 | 72 | 77 | 80 | 81 | 81 | 80 | 78 | 75 | 72 |

The perturbations are expressed in hundredths of a second of arc.

| - | Perturbations of the Longitude by Saturn. <br> Horizontal Argument $=\mathbf{I}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Constant added $0^{\prime \prime} .40$. |  |  |  |  |  |  | Period of Argument XIV., 36 units. |  |  |  |  |  |  |  |
| $\begin{aligned} & \text { Arg. } \\ & \text { XIV. } \end{aligned}$ | $120^{\text {d }}$ | $1.28{ }^{\text {d }}$ | $13{ }^{\text {d }}$ | $14{ }^{\text {d }}$ | $15{ }^{\text {d }}$ | $160^{\text {d }}$ | $169^{\text {d }}$ | 176 | $184{ }^{\text {d }}$ | $1.92$ | $200^{d}$ | $2{ }^{\mathrm{d}}$ | $216^{\mathrm{d}}$ | 224 | $23{ }^{\text {d }}$ |
| 0 | 70 | 68 | 66 | 63 | 61 | 59 | 56 | 52 | 48 | 45 | 41 | 38 | 37 | 37 | 40. |
| 1 | 71 | 69 | 67 | 65 | 63 | 61 | 58 | 55 | 51 | 47 | 44 | 40 | 38 | 36 | 37 |
| 2 | 72 | 69 | 67 | 65 | 63 | 61 | 59 | 57 | 54 | 50 | 46 | 43 | 39 | 36 | 35 |
| 3 | 72 | 69 | 67 | 64 | 63 | 61 | 59 | 57 | 55 | 52 | 48 | 44 | 40 | 36 | 34 |
| 4 | 71 | 69 | 66 | 64 | 62 | 60 | 58 | 57 | 55 | 52 | 49 | 45 | 41 | 37 | 34 |
| 5 | 70 | 68 | 65 | 62 | 60 | 58 | 56 | 55 | 53 | 52 | 49 | 46 | 42 | 38 | 34 |
| 6 | 68 | 66 | 64 | 61 | 58 | 56 | 54 | 53 | 51 | 50 | 48 | 46 | 42 | 39 | 35 |
| 7 | 65 | 64 | 62 | 59 | 57 | 54 | 52 | 50 | 48 | 47 | 46 | 44 | 42 | 38 | 35 |
| 8 | 60 | 61 | 60 | 58 | 55 | 52 | 49 | 47 | 46 | 44 | 43 | 42 | 40 | 38 | 34 |
| 9 | 55 | 57 | 57 | 55 | 53 | 50 | 47 | 45 | 43 | 41 | 40 | 39 | 38 | 36 | 34 |
| 10 | 49 | 52 | 53 | 53 | 51 | 49 | 46 | 43 | 40 | 38 | 37 | 36 | 35 | 34 | 32 |
| 11 | 42 | 46 | 49 | 50 | 49 | 47 | 45 | 42 | 38 | 36 | 34 | 33 | 31 | 31 | 29 |
| 12 | 35 | 40 | 44 | 46 | 47 | 46 | 44 | 41 | 38 | 35 | 32 | 30 | 28 | 28 | 27 |
| 13 | 28 | 33 | 38 | 42 | 43 | 44 | 43 | 40 | 37 | 34 | 31 | 29 | 27 | 26 | 24 |
| 14 | 21 | 27 | 32 | 37 | 40 | 41 | 41 | 40 | 37 | 34 | 3 | 28 | 25 | 24 | 23 |
| 15 | 15 | 21 | 27 | 32 | 36 | 39 | 40 | 39 | 38 | 35 | 32 | 28 | 25 | 23 | 21 |
| 16 | 11 | 16 | 21 | 27 | 32 | 36 | 38 | 39 | 38 | 36 | 33 | 30 | 27 | 24 | 22 |
| 17 | 7 | 11 | 16 | 22 | 28 | 32 | 36 | 38 | 39 | 38 | 35 | 32 | 20 | 26 | 23 |
| 18 | 5 | 8 | 13 | 18 | 23 | 29 | 33 | 37 | 38 | 39 | 37 | 35 | 32 | 29 | 25 |
| 19 | 4 | 6 | 10 | 15 | 20 | 25 | 31 | 35 | 38 | 40 | 40 | 38 | 36 | 32 | 29 |
| 20 | 4 | 6 | 8 | 12 | 17 | 23 | 28 | 33 | 38 | 40 | 41 | 41 | 40 | 37 | 33 |
| 21 | 6 | 6 | 8 | 11 | 15 | 20 | 26 | 32 | 37 | 40 | 43 | 44 | 43 | 41 | 38 |
| 22 | 8 | 8 | 9 | 11 | 14 | 19 | 24 | 30 | 35 | 40 | 44 | 46 | 47 | 45 | 43 |
| 23 | 11 | 10 | 10 | 12 | 14 | 18 | 23 | 28 | 34 | 39 | 44 | 47 | 49 | 49 | 48 |
| 24 | 15 | 13 | 13 | 13 | 15 | 18 | 22 | 27 | 33 | 39 | 44 | 48 | 51 | 53 | 53 |
| 25 | 19 | 17 | 16 | 16 | 16 | 18 | 22 | 26 | 32 | 38 | 43 | 49 | 53 | 55 | 56 |
| 26 | 24 | 22 | 20 | 19 | 19 | 20 | 22 | 26 | 31 | 36 | 43 | 48 | 53 | 57 | 59 |
| 27 | 30 | 27 | 25 | 23 | 22 | 42 | 23 | 26 | 30 | 35 | 41 | 47 | 53 | 58 | 61 |
| 28 | 35 | 33 | 30 | 28 | 26 | 25 | 25 | 27 | 30 | 34 | 40 | 46 | 52 | 58 | 62 |
| 29 | 41 | 39 | 36 | 33 | 30 | 29 | 28 | 28 | 30 | 34 | 38 | 44 | 50 | 57 | 62 |
| 30 | 47 | 44 | 41 | 38 | 35 | 33 | 31 | 30 | 31 | 33 | 37 | 42 | 48 | 55 | 60 |
| 31 | 53 | 50 | 47 | 44 | 41 | 38 | 35 | 33 | 33 | 34 | 36 | 40 | 46 | 52 | 58 |
| 32 | 57 | 55 | 52 | 49 | 46 | 42 | 39 | 36 | 35 | 34 | 36 | 39 | 43 | 49 | 55 |
| 33 | 63 | 60 | 57 | 54 | 51 | 47 | 44 | 40 | 38 | 36 | 36 | 37 | 41 | 45 | 51 |
| 34 | 65 | 63 | 61 | 58 | 55 | 52 | 48 | 45 | 41 | 39 | 37 | 37 | 39 | 42 | 47 |
| 35 | 68 | 66 | 64 | 61 | $59^{*}$ | 56 | 53 | 49 | 45 | 41 | 39 | 37 | 38 | 39 | 43 |
| 36 | 70 | 68 | 66 | 63 | 61 | 59 | 56 | 52 | 48 | 45 | - 41 | 38 | 37 | 37 | 40 |

Add 0.8 to Arg. XIV. when $224^{\mathrm{d}} .7$ is subtracted from Arg. I.

## TABLE XXVI.

| Logarithm of the Elliptic Radius Vector for nad $=0$. Constant subtracted 0.0000257 . Period of Argument I. $2244^{4} .5008$ |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Arg. 1. | 0.0 | 9. ${ }^{\text {a }}$ | 0.2 | 0.8 | 0. 1 | 0.6 | 0.6 | 0.8 | 0.8 | 0.3 | $\begin{aligned} & \text { Diff. } \\ & \text { for } 0^{\mathrm{d}} .1 . \end{aligned}$ |
| ${ }_{0}^{14}$ | 9.8563298 | 63298 | 63298 | 63299 | 63300 | 63301 | 63302 | 633304 | 63305 | 63307 | +1 |
| 1 | 63310 | 68312 | 63315 | 63:318 | 6:3321 | $63: 321$ | 683328 | 633332 | 63336 | 63341 | 4 |
| 2 | $6: 3345$ | 63350 | 93355 | 63360 | $6: 3366$ | 6337: | 63378 | 63381 | 633391 | 63397 | 6 |
| 3 | 63404 | 63412 | 63419 | 63427 | 63135 | 63443 | 63451 | 63460 | 63169 | 63478 | 8 |
| 4 | 63487 | 63197 | 63507 | 63517 | 63527 | 63538 | 63518 | 63559 | 63571 | 63582 | 11 |
| 5 | 63594 | 63606 | $6: 3618$ | 63630 | $6: 3643$ | 63656 | 63669 | 6368: | 63696 | 63710 | 13 |
| 6 | 63724 | 63738 | 6375: | 63767 | $6: 3782$ | 63797 | 63813 | 63828 | 63814 | 63860 | 15 |
| 7 | 63877 | 63893 | 63910 | 63927 | 63945 | 63962 | 63980 | 63998 | 64016 | 64035 | 18 |
| 8 | 64053 | 64072 | 64092 | 64111 | 64131 | 64150 | 64171 | 64191 | 64211 | 64232 | 20 |
| 9 | 64253 | 64274 | 64296 | 61317 | 64339 | 64362 | 64381 | 64407 | 64129 | 64452 | 22 |
| 10 | 64476 | 64499 | 64523 | 64547 | 64571 | 64595 | 64620 | 64645 | 64670 | 64695 | 25 |
| 11 | 64721 | 64747 | 64773 | 64799 | 64825 | 64852 | 64879 | 64906 | 64933 | 64961 | 27 |
| 12 | 64989 | 65017 | 65045 | 65073 | 65102 | 65131 | 65160 | 65189 | 65219 | 65249 | 29 |
| 13 | 65279 | 65309 | 65340 | 65370 | 65401 | 65432 | 65464 | 65495 | 65527 | 65559 | 31 |
| 14 | 65591 | 65024 | 65656 | 65689 | 65722 | 65756 | 65789 | 65823 | 65857 | 65891 | 33 |
| 15 | 65925 | 65960 | 65995 | 66030 | 66065 | 66100 | 66136 | 66172 | 66208 | 66244 | 36 |
| 16 | 66281 | 66318 | 66354 | 66392 | 66429 | 66467 | 66504 | 66542 | 66581 | 66619 | 38 |
| 17 | 66658 | 66697 | 66736 | 66775 | 66814 | 66854 | 66894 | 66934 | 66974 | 67015 | 40 |
| 18 | 67055 | 67096 | 67137 | 67179 | 67220 | 67262 | 67304 | 67346 | 67388 | 67431 | 42 |
| 19 | 67474 | 67517 | 67560 | 67603 | 67647 | 67691 | $67 \% 34$ | 67779 | 67823 | 67868 | 44 |
| 20 | 67912 | 67957 | 68002 | 68048 | 68093 | 68139 | 68185 | 68231 | 68278 | 68324 | 46 |
| 21 | 68371 | 68418 | 68465 | 68512 | 68560 | 68609 | 68656 | 68704 | 68752 | 68800 | 48 |
| 22 | 68849 | 68898 | 68947 | 68996 | 69046 | 69095 | 69145 | 69195 | 69245 | 69296 | 50 |
| 23 | 69346 | 69397 | 69448 | 69499 | 69550 | 69602 | 69654 | 69706 | 69758 | 69810 | 52 |
| 24 | 69862 | 69915 | 69968 | 70021 | 70074 | 70127 | 70181 | 70234 | 70288 | 70342 | 53 |
| 25 | 70396 | 70451 | 70505 | 70560 | 70615 | 70670 | 70726 | 70781 | 70837 | 70893 | 55 |
| 26 | 70949 | 71005 | 71061 | 71118 | 71174 | 71231 | 71288 | 71345 | \%1403 | 71460 | 57 |
| 27 | 71518 | 71576 | 71634 | 71692 | 71751 | 71809 | 71868 | 71927 | 71986 | 72045 | 59 |
| 28 | 72105 | 72164 | $7 \times 224$ | 72284 | 72344 | 72404 | 72464 | 72525 | 72586 | 72616 | 60 |
| 29 | 72707 | 72769 | 72830 | 72891 | 72953 | 73015 | .73077 | 73139 | 73201 | 73864 | 62 |
| 30 | 73326 | 73389 | 73452 | 73515 | 73578 | 73612 | 73705 | 73769 | 73833 | 73897 | 63 |
| 31 | 73961 | 74025 | 74089 | 74154 | 74219 | 74284 | 74349 | 74414 | 74479 | 74544 | 65 |
| 32 | 74610 | 74676 | 74742 | 74808 | 74874 | 74940 | 75007 | 75073 | 75140 | 75207 | 66 |
| 33 | 75274 | 75341 | 75408 | 75176 | 75543 | 75611 | 75679 | 75747 | 75815 | 75883 | 68 |
| 34 | 75951 | 76020 | 76089 | 76157 | 76226 | 76295 | 76364 | 76434 | 76503 | 76573 | 69 |
| 35 | 76642 | 76712 | 76782 | 76852 | 76922 | 76993 | 77063 | 77131 | 77204 | 77275 | 70 |
| 36 | 77346 | 77417 | 77488 | 77560 | 77631 | 77703 | 77774 | 77846 | 77918 | 77990 | 72 |
| 37 | 78062 | 78134 | 78207 | 78279 | 78352 | 78425 | 78497 | 78570 | 78613 | 78716 | 73 |
| 38 | 78790 | 78863 | 78937 | 79010 | 79084 | 79158 | 79232 | 793306 | 79380 | 79.454 | 74 |
| 39 | 79528 | 79603 | 79677 | 79752 | $798: 27$ | 79902 | 79977 | 80052 | 80127 | 80:02 | 75 |
| 40 | 80277 | 80352 | 80428 | 80504 | 80580 | 80656 | 80732 | 80808 | 80884 | 80960 | 76 |
| 41 | 81036 | 81113 | 81189 | 81266 | 81343 | 81419 | 81496 | 81573 | 81650 | 81727 | 77 |
| 42 | 81805 | 81882 | 81959 | 82037 | 82114 | 82192 | 82270 | 82348 | 82425 | 82503 | 78 |
| 43 | 82582 | 82660 | 82738 | 82816 | 82895 | 82973 | 83052 | 83130 | 83209 | $83: 88$ | 78 |
| 44 | 83366 | 83445 | 83524 | 83603 | 83682 | 83762 | 83841 | 83920 | 81000 | 84079 | 79 |
| 45 | 84159 | 84238 | 84318 | 84398 | 84477 | 84557 | 84637 | 84717 | 84797 | 84877 | 80 |
| 46 | 84958 | 85038 | 85118 | 85199 | 85279 | 85359 | 85110 | 85521 | 85601 | 85682 | 81 |
| 47 | 9.8585763 | 85844 | 85924 | 86005 | 86086 | 86167 | 86219 | 86330 | 86.111 | 86192 | $+81$ |



|  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| re. | 0.0 | 0.18 | 0.2 | 0.3 | D. 1 | ${ }^{\text {a }}$. 5 | 0. ${ }^{\text {a }}$ | 0.7 | a,s | Q. ${ }^{\text {a }}$ |  |
| $\begin{gathered} 96 \\ 96 \\ 96 \\ 98 \\ 99 \end{gathered}$ |  | $\begin{aligned} & 19780 \\ & 201: 7 \\ & 20454 \\ & 20760 \end{aligned}$ | $\begin{aligned} & 19815151 \\ & \hline 20156 \\ & 20.656 \\ & 202099 \end{aligned}$ |  | $\begin{aligned} & 198969696 \end{aligned}$ |  | $\begin{aligned} & 19956 \\ & 20294 \\ & 20610 \\ & 20905 \end{aligned}$ |  |  |  | ${ }_{\substack{35 \\ 38}}^{\substack{35}}$ |
| $\begin{aligned} & \text { coo } \\ & \text { a } 101 \\ & 100 \\ & 103 \end{aligned}$ |  | $\begin{aligned} & 21045 \\ & 21308 \\ & 21549 \\ & 21769 \end{aligned}$ |  |  |  |  | $\begin{aligned} & 21179 \\ & 21431 \\ & 21664 \\ & 21687 \\ & 2187 \end{aligned}$ | $\begin{aligned} & 21205 \\ & 21455 \\ & 21683 \\ & 21890 \end{aligned}$ | $\begin{array}{\|l\|l\|} \hline 21231 \\ 21479 \\ 21795 \\ 21009 \end{array}$ |  |  |
| $\begin{aligned} & 100 \\ & \text { and } \\ & \text { 105 } \\ & 107 \end{aligned}$ |  | $\begin{aligned} & \text { 21966 } \\ & \hline 291 \\ & \hline 201291 \\ & \hline 22424 \end{aligned}$ |  | $\begin{aligned} & 290030 \\ & \hline 203 \end{aligned}$ |  |  |  |  |  <br> 2.2:38 |  | 13 |
| $\begin{aligned} & 108 \\ & 109 \\ & 110 \\ & 1110 \end{aligned}$ |  |  |  | $\begin{aligned} & \text { 29851 } 295120 \end{aligned}$ |  |  |  |  |  |  | 9 9 4 +2 |
| $\begin{aligned} & 112 \\ & 111 \\ & 114 \\ & 115 \end{aligned}$ |  |  | $\begin{aligned} & \text { ancric } \\ & \hline 2 \end{aligned}$ |  |  | $\begin{aligned} & 2.277 \\ & \hline 2 y y \end{aligned}$ | $\begin{aligned} & 29737 \\ & \hline 297 \\ & \hline 2250 \end{aligned}$ |  |  |  | ${ }_{-0}^{0}$ |
| $\begin{aligned} & 116 \\ & 117 \\ & 118 \\ & 119 \end{aligned}$ |  |  |  |  |  |  | $\begin{aligned} & \text { ang 290 } \end{aligned}$ |  |  | (e2053 | - $\begin{gathered}12 \\ 14 \\ 16 \\ 16\end{gathered}$ |
| $\begin{aligned} & 190 \\ & \text { an } \\ & 1921 \\ & 1223 \end{aligned}$ | $\begin{aligned} & 22074 \\ & 221890 \end{aligned}$ $\begin{aligned} & 21683 \\ & 91155 \end{aligned}$ $21455$ | $\begin{aligned} & 22056 \\ & 21870 \\ & 21662 \\ & 21431 \end{aligned}$ | $\begin{aligned} & 22039 \\ & 2180 \\ & 21639 \\ & 21499 \end{aligned}$ |  |  | 21981 <br> 21789 ${ }_{21333}$ | $\begin{aligned} & 21966 \\ & 2179 \\ & 21519 \\ & 21308 \\ & 2108 \end{aligned}$ |  | $\begin{aligned} & 21928 \\ & 21726 \\ & 21503 \\ & 21257 \end{aligned}$ | $\begin{aligned} & 21909 \\ & 21705 \\ & 21479 \\ & 21231 \end{aligned}$ | 181 |
| $\begin{aligned} & 124 \\ & \begin{array}{c} 125 \\ 126 \\ 127 \end{array} \\ & \hline \end{aligned}$ | $\begin{aligned} & 21205 \\ & 20934 \\ & 20640 \\ & 20326 \end{aligned}$ |  | $\begin{aligned} & 2153 \\ & \hline 2057 \\ & 2025979 \\ & 202026 \end{aligned}$ |  | $\begin{aligned} & 21099 \\ & 20819 \\ & 20517 \\ & 20195 \end{aligned}$ | $\begin{aligned} & 91072 \\ & 2079 \\ & 20756 \\ & 20161 \end{aligned}$ | $\begin{aligned} & 21015 \\ & 20760 \\ & 20455 \\ & 20128 \end{aligned}$ | $\begin{aligned} & 21017 \\ & 20731 \\ & 204 \because 3 \\ & 20094 \end{aligned}$ | $\begin{aligned} & 20990 \\ & 20701 \\ & 20391 \\ & 20060 \end{aligned}$ |  | ¢ |
| $\begin{gathered} 128 \\ \begin{array}{c} 129 \\ 139 \\ 131 \end{array} \\ \hline \end{gathered}$ | $\begin{aligned} & 19999559 \\ & 199555 \\ & 188662 \end{aligned}$ |  | $\begin{aligned} & 19991 \\ & \hline 1961 \\ & \hline 196181 \\ & 18780 \end{aligned}$ | $\begin{aligned} & 19886 \\ & \hline 1984 \\ & \hline 194141 \\ & 187393 \end{aligned}$ |  | $\begin{aligned} & 19816 \\ & 1919 \\ & 19063 \\ & 18656 \end{aligned}$ |  |  | $\begin{aligned} & 19508 \\ & 199393 \\ & 199593 \\ & 18530 \end{aligned}$ |  | 36 88 40 42 |
| $\begin{aligned} & 1323 \\ & \left.\begin{array}{l} 133 \\ 134 \\ 135 \end{array}\right) \end{aligned}$ | 18145 <br> 18009 17554 17079 | $\begin{aligned} & 18402 \\ & 17964 \\ & 17507 \\ & 17031 \end{aligned}$ | $\begin{aligned} & 1839999 \\ & 17740 \\ & 16968 \end{aligned}$ | $\begin{array}{ll} 1890 \end{array}$ |  | $\begin{gathered} 182304 \\ 177894 \\ 179395 \\ 168330 \end{gathered}$ |  | $\begin{aligned} & 18192 \\ & 17929 \\ & 17292 \\ & 16763 \end{aligned}$ | $\begin{aligned} & 18098 \\ & \hline 1796 \\ & 177176 \\ & \hline 1686 \end{aligned}$ | $\begin{gathered} 18051 \\ 18 x a n 0 \end{gathered}$ $\begin{aligned} & 17600 \\ & 17728 \end{aligned}$ | 44 46 47 49 |
| $\begin{aligned} & 136 \\ & \begin{array}{l} 137 \\ 138 \\ 139 \end{array} \\ & \hline \end{aligned}$ | $\begin{aligned} & 16586 \\ & \hline \end{aligned}$ |  | $\begin{gathered} 161185 \\ \hline 1571 \\ 157888 \\ 14888 \end{gathered}$ |  | $\begin{aligned} & 16884 \\ & \hline 15959 \\ & 159595 \\ & 14976 \end{aligned}$ |  |  | 16330 $\underset{\substack{15706 \\ 15165}}{151}$ 14607 |  | $\begin{aligned} & 16127 \\ & \hline 1600 \\ & \hline 15055 \\ & 14493 \end{aligned}$ | 51 <br> 53 <br> 55 <br> 56 <br> 6 |
|  |  |  |  | $\begin{aligned} & 12964979 \\ & 13977 \\ & 12974 \end{aligned}$ | $\begin{aligned} & \substack{14206 \\ 1390619 \\ 129016 \\ 123998} \end{aligned}$ |  |  | $\begin{aligned} & 14031 \\ & 18440 \\ & 12833 \\ & 12210 \end{aligned}$ | $\begin{aligned} & \substack{13973 \\ 132307 \\ 1227147} \\ & 127 \end{aligned}$ | $\begin{aligned} & 13994 \\ & \begin{array}{l} 1320 \\ 12209 \\ 12003 \end{array} \\ & \hline 1 \end{aligned}$ | 58 <br> 60 <br> 8 |


| Lagarithm of the Elliptic Radius Vector for esa $=0$. Constanl subtracted 0.00002:57. P'erind of Argment 1 . 2040.500 s . |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Arg. 1. | 0.0 | 0.1 | 0.2 | 0.13 | 0.1 | 0. ${ }^{18}$ | 0.fis | 0.7 | 0.4 | 0.9 | $\begin{aligned} & \text { Diff. } \\ & \text { for } 0 \mathrm{~d} .1 . \end{aligned}$ |
| $111^{11}$ | 9.861:030 | 11956 | 1180:3 | 11829 | 11765 | 11701 | 11636 | 11572 | 11.507 | 11143 | -64 |
| 145 | 11:388 | 11313 | 11218 | 1118: | 11117 | 110.51 | 10986 | 109:0 | 104.51 | 10788 | (66 |
| 1.16 | 10721 | 1065\% | 10588 | 10.52: | 1015\% | 10:3s\% | 10321 | 10251 | 10186 | 10119 | (i) |
| 117 | 100.1 | 0998:3 | 09916 | 09318 | 09779 | 09711 | 09613 | 09531 | 09505 | 091337 | 68 |
| 119 | 03369 | $09: 99$ | 00229 | 09160 | 09091 | 090:1 | 05951 | 0485: | 0881: | 08711 | 70 |
| 119 | 08671 | 05601 | 085i31 | 08160 | 08354 | 0x318 | 0x:14 | 08176 | 0810.3 | 080:31 | 71 |
| 150 | 07963 | 078.) | 07819 | 07718 | 07676 | 07601 | 075i3: | 07159 | 07387 | 07315 | 7: |
| 151 | 07: | 07169 | 07097 | 07021 | 069.51 | $065 \%$ | 06801 | 06731 | $0665 \overline{8}$ |  | 73 |
| $15:$ | 06.511 | 06133 | 06366 | $06: 89$ | 0621a | 09141 | 05066 | 0.9092 | 0.917 | 0.58 4.3 | 71 |
| 153 | 0.768 | 0.693 | 0.5619 | 05.511 | 0.168 | 0.2393 | 05318 | 0.0: $1: 3$ | 0.5167 | 0.091 | \%.) |
| 151 | 05016 | 01910 | 01861 | 01isa | 01712 | 016336 | 01.960 | 01181 | 01107 | 013331 | 76 |
| 155 | $01: 551$ | 01177 | 01101 | 010:3 | 03917 | 03870 | 037933 | 03715 | 036:39 | 03561 | 77 |
| 156 | 03183 | 03106 | 033:3 | 03251 | 03173 | 03095 | 03017 | 02:933 | 02861 | 02783 | 78 |
| 157 | $0: 701$ | 020 68 | 02514 | 02169 | 02390 | 02312 | 0.2e:33 | 022151 | 02075 | 01997 | 79 |
| 158 | 01918 | 01834 | 01759 | $016 \bigcirc 0$ | 01601 | 015:1 | 01112 | 01866 | 01283 | 01803 | 7) |
| 159 | 01121 | 01014 | 00961 | $00<81$ | 00801 | 00721 | 00811 | 00561 | 00181 | 00103 | 80 |
| 160 | 9.8600323 | 00213 | 0016: | 0008: | 00001 | :09921 | 99810 | 99759 | 99678 | 99598 | 81 |
| 161 | 9.85.j\%\%17 | 99136 | 99355 | 99:71 | 9919:3 | 99111 | 990:30 | 98919 | 988 (i8 | 98786 | 81 |
| 162 | 9870.5 | 98601 | 98512 | 98161 | 98379 | 98:97 | 94:16 | 98131 | 98052 | 97971 | 8 |
| 163 | 97889 | 97807 | 97725 | 97613 | 97561 | 97479 | 97397 | 97315 | 9723:3 | 97151 | $8:$ |
| 16.1 | 97008 | 96986 | 96901 | 96822 | 96739 | 96657 | 96575 | 96199 | 96110 | 96327 | 82 |
| 165 | $96: 15$ | 9616: | 96080 | 95997 | 9.914 | 95s:32 | 95749 | 95666 | 95.581 | 95501 | $8: 3$ |
| 166 | 95118 | 95335 | $95 \pm 53$ | 95170 | 95087 | 95001 | 91921 | 91839 | 94756 | 91673 | 83 |
| 167 | 91590 | 94507 | 914:1 | 91311 | 91258 | 94175 | 91092 | 91009 | 93920 | 9:38:13 | 83 |
| 168 | 93760 | $93677^{\circ}$ | 93594 | 93510 | 93127 | 93314 | 93261 | 93178 | 93095 | 93012 | 83 |
| 169 | 92929 | 92816 | 92763 | 92679 | 92596 | 92513 | 92130 | 9:3317 | 92:261 | 92181 | 83 |
| 170 | 92098 | 92015 | 91932 | 91818 | 91765 | 9168: | 91599 | 91516 | 91433 | 91350 | $8: 1$ |
| 171 | 91267 | 91181 | 91101 | 91018 | 90935 | 90852 | 90769 | 90686 | 90603 | $905: 1$ | 83 |
| 17: | 90138 | 9035\% | 90272 | 90189 | 90106 | 90021 | 899.11 | 898:5 | 89775 | 8969:3 | $8: 3$ |
| 173 | 89610 | 895:7 | 89445 | 8936: | 89:30 | 89197 | 89115 | 8903: | 88950 | 88967 | $8: 3$ |
| 17.4 | 88785 | 88702 | 886:0 | 88.338 | 88.156 | 88:373 | $88: 91$ | 88209 | 88127 | 88015 | $8:$ |
| 175 | 87963 | 87881 | 87798 | 87717 | 87635 | 87:53 | 87.171 | 87389 | 87308 | $87 \times 26$ | 82 |
| 176 | 87141 | 87063 | 86981 | 86900 | 86818 | 86737 | 86655 | 86571 | 86193 | 86112 | 81 |
| 177 | 86330 | $86 \div 19$ | 86168 | 86087 | 86006 | 85925 | 8581.1 | $8: 763$ | 855683 | 85602 | 81 |
| 178 | 85521 | 85141 | 85360 | 85280 | 85199 | 85119 | 85039 | 81959 | 81878 | 81798 | 80 |
| 179 | 84718 | 81638 | 81558 | 81178 | 81399 | 81319 | $81: 33$ | 81159 | 81080 | 81000 | 80 |
| 180 | 83921 | 83812 | $8376{ }^{2}$ | 83683 | 83601 | 83.25 | 83416 | 833637 | 83288 | 8:3 10 | 79 |
| 181 | 83131 | 83052 | $8: 971$ | 89895 | 82817 | 82739 | 82661 | 82:88: | 82501 | 82126 | 78 |
| 182 | 82318 | 82271 | 8:193 | 82115 | 82038 | 81960 | 81883 | 81806 | 81798 | 81651 | 77 |
| 183 | $815 \% 4$ | 81497 | 81421 | 8134.4 | 81267 | 81190 | 81114 | 81038 | 80961 | 80885 | 77 |
| 184 | 80809 | 80733 | 80657 | 80581 | 80505 | 801:30 | 803.51 | 80278 | 80203 | 80128 | 76 |
| 185 | $800 \overline{5} 3$ | 79978 | 79903 | 79828 | 79753 | 79678 | 79601 | 79509 | 7915.5 | 79381 | 75 |
| 186 | 79307 | 79233 | 79159 | 79085 | 79011 | 789:38 | 78861 | 78791 | 75717 | 78611 | 71 |
| 187 | 78571 | 78198 | 78126 | 78353 | 78280 | 78008 | 78135 | 78053 | 77991 | 77919 | 72 |
| 188 | 77817 | 77775 | 77701 | 77632 | 77561 | 77189 | 77.118 | 77317 | 77276 | 77205 | 71 |
| 189 | 77135 | 770G1 | 76991 | 76923 | 7685.3 | 76783 | 76713 | 76613 | 7 76.7.1 | 76.501 | 70 |
| 190 | 76435 | 76363 | 76296 | $763: 27$ | 76158 | 76090 | 76021 | 7595 | 75881 | 75816 | 69 |
| 19.1 | 9.8575748 | 75680 | 75612 | 75514 | 75177 | 75109 | 7534 | 7027\% | $75 \pm 08$ | 7514 | $-67$ |


| Logarithm of the Elliptic Rudius Vector for $\mathbf{5}$ n $=0$. Constant subtracted 0.0000257 . Period of Argument I. 224 d .7008. |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Arg. I. | 0. ${ }^{1}$. 0 | ${ }^{\text {d }}$. 1 | 0.2 | 0.3 | Q. 1 | 0.5 | ${ }^{\text {d }}$ d 6 | 0.8 | ${ }^{\text {d }}$ d | 0.9 | $\begin{aligned} & \text { Diff. } \\ & \text { for } 0^{\mathrm{d}} .1 . \end{aligned}$ |
| 192 | 9.8575074 | 75008 | 74941 | 74875 | 74809 | 74743 | ' 71677 | 74611 | 74545 | 74480 | -66 |
| 193 | 74415 | 74350 | 74:85 | 742:0 | 74155 | 74090 | 740:6 | 73962 | 73898 | 73831 | 64 |
| 191 | 73770 | 73706 | 73643 | 73579 | 73516 | 73453 | 73390 | 73327 | 73265 | 7320: | 63 |
| 195 | 73140 | 73078 | 73016 | 7:951 | 72893 | 72831 | 72770 | 72709 | 72648 | 72587 | 61 |
| 196 | 70.526 | 72465 | 72105 | 72345 | 72285 | 72225 | 72165 | 72106 | 7:046 | 71987 | 60 |
| 197 | 71928 | 71869 | 71810 | 7175\% | 71693 | 71635 | 71577 | 71519 | 71462 | 71404 | 58 |
| 198 | 71347 | 71289 | 71232 | 71175 | 71119 | 71062 | 71006 | 70950 | 70894 | 70838 | 56 |
| 199 | 7078: | 70727 | 70671 | 70616 | 70561 | 70507 | 70152 | 70398 | 70343 | 70:89 | 55 |
| 200 | 70236 | 70182 | 70128 | 70075 | 70022 | 69969 | 69916 | 69863 | 69811 | 69759 | 53 |
| 201 | 69707 | 69655 | 69603 | 69552 | 69500 | 69149 | 69398 | 69317 | 69:397 | 69246 | 51 |
| 202 | 69196 | 69146 | 69096 | 69047 | 69899 | 68918 | 68899 | 68850 | 68801 | 68753 | 49 |
| 203 | 68705 | 68657 | 68509 | 68561 | 68514 | 68166 | 68119 | 683\% | 68326 | 68:279 | 47 |
| 204 | 68233 | 68186 | 68140 | 68095 | 68049 | 68004 | 67959 | 67914 | 67869 | 67824 | 45 |
| 205 | 67780 | 67736 | 67692 | 67618 | 67605 | 67561 | 67518 | 67475 | 6743:2 | 67390 | 43 |
| 206 | 67317 | 67305 | 67263 | 672:2 | 67180 | 67139 | 67098 | 67057 | 67016 | 66975 | 41 |
| 207 | 66935 | 66895 | 66855 | 66815 | 66776 | 66737 | 66698 | 66659 | 66620 | 6658:2 | 39 |
| 208 | 66511 | 65506 | 66468 | 66130 | 66393 | 66350 | 66319 | 66282 | 66246 | 66209 | 37 |
| 209 | 66173 | 66137 | 66102 | 66066 | 66031 | 65996 | 65961 | 65927 | 65892 | 65858 | 35 |
| 210 | 658:4 | 65790 | 65757 | 65711 | 65690 | 65658 | 65625 | 6559: | 65560 | 65528 | 33 |
| 211 | 65496 | 65465 | 65434 | 65403 | 65372 | 65341 | 65310 | 65280 | 65250 | 65220 | 31 |
| 212 | 65191 | 65162 | 65133 | 65101 | 65075 | 65016 | 65018 | 61990 | 61962 | 61935 | 28 |
| 213 | 61907 | 64880 | 64853 | 648:7 | 64800 | 64774 | 64748 | 61722 | 61697 | 64672 | 26 |
| 214 | 64646 | 64622 | 61597 | 64573 | 64548 | 64524 | 64501 | 64477 | 64454 | 64431 | 24 |
| 215 | 64408 | 64385 | 61363 | 64311 | 61319 | 64297 | 61276 | $64: 55$ | 64234 | 64213 | 22 |
| 216 | 61192 | 64.172 | 64152 | 64132 | 61112 | 64093 | 64074 | 64055 | 64036 | 64018 | 19 |
| 217 | 63999 | 63981 | 63964 | 63946 | 63929 | 63912 | 63895 | 63878 | 63862 | 63816 | 17 |
| 218 | 63830 | 63814 | 63799 | 63781 | 63769 | 63754 | 63739 | 63725 | 63711 | 63697 | 15 |
| 219 | 63681 | 63670 | 63657 | 63611 | 63632 | 63619 | 63607 | 63595 | 63584 | 63572 | 12 |
| 220 | 63561 | 63550 | 63539 | 63528 | 63518 | 63508 | 63498 | 63489 | 63179 | 63170 | 10 |
| 221 | 63161 | 63453 | 63414 | 63436 | 63428 | 63420 | 63413 | 63406 | 63399 | 6339:2 | 8 |
| 222 | 63386 | 63379 | 63373 | 63367 | 63362 | 63357 | 63351 | 63317 | 63312 | 63338 | 5 |
| 223 | 63333 | 63330 | 63326 | 6332: | 63319 | 63316 | 63314 | 63311 | 63309 | 63307 | 3 |
| 224 | 9.8563305 | 63303 | 63302 | 63301 | 63300 | 63300 | 63:99 | 63:299 | 63299 | 63300 | -0 |
|  |  |  |  |  |  |  |  |  |  |  |  |

## TABLE KXVH．

|  |  |  |  |  |  |  |  |  |  |  |  | Pert．of Log．r． <br> Fact．to be $\times\left(\begin{array}{c}\mathbf{m 1 0 0}\end{array}\right)^{2}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Arg． 1 | Factor． | log．fac． | Arg． 1. | Factor． | $\log$ ．fise． | Arg． 1. | Factor． | $\log$ ．fiue． | Arg．I． | Fuctor． | Iog．fac． | Arg． 1. | Factor． |
| 1 | ＋13．4． | 1．16－4 | （i） | － 1.61 | n 1．： 0 \％ | 1：1 | －12．14 | 21．113： | 1－1 | ＋1．06 |  | 0 | －2．1 |
| 1 | 13．45 | $1.12 \times 6$ | （ii． | 1.97 | 0．2゙5゙5 | 121 | 12．10 | 1．1115\％ | 1－1 | ＋1．11 | 1）（il4！） | 4 | 2.1 |
| $\stackrel{2}{2}$ | 1343 | 1.1231 | 69 | 9.34 | 0．31；\％ | 129 | 1：201 | 1．10\％ | $1 \div$ | 1.7 | 10．1204 | 8 | 2.0 |
| 3 | 13.10 | 1．1283 | 6.1 | 2.61 | $0.435 \%$ | 123 | 1：こ1 | 1．14．） | 1－3 | 5.12 | 0.8093 | 12 | 2.0 |
| 4 | ＋13．36 | $1.1 \pm 69$ | 61 | － 3.07 | ก $0.1 \times 51$ | 12.1 | $-10.5!$ | n1．10rs | 131 | $+5.47$ | $0.73 \% 7$ | 16 | $-1.9$ |
| 5 | 13．3： | 1.124 | （6） | 3.13 | 0.5354 | 12.5 | 10.13 | 1．0：61 | 1－5 | 5.81 | 0.7612 | 2） | 1.8 |
| （i） | 13．26 | $1.12 \% 1$ | 66 | 3.79 | $0.57 \div 1$ | 129 | 12．35） | $1.19 \%$ | 1－6 | 6.15 | $0.75+3$ | 21 | 1.6 |
| 7 | 13.19 | 1.123 | 6 | 1.14 | $0.618 \%$ | $1: 7$ | 12．21 | $10 \leq 6{ }^{\circ}$ | 187 | 6.42 | 0.8113 | 23 | 1.5 |
| ¢ | ＋13．10 | 1.1174 | 63 | $-449$ | n0．6．01 | 123 | $-13.06$ | 21．0×13 | 128 | $+6.81$ | 0．8：133 | 34 | －1．3 |
| 9 | 13．01 | 1.1144 | （\％） | 4.81 | 0．6－47 | 129 | 11.90 | 1．07．57 | $1 \times!$ | 7.13 | 0．e－5：34 | 36 | 1.1 |
| 11 | 12．91 | 1.1110 | 70 | 5.13 | 0.714 .1 | 1：31 | 11.71 | 1 UGiMs | 190 | $74 \%$ | 0.8823 | 40 | 0.9 |
| 11 | 12.50 | 1．1072 | 71 | 5.50 | 0．7．11！ | 131 | 11.66 | $1.06: 30$ | 191 | 7.85 | 0.8932 | 41 | 0.7 |
| 12 | $+12.63$ | 1.1030 | 72 | － 5.85 | ทา．\％6\％． | 139 | 11.38 | 41.0561 | 192 | $+8.07$ | 0.9070 | 43 | －0．5 |
| 13 | 12.51 | 1.0984 | 71 | 6.18 | ก．7：リ！ | 1：33 | 11.119 | 1．0．14\％ | 1193 | 8．11\％ | 0.91293 | $5 \%$ | －0．2 |
| 14 | 12.40 | 1.09135 | 74 | 6.51 | 0.4134 | 1：31 | 10.113 | 1．041）8 | 19.4 | 8.67 | $0.137!1$ | 56 | 0.0 |
| 15 | 19．25 | 1.0880 | 75 | 6.83 | $0.834 *$ | 135 | 10.77 | $1.03 \% 4$ | 195 | 8.95 | $0.90 \cup 0$ | 60 | ＋0．2 |
| 16 | ＋12．08 | 1.0322 | 76 | $-7.14$ | n0．853\％ | 136 | －10．56 | n1．0335 | 196 | $+9.23$ | 0.96 .53 | 64 | $+0.5$ |
| 17 | 11.11 | 1.0760 | 77 | 7．4．） | 0．87： 0 | 137 | 10.33 | 1.0141 | 197 | 9.51 | 0.9750 | 63 | 0.7 |
| 18 | 11.73 | 1.0619 | 78 | 7．7．5 | 0.48 .13 | 133 | 10.10 | 1.0041 | 193 | 0.77 | 0.9899 | 72 | 0.9 |
| 19 | 11.54 | 1．06：2 | 79 | 8.05 | 0.9056 | 139 | 9.85 | $0.99 \% 36$ | 199 | 10.03 | 1.0013 | 76 | 1.1 |
| ${ }_{2}$ | ＋11．34 | 1.05 .15 | 80 | － 8.33 | $n 0.9279$ | 140 | $-9.69$ | n0．942\％ | 200 | ＋10．23 | 1.0119 | 80 | ＋1．3 |
| 21 | 11.13 | 1.046 .3 | 81 | 8.69 | 0.931 .4 | 141 | 9．3．） | 0.19717 | 201 | 10.52 | 1.0240 | 81 | 1.5 |
| 929 | 10.91 | $1.037!$ | 8. | $8.8!9$ | 0.9491 | 142 | 9.05 | 0．9583 | 20： | 10．\％ | $1.0315^{\circ}$ | 83 | 1.6 |
| 23 | 10.68 | 1.0237 | 83 | 11.16 | $0.96 \div 1$ | 143 | 8.81 | 0.0451 | 903 | 10.98 | 1.0405 | 02 | 1.8 |
| 21 | $+10.45$ | 1.0190 | 84 | $-9.43$ | n0．9543 | 144 | －8．53 | $n 0.9311$ | 20.1 | ＋11．19 | 1.0439 | 96 | $+1.9$ |
| 2.5 | 10.23 | 1.0084 | 8.5 | 9.64 | 0.158 .9 | 145 | 8.25 | 0.916 .1 | 20.8 | 11.40 | $1.056 ?$ | 100 | $2.1)$ |
| 26 | 9.95 | 0.9979 | 86 | 0.93 | 0.9969 | 146 | 7.96 | 0.9008 | $\because 06$ | 11.69 | 1.0611 | 104 | 2.0 |
| 27 | 9.69 | 0.9861 | 87 | 10.17 | 1．0072 | 147 | 7.66 | 0.8812 | 207 | 11.79 | 1.081 .1 | 108 | 2.1 |
| 33 | ＋ 9.43 | 0．974：3 | 88 | －10．40 | $n 1.0170$ | 143 | － 7.36 | $n 0.8666$ | 278 | ＋11．96 | $1.0 \% 79$ | 112 | ＋ 2.1 |
| 29 | 9.15 | 0.10614 | 89 | 10.62 | 1.056 | 119 | 7.0 .7 | 0.8480 | 24.9 | 12．13 | 1.02419 | 116 | 2.1 |
| 30 | 8.87 | 0.19178 | 91 | 10.84 | 1．033．19 | 150 | 6.73 | 0.8021 | 210 | 12．？ | 1.08 .17 | 120 | 2.1 |
| 11 | 8.58 | 0．933 | 91 | 11.05 | 1.0432 | 151 | 6.41 | 0.8069 | 211 | 12.4 .1 | 1.0950 | 121 | 2.0 |
| 32 | ＋ 8.23 | 0.918 | 94 | －11．24 | n1．0509 | 152 | － 6.08 | n）． 8316 | 212 | $+12.58$ | 1.0999 | 123 | $+1.9$ |
| $: 13$ | 7.15 | $0.9) 51$ | 93 | 11.43 | 1.0532 | 1.73 | 5.75 | 0.7690 | 213 | 12.71 | 1.1043 | 132 | 1.8 |
| 3.1 | 7.67 | 0.85 .0 | 94 | 11.61 | $1.0630)$ | 151 | 5.42 | 0．73139 | 91.1 | 12.8 | 1.1053 | 136 | 1.7 |
| 35 | 7.36 | 0.8663 | 95 | 11.79 | 1.0714 | 155 | 5.03 | 0.8059 | 215 | 12.94 | 1.112 | 1.10 | 1.5 |
| 36 | ＋ 7.04 | 0.8476 | 9 | $-11.95$ | $n 1.0774$ | 156 | － 4.73 | n0．（i\％ 5.3 | 216 | ＋13．0．1 | 1.1153 | 141 | $+1.3$ |
| 37 | 6.71 | $0.8 \times 7{ }^{\text {a }}$ | 97 | 12.10 | 1.0833 | 137 | 4．33） | （1）．i．2．2 | 217 | 13.13 | 1．118：3 | 148 | 1.1 |
| 38 | 6.38 | 0.8051 | 15 | 12．25 | 11881 | 158 | 4.04 | 0.60 .99 | 213 | 13.21 | 1．120， | 15： | 0.9 |
| 39 | 6.05 | 0.7516 | 99 | 12.39 | 1.0930 | 159 | 3.68 | 0.5660 | $211)$ | 13．28 | 1．12：31 | 156 | 0.7 |
| 10 | $+5.71$ | 0.7565 | 100 | $-12.51$ | n1．0974 | 160 | － 3.32 | n0．5215 | $2 \pm 0$ | ＋13．33 | 1.1249 | 160 | $+0.5$ |
| 41 | 5.36 | 0.85196 | 101 | 12.63 | 1.1014 | 161 | 2.96 | 0.4716 | 291 | 1：1．3．4 | 1.126 .1 | 161 | 0.3 |
| 42 | 5.02 | 0.7004 | 102 | 19.74 | 1．10\％0 | 162 | 2.63 | 0.4146 | 229 | 13.41 | 1．1275 | 168 | $+0.0$ |
| 43 | 4.66 | 0.6638 | 103 | 12.83 | $1.10 \pm 3$ | 163 | 2．93 | 0.3158 | 293 | 13．4． | 1.1253 | $17 \%$ | －0．2 |
| 44 | ＋ 4.311 | 0.6341 | 104 | －12．92 | n1．1113 | 164 | － 1.86 | $n 0.2707$ | 22.1 | ＋13．45 | 1．1247 | 176 | －0．1 |
| 4.5 | ．1．95 | 0.5166 | 105 | 13.00 | 1．113！） | 163 | $1.4!)$ | 0.1746 | 23.3 | 1：3．43 | 1.1235 | 180 | 0.7 |
| 46 | 3.59 | 0.5350 | 106 | 13.07 | 1．1162 | 166 | 1.12 | 0.0271 | 246 | 13.41 | 1．128．7 | 184 | 0.9 |
| 47 | 3.22 | 0.5053 | 107 | 13.13 | 1.1182 | 167 | 0.75 | 9.876 | $2: 57$ | 13．42 | 1.1279 | 188 | 1.1 |
| 48 | ＋ 2.86 | 0.4503 | 108 | －13．17 | n1．1198 | 163 | － 0.33 | n9．55－6 | 243 | ＋13．30 | 1.129 | 102 | －1．3 |
| $4!$ | 2．4！ | 0.3961 | 10？ | 13.21 | 1.1210 | 169 | － 0.01 | $n 7.7833$ | 939 | 13．3． | 1.1506 | 196 | 1.5 |
| 50 | 2.19 | 0．826： | 110 | 13.81 | 1.1660 | 170 | $+0.37$ | p9．n（0） | $2: 30$ | 13.30 | 1.1239 | 290 | 1.6 |
| 51 | 1.75 | 0.2430 | 111 | 1：1．26 | 1.1223 | 171 | 0.74 | 9.8704 | 9：31 | 13.91 | 1.1218 | 204 | 1.8 |
| 54 | $+1.33$ | 0.1389 | 112 | －1：3．47 | n1．1623 | 1\％2 | ＋ 1.12 | $0.047 \%$ | 234 | ＋13．17 | 1.11113 | 208 | －1．9 |
| 63 | 1.00 | 0．0017 | $11: 3$ | 11．27 | 1．11023 | 173 | 1.43 | 0.1726 | $2: 3$ | 13.09 | 1．116．7 | 212 | 40 |
| 54 | 0.61 | 9．7923 | 114 | 113．26 | 1．15－1 | 17．1 | 1.86 | 0．26\％ | 23.4 | 12.99 | 1.1131 | 216 | 40 |
| 55 | ＋ 0.20 | $p^{0} .40 \leq 2$ | 115 | 13.23 | 1.1217 | 175 | 2.23 | 0.3457 | 235 | 12．88 | 1.1093 | 223 | 2.1 |
| 56 | －0．1： | n9．0719 | 116 | －13．2） | n1．127 | 176 | ＋2．60 | 0.4151 | 236 | ＋12．77 | 1.1067 | 221 | －2．1 |
| 57 | 0.119 | 9.6011 | $11 \%$ | 13.16 | 1．11！ 17 | 177 | 2.97 | 0.172 .5 | 2：17 | 13．1） | 1.1017 | 223 | 2.1 |
| 58 | 0．86 | 0.9363 | 118 | 1：1．11 | 1.1176 | 178 | 3.33 | $0.5 \div 3$ | 2.56 | 12.51 | 1．10370 | 2，3\％ | 2.1 |
| 59 | 1．21 | 0.01917 | 119 | 13.05 | 1．11．29 | $17!$ | 3.70 | 0 2igen | 2319 | 12．36 | $1.0311!$ | $2 \cdot 36$ | 90 |
| 6） | $\bigcirc 1.61$ | n0．9057 | 120 | $-12.98$ | n1．1132 | 18J | $+4.06$ | 0.6083 | $24 \%$ | ＋12．20） | 1：0c6：3 | 210 | －1．9 |

Perturbations of Log. r, by the Earlh.
Constant added 15.94
Period of Argument V1., 583 d .92.

| Arg. V1. | Equa. | Arg. V1. | Equa. | Arg. Vl. | Equa. | Arg. VI. | Equa. | Arg. V1. | Equa. | Arg. VI. | Equa. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (1) | 1716 | $104^{4}$ | 185! | 208 ¢ | 5.50 | 318 | 28.50 | $416^{\text {d }}$ | 45 | $520^{\text {d }}$ | 2527 |
| 2 | 1718 | 106 | 17\% | 210 | 614 | 314 | 2811 | 418 | 64 | 592 | 25\%4 |
| 4 | 1725 | 108 | 1729 | 212 | $6 \leq 1$ | 316 | 2769 | 420 | 87 | 524 | 2518 |
| 6 | 1736 | 110 | 1662 | 214 | \% 51 | 318 | 2709 | 422 | 11.1 | $5 \pm 6$ | 2509 |
| 8 | 1751 | 112 | 159)3 | 216 | 824 | 3:0 | 2653 | 494 | 145 | 598 | 2496 |
| 10 | 1769 | 114 | 1593 | 218 | 816 | $3 \times 2$ | 2594 | 426 | 179) | 530 | 2480 |
| 12 | 1792 | 116 | 1452 | 220 | 972 | $3: 24$ | 2531 | 428 | 216 | 533 | 2460 |
| 14 | 1818 | 113 | 1381 | 2 | 1049 | 320 | 2466 | 430 | 2.8 | 534 | 2438 |
| 16 | 1846 | 120 | 1310 | 2.21 | 1123 | 328 | 2:307 | 432 | 302 | $5 \cdot 36$ | 2413 |
| 18 | 1578 | 192 | 1933 | 2926 | 1209 | 330 | 2-326 | 434 | 350 | 538 | 2385 |
| 20 | 1912 | 124 | 1166 | $\underline{29}$ | 1210 | 332 | 2253 | 436 | 401 | 540 | 2356 |
| 2 | 194 | 126 | 1095 | 230 | 1372 | 334 | 2178 | 438 | 454 | 542 | 2323 |
| 24 | 1985 | 198 | 102.1 | $2: 12$ | 1455 | 336 | 2101 | 440 | 510 | 54.1 | 223: |
| 26 | $20: 4$ | 130 | 95.5 | 234 | 15.38 | 338 | $2(1) 2$ | 442 | 569 | 5.16 | 283 |
| 28 | 2061 | 132 | 886 | 236 | 1621 | 340 | 1942 | 444 | $62 ?$ | 548 | 2216 |
| 30 | 2103 | 134 | 818 | 238 | 1704 | 312 | 1861 | 446 | 692 | 550 | 2177 |
| 32 | 2143 | 136 | 752 | 240 | 1787 | 344 | 1780 | 448 | 757 | 5.5 | 2138 |
| 34 | $218: 1$ | 138 | 657 | 24. | $1-69$ | 346 | $16!97$ | 450 | 823 | 5.4 | 2098 |
| 36 | $2 \times 2$ | 140 | 624 | 244 | 1950 | 348 | 1614 | 45.2 | 891 | 556 | 2059 |
| :38 | 2259 | 142 | 563 | 246 | 2030 | 350 | 1531 | 454 | 960 | 558 | 2015 |
| 40 | (3).91 | 114 | 505 | 248 | 2108 | 352 | 1448 | 456 | 1099 | 560 | 1981 |
| 42 | $\underline{3} 39$ | 146 | 449 | 250 | 2185 | 35.1 | 1365 | 458 | 1100 | 56 | 1944 |
| 14 | 2361 | 148 | 395 | 252 | 2260 | 3.6 | 1283 | 4619 | 1171 | 564 | 1908 |
| 46 | 2391 | 150 | 345 | 254 | 2333 | 358 | 1202 | $46 \%$ | 1243 | 566 | 1874 |
| 48 | 2418 | 15 | 297 | 256 | 2404 | 360 | 1123 | 464 | 1:115 | 568 | 1813 |
| 50 | 2443 | 154 | 253 | 258 | 24.2 | 362 | 1044 | 466 | $13 \pm 6$ | 570 | 1814 |
| 59 | 2465 | 156 | 212 | 260 | $253{ }^{\circ}$ | 364 | 967 | 468 | 14.7 | 57.2 | 178! |
| 54 | 2484 | 158 | 174 | 26. | 2600 | 366 | 891 | 470 | 1528 | 574 | 1767 |
| 56 | 2500 | 160 | 140 | 264 | 2659 | 368 | 818 | 472 | 1508 | 576 | 1749 |
| 58 | 2513 | 162 | 109 | 266 | 2715 | 370 | 746 | 474 | 1666 | 578 | 1734 |
| 60 | 2522 | 164 | 83 | 269 | 2767 | $37 \times$ | 677 | 476 | 1733 | 580 | 1784 |
| 62 | 20528 | 166 | 60 | 270 | 2815 | 374 | 610 | 478 | 1799 | -502 | 1718 |
| 64 | 2531 | 168 | 41 | 272 | 2860 | 376 | 546 | 480 | 1863 | 584 | 1716 |
| 66 | 2530 | 170 | 47 | 274 | 2901 | 378 | 485 | $48: 2$ | $1!24$ | 586 | 1718 |
| 68 | 25\%) | 172 | 17 | 276 | 2938 | 380 | 427 | 484 | 1984 | 588 | 1725 |
| 70 | 2517 | 174 | 11 | 278 | 20 | 351 | 372 | 486 | 2041 | 590 | 1737 |
| 72 | 2505 | 176 | 9 | 280 | 2999 | 334 | 321 | 488 | 2095 | 593 | 1752 |
| 74 | $24!0$ | 178 | 12 | 282 | :1023 | 386 | 273 | 490 | 2147 | 594 | 1780 |
| 76 | 2471 | 180 | $1!$ | $2 \triangleleft 4$ | 83043 | 388 | 229 | $49 \%$ | 2196 | 596 | 1793 |
| 78 | 2449 | 182 | 31 | 286 | 3058 | 390 | 188 | 494 | 2242 | 598 | 1819 |
| 80 | 2493 | 184 | 46 | 288 | 3069 | 392 | 152 | 496 | 2985 | 600 | 1847 |
| 82 | 2393 | 186 | 66 | 290 | $30 \% 6$ | 394 | 119 | 498 | 2324 | $601 \%$ | 1879 |
| 84 | $\because 2360$ | 188 | 91 | 402 | 3078 | 396 | 91 | 500 | 2361 | 604 | 1913 |
| 86 | 2323 | 190 | 1:20 | 294 | $30 \% 5$ | 398 | 67 | 509 | $23!3$ | 606 | 1950 |
| 88 | 2284 | 192 | 153 | 296 | 3068 | 400 | 47 | 504 | 2422 | 608 | 1987 |
| 90 | 2241 | 194 | 189 | 998 | 3057 | 402 | 32 | 506 | 2448 | 610 | 2026 |
| 92 | 2194 | 196 | 2:30 | 300 | 3041 | 404 | 20 | 508 | 2470 | 612 | 2066 |
| :14 | 2145 | 198 | 275 | 302 | 3090 | 406 | 14 | 510 | 2489 | 614 | 2105 |
| 96 | 2093 | 200 | 393 | 304 | 2996 | 408 | 11 | $51:$ | 2503 | 616 | 2145 |
| 18 | 2039 | 202 | 375 | 306 | 2967 | 410 | 13 | 514 | 2515 | 618 | 2185 |
| 100 | 1981 | 204 | 4:30 | 308 | 2934 | 412 | 90 | 516 | 2523 | 620 | $2 \because 23$ |
| 102 | 19:2 | 206 | 488 | 310 | 2097 | 414 | 30 | 518 | 2527 | 64 | 2261 |
| 104 | 183! | 208 | 550 | 312 | 2856 | 416 | 45 | 520 | 2527 | 69.1 | 2295 |


| TABLE XXX. <br> Perturbations of Log, $r$, by the Earth. Constant added 162. Period of Arg. VII. 243a.16. |  |  |  | TABLE XXXI. <br> Perturbations of Log. r, by Jupiter. <br> stant added 445. <br> Poriod of Arg. 1X., $236^{3} .99$. |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Arg. VII. | Equa. | Arg. VII. | Equa. | Arg. IX. | Equa. | Arg. IX. | Equa. | Arg. IX. | Equa. |
| d 0 0 -4 8 12 | 171 154 137 121 | 128 138 136 140 | 180 197 213 228 | $\begin{aligned} & \text { d } \\ & 0 \\ & 2 \\ & 4 \\ & 6 \\ & 6 \end{aligned}$ | $\begin{aligned} & 585 \\ & 585 \\ & 586 \\ & 588 \end{aligned}$ | 80 80 82 84 86 | 321 295 269 244 | 160 162 164 166 | 363 389 414 438 |
| 16 20 24 28 | 105 90 75 61 | 144 148 152 156 | 243 257 270 282 | $\begin{array}{r} 8 \\ 10 \\ 12 \\ 14 \end{array}$ | $\begin{aligned} & 591 \\ & 594 \\ & 598 \\ & 603 \end{aligned}$ | 88 90 92 94 | 219 194 171 148 | $\begin{aligned} & 168 \\ & 170 \\ & 172 \\ & 174 \end{aligned}$ | $\begin{aligned} & 462 \\ & 484 \\ & 506 \\ & 526 \end{aligned}$ |
| 32 36 40 44 | 49 37 37 19 | 160 164 168 172 | 293 302 310 316 | $\begin{aligned} & 16 \\ & 18 \\ & 20 \\ & 22 \end{aligned}$ | 608 613 618 623 | 96 98 100 102 | 127 106 88 71 | 176 178 180 182 | 545 563 579 593 |
| 48 52 56 60 | 12 6 2 0 | 176 180 184 188 | 320 323 324 324 | $\begin{aligned} & 24 \\ & 26 \\ & 28 \\ & 30 \end{aligned}$ | 629 633 638 642 | 104 106 108 110 | 55 41 49 29 19 | 184 186 188 190 | 606 <br> 617 <br> 627 <br> 635 |
| $\begin{aligned} & 64 \\ & 68 \\ & 72 \\ & 76 \end{aligned}$ | 0 1 4 4 | 192 196 200 204 | 321 317 311 304 | $\begin{aligned} & 32 \\ & 34 \\ & 36 \\ & 38 \end{aligned}$ | 645 647 648 648 | 112 114 116 118 | 12 6 2 1 | 192 194 196 198 | 641 646 649 651 |
| 80 84 88 92 | 15 23 23 43 | 208 212 216 220 | 205 285 283 261 | $\begin{aligned} & 40 \\ & 42 \\ & 44 \\ & 46 \end{aligned}$ | 647 644 640 635 | 120 122 124 126 | 1 4 9 16 | 200 202 204 206 | 651 651 649 646 |
| 96 100 104 108 | 56 69 83 98 | 224 224 238 238 236 | 247 232 216 200 | $\begin{array}{r} 48 \\ 50 \\ 50 \\ 52 \\ 54 \end{array}$ | $\begin{aligned} & 628 \\ & 619 \\ & 608 \\ & 596 \end{aligned}$ | 128 130 132 134 | 25 36 49 64 | 208 210 212 214 | 642 638 633 628 |
| $\begin{aligned} & 112 \\ & 116 \\ & 120 \\ & 124 \end{aligned}$ | $\begin{aligned} & 114 \\ & 130 \\ & 146 \\ & 163 \end{aligned}$ | 240 244 248 252 | 184 167 151 134 | $\begin{aligned} & 56 \\ & 58 \\ & 60 \\ & 62 \end{aligned}$ | $\begin{aligned} & 583 \\ & 567 \\ & 551 \\ & 532 \end{aligned}$ | 136 138 140 142 | 81 99 118 139 | 216 218 220 222 | $\begin{aligned} & 623 \\ & 617 \\ & 612 \\ & 607 \end{aligned}$ |
|  66 492 146 185 226 597 <br>  68 470 148 209 228 593 <br>  70 447 150 234 230 590 <br>  72 423 152 259 232 $: 588$ <br>  74 398 154 285 434 586 <br>  76 373 156 311 236 585 <br>  78 347 158 337 238 585 <br>  80 321 160 363 240 586 |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |

The perturbations are in units of the eighth decimal place.

'1'he perturbations are in units of the cighth decmat prace.



The perturbations are in units of the eighth decimal plaee.

| Perturbations of Log. r, by the Earth. <br> Horizontal Argument $=\mathbf{I}$. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cinstant added 150. Period of Argument X1, 240 unit |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Arg. NI . | 120 | 128 | 136 | 14. | $15 \stackrel{1}{4}$ | 160 | 16* | 176 | 181' | $19 \stackrel{\text { d }}{2}$ | $200^{\circ}$ | 208 | 216 | 221 | 23 |
| 0 | 210 | 217 | 2 | 231 | 23.3 | 2:13 | 239 | 2:3 | 237 | $2: 16$ | 236 | 239 | 214 | 252 | 269 |
| 2 | 2) | 212 | 215 | 293 | $2: 27$ | 9e9 | 2:10 | (2) | 927 | 326 | 298 | 2313 | 2:36 | 25 | 2.56 |
| 4 | 202 | 216 | 211 | 21.5 | 218 | $2: 0$ | $2 \geq 1$ | 219 | 217 | 216 | 216 | 219 | 42, | 234 | 246 |
| 6 | 196 | 199 | $20 \cdot$ |  | 209 | 210 | 210 | 299 | 206 | 20.1 | 29 | 209 | 211 | 290 | 215 |
| $\checkmark$ | 1*:) | 191 | 194 | 197 | 199 | 1919 | 199 | 196 | 193 | 190 | 188 | 190 | 194 | 213 | 25 |
|  | 133 | 104 | 186 | 158 | 189 | 1-4 | 136 | 1-3 | 173 | 174 | 171 | 121 | 173 | 181 | $1: 3$ |
| 12 | 179 | 131 | 180 | 181 | 189 | 1\% | 171 | 169 | 169 | 150 | 150 | 143 | 149 | 156 | 166 |
| 14 | 178 | $1: 7$ | 176 | 176 | 174 | 170 | 164 | 156 | 147 | 1:39 | 130 | 125 | 124 | 129 | 1:38 |
| 16 | 137 | 176 | 18.5 | $17: 3$ | 1310 | 16.5 | $15 \%$ | 148 | 1336 | 194 | 113 | 105 | 101 | 102 | 109 |
| 13 | 175 | 174 | 173 | 172 | 169 | 164 | 156 | 1.15 | 131 | 117 | 102 | 4 | 83 | 81 | 84 |
| 20 | 180 | 169 | 120 | 170 | 169 | 364 | 158 | 1.17 | 134 | 118 | 101 | 87 | 2 | 63 | 67 |
| 2 | 159) | 16. | 163 | 165 | 167 | 160 | 162 | 15.3 | 142 | 126 | 109 | 32 | 76 | 6.9 | (6) |
| 24 | 14.4 | 147 | 151 | 157 | 16: | 16. | 166 | 161 | 169 | $1: 19$ | 12 | 10.5 | 87 | 72 | 62 |
| 9 | 123 | 1311 | 136 | 144 | 153 | 16) | 16 | 16. | 161 | 151 | 137 | 121 | $10: 3$ | $\stackrel{8}{81}$ | 78 |
| 2y | 113 | 114 | 140 | 123 | 138 | 149 | 158 | 163 | 16.4 | 160 | 150 | 137 | 120 | 103 | 8 |
| 30 | 102 | 100 | 10.4 | 111 | 121 | 133 | 145 | 154 | 169 | 161 | 156 | 147 | $1: 34$ | 119 | 104 |
| : 2 | : 8 | 级 | ! 11 | 96 | 104 | 115 | 129 | 1:39 | 149 | 15.1 | 15.5 | 150 | 14.3 | 130 | 118 |
| :11 | 110 | ! | 8.5 | 8.1 | 8 | ! 18 | 109 | 12 | 133 | 142 | 147 | 147 | 14.3 | 136 | 123 |
| 36 | 103 | 9.5 | 8.5 | 8!) | $7!$ | 84 | 193 | 104 | 116 | 127 | 135 | 1:192 | 14.10 | 1:178 | $1: 11$ |
| 38 | 119 | 103 | 90 | 80 | \% | 76 | 82 | 91 | 102 | 114 | 123 | 130 | 13.1 | 135 | 1:11 |
| 4) | 1:31 | 11.3 | 93 | 86 | \% | \% | 77 | 84 | 93 | 104 | 114 | 192 | 123 | 131 | 13:3 |
| 4 | 111 | $1: 4$ | 103 | 94 | 84 | is | 33 | 82 | 8 | 136 | 117 | 116 | 123 | $1: 7$ | 1:3) |
| 44 | 146 | 139 | 117 | 103 | \% | 8. | 82 | 81 | 89 | 96 | 10.4 | 119 | 118 | 123 | 1\%i |
| 46 | 14: | 137 | $1: 4$ | 111 | 100 | 9 | 83 | 87 | 90 | 45 | 102 | 105 | 114 | 119 | 120 |
| 48 | 149 | 141 | 129 | 115 | 107 | 99 | 9:3 | 91 | 92 | 15 | 100 | 105 | 110 | 113 | 116 |
| 50 | 147 | 141 | 133 | 123 | 113 | 104 | 19 | 94 | 9 | 95 | 93 | 101 | 105 | 107 | 109 |
| 5 | 14.3 | 140 | 1313 | 125 | 116 | 103 | 101 | 97 | 9 | 93 | 96 | 03 | 101 | 102 | 103 |
| 54 | 136 | 135 | 131 | 12. | 117 | 111 | 105 | 100 | 0 | 93 | 93 | 03 | 919 | 100 | 93 |
| 56 | 10. | 127 | 125 | 122 | 117 | 112 | 108 | 10.7 | 103 | 103 | 103 | 103 | 102 | 101 | 93 |
| 3\% | 112 | 115 | 116 | 136 | 113 | 111 | 110 | 109 | 109 | 110 | 111 | 111 | 111 | 108 | 104 |
| 60 | 96 | 101 | 10.5 | 107 | 108 | 108 | 110 | 112 | 115 | 114 | 121 | 123 | 123 | 120 | 11.5 |
| 62 | 81 | 87 | 92 | 96 | 99 | 102 | 107 | 119 | 119 | 145 | 131 | 135 | 136 | 135 | 129 |
| 61 | 70 | 75 | 80 | 84 | 89 | 94 | 100 | 108 | 117 | 127 | 136 | 144 | 148 | 149 | 145 |
| 66 | 66 | 20 | 73 | 76 | 79 | 84 | 91 | 100 | 111 | 123 | 133 | 146 | 150 | 159 | 158 |
| 6 | 73 | 72 | 72 | 73 | \% 4 | 76 | 81 | 90 | 100 | 114 | 129 | 14: | 155 | 163 | 166 |
| 70 | 89 | 85 | 81 | 7 | 74 | 73 | 85 | 81 | 90 | 103 | 118 | 133 | 148 | 161 | 165 |
| 72 | 114 | 107 | 99 | 91 | 84 | 78 | 76 | \% 7 | ${ }_{83}^{83}$ | 93 | 107 | 123 | 140 | 150 | ${ }^{1675}$ |
| 74 | 144 | 134 | 123 | 312 | 101 | 92 | 84 |  |  |  | 101 | 115 | 139 |  |  |
| 78 | 176 205 | 16. <br> 105 <br> 105 | 153 183 | 140 180 | 126 156 | 114 142 | 103 120 | 96 118 | 93 111 | 109 | 112 | 114 | 131 | 144 145 | 1.9 159 |
| 78 | 205 | 195 | 183 | 18) | 156 | 142 | 129 | 118 | 111 | 109 | 112 | 120 | 181 |  |  |
|  | 230 | 2\% | 212 | 200 | 188 | 122 | 153 | 14.5 | 136 | 130 | 129 | 133 | 14 | 1.16 | $1{ }^{122}$ |
| 82 | 2.50 | 244 | 237 |  | $\stackrel{125}{0}$ | 202 | 188 | 174 | 163 | 15.4 | 150 | 150 | 15.5 | 161 <br> 173 | 170 |
| 84 | 266 | ${ }_{263}$ | 258 | 250 | 240 | 228 | 214 | 2001 |  | 178 |  |  |  |  |  |
| 86 88 | 279 289 | 278 | 274 237 | 263 482 | 2200 | 24: 29 | 236 23 | ${ }_{238}^{238}$ | 208 | 197 212 | 189 202 | 1334 | 183 | 18.1 19.1 | 189 198 |
| 88 | 239 | 2 3 | 237 | 482 | 274 | 264 | $25 \%$ | 238 | 2 | 212 | 202 | 59 | 19 |  |  |
|  | 293 | 99 | 295 | 291 | 235 | 275 | 263 | 2:0 | 236 | 221 | 213 | 205 | 201 | 200 | 203 |
| 32 | 293 | 297 | 29\% | 296 | 291 | 233 | 972 | 259 | 245 | 238 | $2 \cdot 1$ | 212 | 236 | 205 | 2.10 |
| 94 | 235 | 292 | $2: 16$ | 2.17 | 29.1 | 297 | 298 |  |  |  |  | -218 |  | 209 213 | 211 212 |
| 96 | 269 | $\stackrel{279}{290}$ | 283 272 | 291 | 291 | 2483 | 230 279 | 270 | 461 | 24.5 | ${ }_{233}^{238}$ | 2203 | 216 | 215 | 212 213 |
| 93 | 246 | 260 | 272 | 280 | 23.4 | 233 | 289 | 271 | 201 | 245 | 23 |  |  |  |  |
| 100 | 219 | 236 | 231 | 263 | 270 | 273 | 27\% | $2{ }^{6} 7$ | 250 | 243 | 239 | 223 | 290 | 215 | 212 |
| 102 | 139) | 207 | 205 | 240 | 251 | 20, | 259 | 257 | 2, 21 | $2 \cdot 2$ | 23, | - 214 | 216 | 210 | ${ }_{127}^{297}$ |
| 104 | 160 | 178 | 197 | 214 | 227 | ${ }_{213}^{237}$ | 243 219 | 退 |  | 2931 214 | $\stackrel{202}{207}$ | (1914 | 2968 |  | 198 |
| ${ }_{108}^{106}$ | 133 109 | 19 | 149 | 159 | 37. | 187 | 196 | 20 | 230 | 196 | 181) | 182 | 175 | 170 | 169 |
| 110 | 89 | 101 | 116 | 133 | 149 | 162 | 173 | 189 | 183 | 174 | 173 | 166 | 15.5 | 155 | 153 |
| 112 | 63 | \% 9 | 92 | . 108 | 131 | 13: | 1.51 | 16. | 16.3 | 16:1 | 159) | 15.3 | 147 | 142 | 1339 |
| 114 | 50 | 58 | 7. | 84 | 101 | 117 | 131 | 14. | 149 | 151 | 150 | 145 | $1: 19$ | 13.1 | 130 |
| 116 | 39 | 39 | 49 | 62 | \% 8 | 96 | 112 | 12 | 13.3 | 110 | 112 | 140 | 13. | 140 | 20, |
| 118 | 18 | 2 | 16 | 4 | 8 | 54 53 | ${ }_{71}$ | 88 | 103 | 11. | 124 | 130 | 123 | 1:27 | 12\% |
| 120 | 10 | 11 | 16 | 21 | 3 |  |  |  |  |  |  |  |  |  |  |





# TABLE XXXIV. 






The perturbations are in units of the eighth decimal place.

| \％\％\％ | ¢\％\％\％\％\＃¢ ¢ | \％\％\％\％\％ |  | あぁち ぶ |  | －¢ ¢ ar | －$\omega$ O－O | 发 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \％ | А灾会 | A $0_{6}$ |  | びひひひ | －orerato | ※ちろ ※ \％ | \＄\％\％\％M M | 朢 |  |
| © | 合念 |  |  | Esours | ขras $\cos _{\text {¢ }}$ |  | ¢ \％\％M \％ | ${ }_{80}$ |  |
| $\stackrel{*}{\text { A }}$ | 令 | ¢ ¢ ¢ \％\％\＆ |  | 大ras－ar |  | 10 \％\％\％\％ | \％\％\＃\％ | $\underset{\sim}{\text { win }}$ |  |
| $\pm$＊ | ＊ | \％ | そこぢめの | Or - Oros $\infty$ | あムちゃ \％ | K $8 \pm \mathscr{\leftrightarrow}$ | H．： |  |  |
| ＊せ | $\wedge \pm 4 \square_{4}^{\circ}$ | ¢ \％ | むくッणメ | A oraso | 二あ心込 | \％\％w \％\％ | \％ | $\underset{心}{\underset{心}{心}}$ |  |
| ह |  | § \％Ј ¢ ¢ | $\infty \mathrm{O} \sim \mathrm{c}_{0}$ | のッひた |  | ¢゙¢ \％\％\％\％ | \％\％今＊＊ | $\hat{e}_{\hat{\theta}}$ |  |
| $\hat{*}$ | ¢9\％\＃\＃w |  | or $\omega$ co co or | メあむそ | \＆ | ¢ |  |  |  |
| $\pm \%$ | ¢ | चちゃの－ | 10 co era |  | \＃\％¢ \％¢ ¢ \％ | $\underset{¢}{4}$ |  | $\stackrel{\rightharpoonup}{\alpha}^{\prime \prime}$ |  |
| \％\％ |  | Wosercoso | 10 coera | ¢゙ひ \＆ | W¢ \％¢ \％M | $\ddagger \sharp 4 \%$ \％\％ | $\Delta \# \#$ ¢ | ${ }^{\text {a }}$ |  |
| ¢ \％ | ¢88 ¢ \％＝ | $\sim \Delta 10 \sim+$ | cor＊ |  | ¢ | \＃\％\％ |  | ${ }_{8=}^{5}$ |  |
| \％\％ |  | $\omega ー$ ーレ | の๐ムそ（ |  | ¢ֻ¢ ¢ M M M M | \％\％\％\％\％ | 台台 80 | ${ }_{80}^{08}$ |  |
| ＊ | ¢500 | －o－wo | こち禹む | ¢్\％\％M \％\％\％\％ | \＆¢ ¢ M M M M |  | $\mathscr{6}$ | ${ }_{80}{ }^{10}$ |  |
| \＆ | むouso | －－の の | 元ちさ \％ |  |  | \％\％\％ | ¢ \％¢ M \＆ | $\stackrel{\sim}{8}$ |  |
| こ ¢ | $\infty-100$ | －${ }^{\text {－}}$－ | \％ | ¢్¢ M M M M | ¢ M M ¢ ¢ ¢ | ¢్ర M\％¢ ¢ ¢ ¢ M M |  | 皆 |  |
| उ－ | －－00－ | －いた ¢－ | \％ 84 |  |  |  | め芯先こた | 帯芯 |  |

When $224^{\mathrm{d}} .7$ is subtracted from Arg．I．add 0.8 to Arg．XIV．


The perturbations are expressed in hundredtlis of a second of arc.

| ジスニニニ゙ | 흥ㅎㅇ웅흉 |  | ※®\＃\＃ | 중⼷ㅚ서앙 | 8989ㅇ¢ㅇㅇㅇ | cricgicicy |  | ¢ M\％Mg | 20\％20 | あぁこむす | $\propto の-$＊ | $\stackrel{\square}{4}$ |  |
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Perturbations of the Latitude, by the Earth.
Horizontal Argument $=1$.
Constant added $0^{\prime \prime \prime} .62$.
l'eriod of Argument 1., 224a.7.

| $\begin{aligned} & \text { Arg. } \\ & \text { N1. } \end{aligned}$ | $\stackrel{1}{-}$ | ${ }_{8}^{\text {d }}$ | $1{ }^{\text {d }}$ | 21 | 32 | $4{ }_{4}^{\text {d }}$ | $4{ }^{\text {d }}$ | $5{ }_{6}^{\text {d }}$ | $6{ }^{\text {d }}$ | 78 | $8{ }^{\text {d }}$ | 88 | $9{ }_{6}^{\text {d }}$ | 10.1 | $11^{\text {di }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 120 | 8.5 | 91 | 95 | 93 | 99 | 99 | 96 | 91 | 85 | 77 | 69 | 69 | 52 | 45 | 39 |
| 12: | $8:$ | 89 | 96 | 109 | 103 | 105 | 104 | 101 | 96 | 89 | 81 | 73 | 64 | 57 | 51 |
| 12.1 | 76 | 8.5 | 93 | 93 | 105 | 103 | 110 | 1013 | 105 | 99 | 93 | 8.5 | 37 | 70 | 63 |
| 126 | (6) | 78 | 88 | 96 | 103 | 10¢ | 112 | 112 | 111 | 107 | 102 | 95 | 83 | 81 | 3 |
| 123 | 61 | 71 | 81 | 91 | 99 | 106 | 112 | 114 | 114 | 112 | 109 | 04 | 93 | 92 | 86 |
| 130 | 54 | 64 | 74 | 84 | 94 | 103 | 109 | 113 | 115 | 115 | 113 | 09 | 104 | 100 | 94 |
| 132 | 47 | 57 | 67 | 77 | 88 | 97 | 105 | 110 | 114 | 116 | 115 | 13 | 109 | 106 | 101 |
| 134 | 41 | 50 | 60 | 70 | 81 | 91 | 99 | 107 | 112 | 114 | 115 | 14 | 112 | 110 | 106 |
| 136 | 36 | 44 | 53 | 63 | 74 | 84 | 94 | 10 t | 108 | 112 | 114 | 14 | 113 | 112 | 110 |
| 135 | 32 | 39 | 47 | 56 | 67 | 7 | 87 | 95 | 103 | 108 | 111 | 13 | 113 | 112 | 111 |
| 140 | 29 | 35 | 41 | 50 | -59 | 70 | 79 | 89 | 97 | 102 | 107 | 10 | 111 | 111 | 111 |
| 14. | 23 | 32 | 37 | 44 | 53 | 62 | 72 | 81 | 89 | 96 | 101 | 105 | 107 | 109 | 109 |
| 14.4 | 30 | 30 | 35 | 40 | 47 | 56 | 64 | 73 | 89 | $8!$ | 94 | 99 | 102 | 105 | 106 |
| 146 | 33 | 32 | 35 | 38 | 4:3 | 50 | 53 | 6 GG | 74 | 81 | 87 | 92 | 96 | 93 | 100 |
| 148 | 38 | 37 | 36 | 38 | 41 | 47 | 53 | 60 | 67 | 73 | 79 | 84 | 88 | 91 | 94 |
| 150 | 4.5 | 43 | 41 | 41 | 42 | 46 | 50 | 55 | 61 | 67 | 72 | 76 | 80 | 84 | 8 |
| 152 | 53 | 53 | 47 | 45 | 45 | 47 | 49 | 53 | 57 | 62 | 66 | 69 | 73 | 77 | 78 |
| 154 | 61 | 57 | 54 | 51 | 50 | 50 | 51 | 53 | 56 | 59 | 62 | 64 | 67 | 69 | 70 |
| 156 | 68 | 6 | 61 | 58 | 56 | 55 | 55 | 55 | 56 | 58 | 60 | 61 | 62 | 63 | 64 |
| 158 | 73 | 71 | 68 | 63 | 62 | 61 | 59 | 59 | 59 | 59 | 59 | 59 | 59 | 59 | 59 |
| 160 | \% | 76 | 74 | 72 | 69 | 67 | 65 | 63 | 62 | 61 | 60 | 59 | 57 | 56 | 55 |
| 163 | 80 | 80 | 79 | 77 | 75 | 73 | 70 | 63 | 66 | 63 | 62 | 59 | 57 | 54 | 52 |
| 164 | 83 | 83 | 83 | 83 | 81 | 79 | 76 | 74 | 71 | 68 | 63 | 61 | 58 | 54 | 50 |
| 166 | 83 | 86 | 87 | 87 | 87 | 85 | 83 | 80 | 77 | 73 | 69 | 64 | 60 | 54 | 50 |
| 163 | 83 | 87 | 90 | 91 | 92 | 91 | 89 | 87 | 83 | 79 | 74 | 68 | 63 | 56 | 50 |
| 170 | 80 | 86 | 90 | 94 | 96 | 96 | 95 | 94 | 90 | 86 | 80 | 74 | 67 | 60 | 52 |
| 172 | 75 | 83 | 89 | 94 | 98 | 100 | 100 | 100 | 97 | 93 | 88 | 81 | 73 | 65 | 56 |
| 174 | 69 | 77 | 85 | 92 | 98 | 102 | 104 | 105 | 103 | 100 | 95 | 89 | 81 | 72 | 62 |
| 176 | 60 | 70 | 79 | 87 | 95 | 101 | 105 | 108 | 108 | 106 | 103 | 97 | 89 | 80 | 69 |
| 178 | 51 | 61 | 71 | 80 | 89 | 97 | 103 | 108 | 110 | 110 | 108 | 104 | 97 | 88 | 78 |
| 180 | 42 | 52 | 61 | 72 | 81 | 91 | 98 | 105 | 110 | 112 | 112 | 09 | 104 | 96 | 87 |
| 182 | 35 | 43 | 52 | 62 | 72 | 82 | 91 | 99 | 106 | 110 | 112 | 11 | 108 | 102 | 94 |
| 184 | 29 | 35 | 43 | 52 | 63 | 72 | 82 | 91 | 99 | 105 | 109 | 111 | 110 | 106 | 100 |
| 186 | 26 | 31 | 36 | 44 | 53 | 62 | 72 | 82 | 90 | 98 | 104 | 107 | 108 | 107 | 103 |
| 188 | 26 | 23 | 32 | 38 | 45 | 53 | 62 | 72 | 81 | 89 | 96 | 01 | 104 | 106 | 103 |
| 190 | 29 | 28 | 30 | 34 | 39 | 46 | 54 | (i2 | 71 | 80 | 87. | 94 | 98 | 101 | 101 |
| 192 | 33 | 31 | 30 | 32 | 35 | 40 | 47 | 54 | 61 | 70 | 78 | 85 | 91 | 94 | 97 |
| 194 | 40 | 35 | 33 | 32 | 34 | 37 | 41 | 46 | 53 | 61 | 68 | 75 | 82 | 87 | 91 |
| 196 | 47 | 41 | 37 | 35 | 34 | 35 | 37 | 41 | 46 | 52 | 59 | 66 | 72 | 78 | 83 |
| 198 | 56 | 48 | 43 | 39 | 36 | 35 | 35 | 37 | 40 | 45 | 50 | 56 | 62 | 68 | 74 |
| 20 | 65 | 57 | 51 | 45 | 41 | 38 | 36 | 35 | 36 | 39 | 43 | 47 | 53 | 59 | 65 |
| 202 | 74 | 67 | 60 | 53 | 47 | 42 | 39 | 36 | 35 | 35 | 37 | 40 | 44 | 49 | 54 |
| 204 | 83 | 76 | 69 | 62 | 55 | 49 | 44 | 39 | 36 | 34 | 34 | 35 | 37 | 41 | 45 |
| 206 | 91 | 85 | 78 | 71 | 64 | 58. | 51 | 45 | 40 | 37 | 34 | 33 | 33 | 35 | 37 |
| 208 | 96 | 92 | 86 | 80 | 74 | $67^{\circ}$ | 60 | 53 | 47 | 42 | 37 | 33 | 31 | 31 | 31 |
| 210 | 99 | 96 | 92 | 88 | 82 | 76 | 69 | 62 | 55 | 49 | 43 | 37 | 33 | 30 | 29 |
| 212 | 98 | 97 | 96 | 93 | 89 | 84 | 78 | 72 | 64 | 58 | 50 | 44 | 38 | 33 | 29 |
| 214 | 94 | 96 | 96 | 95 | 92 | 89 | 85 | 79 | 73 | 67 | 59 | 52 | 45 | 38 | 33 |
| 216 | 89 | 91 | 93 | 94 | 93 | 92 | 89 | 86 | 81 | 75 | 63 | 61 | 53 | 46 | 39 |
| 218 | 82 | 85 | 88 | 90 | 92 | 92 | 91 | 89 | 86 | 81 | 76 | 69 | 62 | 55 | 47 |
| 220 | 74 | 78 | 82 | 85 | 88 | 90 | 91 | 91 | 89 | 86 | 82 | 77 | 70 | 63 | 55 |
| 222 | 67 | 71 | 75 | 7) | 83 | 86 | 88 | 90 | 90 | 89. | 86 | 82 | 77 | 70 | 63 |
| 224 | 60 | 64 | 68 | 73 | 77 | 81 | 84 | 87 | 89 | 89 | 88 | 86 | 82 | 77 | 70 |
| 226 | 5.5 | 58 | 62 | 66 | ${ }_{61}$ | 75 | 80 | 8 | 87 | 88 | 89 |  | 86 | 82 | 76 |
| $2{ }^{2} 8$ | 50 | 52 | 55 | 60 | 65 | 69 | 74 | 79 | 83 | 86 | 89 | 89 | 88 | 86 | 82 |
| 230 | 46 | 47 | 50 | 54 | 58 | 63 | 68 | 74 | 79 | 83 | 87 | 89 | 89 | 88 | 86 |
| 23 | 43 | 43 | 45 | 48 | 52 | 57 | 69 | 68 | 74 | 79 | 84 | 87 | 89 | 90 |  |
| $\stackrel{334}{ }$ | 41 | 40 | 41 | 43 | 46 | 50 | $5{ }^{518}$ | 61 | ${ }_{6}^{67}$ | 73 66 | 79 | 83 79 | 87 83 |  | 90 89 |
| 236 238 | 41 | 39 40 | 38 37 | 39 36 | 40 36 | 34 | 48 42 48 | 54 47 | 60 52 | 66 59 | ${ }^{73}$ | 79 72 | 83 78 78 | 87 | 89 86 |
| 240 | 48 | 43 | 39 | 36 | 34 | 35 | 37 | 41 | 45 | 51 | 58 | 65 | 71 | 77 | 81 |


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|  | ざさひいの | －10－O－ | $10 \wedge \sim$ ®̈ | ニ8\％ | ¢¢ | ¢్¢¢Mus | （\％®®ざひ | びムニずo | －もニム゙． | ⑲\％ |  | $\stackrel{0}{20}$ |  |
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| \％¢以 | ¢゙っ $ニ$ ¢（1） | －10－ | ヘモゃも！ |  | ¢旡品出监 | ¢0w icio | ぎすこムむ | F0000 |  | civicic |  | $\stackrel{10}{8 .}$ |  |
|  | こoのメ＊ | 200006n | もあもむき |  |  | ¢80 | ムあむニち | － |  |  | \％¢ Mququ | ${ }_{\text {cio }}$ |  |
|  | ロサーツo | coscros＝ | 二こざきは |  |  | ※ポ心ぎこ | びひニーか | $\checkmark \infty \infty$ ごた | ニラ8゙ざ | ¢0\％\％\％Mis |  | ®＊ |  |
|  | $\infty \square \Delta \omega$ | －のめニこ |  | \％ | ¢\％\％刃 M | ※ぎもここ | にちゃuNu | マッロニあ | Бもせぎ | ¢G¢゙Mưy | \％¢icusi |  |  |
| 8\％ニちニめ | acrumer | 人もにらい |  |  | \％Wiccic | きこここニ |  | $4 \infty$ ち心或 |  |  | Huccus | 芯 |  |



Fram each of the quantities $K_{x}$. $K_{y}$ and $K_{z}$ the constant $2 y^{\prime \prime} .00$ has been subtracted; and from log $k_{y}$ the constant 0.0000089 , and from $\log _{0} k_{z}$ the constant $0.000006^{\circ}$ ).

Values, for the beginning of the year, of $K_{x}, K_{y}, \& \&$. , and of the Arguments of Nutation, for Washington Mean Noon of Jan. 0 in Common Years and Jan. 1 in Bissextile Years.

| Year. | $K_{x}$. | $K_{y}$. | $K_{z}$. | $\log k_{\mathrm{x}}$. | $\log k_{y}$. | $\log k_{2}$. | XV. | XVI. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1800 | 895888 | 1. 27 \% 0.71 | $35 \underbrace{2} 46{ }^{\prime} \quad 30.37$ | 9.9992901 | 9.9596717 | 9.6186183 | $617{ }^{\text {d }}$. 2 | $1.8{ }^{\text {d }}$ |
| 1801 | 8.88 | 0.84 | 28.48 | 2900 | 6739 | 6080 | 6535.2 | 1.5 |
| 1802 | 8.93 | 0.98 | 26.59 | 2900 | 6761 | 5978 | 102.0 | 1.3 |
| 1803 | 8.98 | 1.11 | 24.70 | 2899 | 6783 | 5875 | 467.0 | 1.0 |
| $1804 B$. | 9.04 | 1.24 | 22.81 | 2898 | 6806 | 5773 | 833.0 | 1.8 |
| 1805 | 9.09 | 1.37 | 20.93 | 2897 | 6828 | 5670 | 1198.0 | 1.6 |
| 1806 | 9.15 | 1.51 | 19.04 | 2897 | 6850 | 5567 | 1563.0 | 1.3 |
| 1807 | 9.20 | 1.64 | 17.16 | 2896 | 6872 | 5464 | 1928.0 | 1.1 |
| $1808 B$. | 9.24 | 1.77 | 15.27 | 2896 | 6894 | 5362 | 2294.0 | 1.8 |
| 1809. | 9.29 | 1.90 | 13.39 | 2895 | 6916 | 5259 | 2659.0 | 1.6 |
| 1810 | 9.33 | 2.03 | 11.50 | 2894 | 6939 | 5156 | 3024.0 | 1.4 |
| 1811 | 9.37 | 2.16 | 9.62 | 2894 | 6961 | 5053 | 3389.0 | 1.1 |
| $1812 B$. | 9.41 | 2.30 | 7.74 | 2893 | 6983 | 4950 | 3755.0 | 1.9 |
| 1813 | 9.45 | 2.43 | 5.85 | 2893 | 7015 | 4848 | 4120.0 | 1.6 |
| 1814 | 9.49 | 2.56 | 3.97 | 2892 | - 7037 | 4745 | 4485.0 | 1.4 |
| 1815 | 9.53 | 2.69 | 2.09 | 2892 | 7059 | 4642 | 4850.0 | 1.1 |
| 1816B. | 9.58 | 2.82 | $35246 \quad 0.21$ | 2891 | 7082 | 4539 | 5216.0 | 1.9 |
| 1817 | 9.63 | 2.95 | $352 \quad 45 \quad 58.33$ | 2890 | 7104 | 4436 | 5581.0 | 1.7 |
| 1818 | 9.69 | 3.08 | 56.45 | 2890 | 7126 | 4334 | 5946.0 | 1.4 |
| 1819 | 9.75 | 3.21 | 54.57 | 2889 | 7148 | 4231 | 6311.0 | 1.2 |
| $1820 \mathrm{~B} .$ | 9.80 | 3.34 | 52.69 | 2888 | 7170 | 4128 | 6677.0 | 1.9 |
| $1821$ | 9.85 | 3.47 | 50.81 | 2887 | 7192 | 4025 | 243.7 | 1.7 |
| 1822 | 9.91 | 3.60 | 48.93 | 2887 | 7215 | 3922 | 608.7 | 1.4 |
| 1823 | 9.97 | 3.73 | 47.06 | 2886 | 7237 | 3820 | 973.7 | 1.2 |
| $1824 B$. | 10.03 | 3.86 | 45.18 | 2885 | 7259 | 3717 | 1339.7 | 2.0 |
| 1825 | 10.08 | 3.99 | 43.30 | 2885 | 7281 | 3614 | 1704.7 | 1.7 |
| 1826 | 10.13 | 4.12 | 41.43 | 2884 | 7303 | 3511 | 2069.7 | 1.5 |
| 1827 | 11.17 | 4.25 | 39.55 | 2883 | 7325 | 3408 | 2434.7 | 1.2 |
| $1828 B$. | 10.21 | 4.38 | 37.68 | 2883 | 7347 | 3305 | 2800.7 | 2.0 |
| 1829 | 10.25 | 4.51 | 35.80 | 2882 | 7370 | 3202 | 3165.7 | 1.7 |
| 1830 | 10.29 | 4.63 | 33.93 | 2882 | 7392 | 3099 | 3530.7 | 1.5 |
| 1831 | 10.33 | 4.76 | 32.06 | 2881 | 7414 | 2996 | 3805.7 | 1.3 |
| $1832 B$. | 10.37 | 4.89 | 30.19 | 2881 | 7436 | 2893 | 4261.7 | 2.0 |
| 1833 | 10.42 10.46 | 5.02 5.15 | 28.31 26.44 | 2880 2879 | 7458 7480 | 2790 2687 | 4626.7 4991.7 | 1.8 1.5 |
| 1834 | 10.46 | 5.15 | 26.44 | 2879 | 7480 | 2687 | 4991.7 | 1.5 |
| 1835 | 10.51 | 5.28 | 24.57 | 2879 | 7503 | 2584 | 5356.7 | 1.3 |
| $1836 B$. | 10.57 | 5.40 | 22.70 | 2878 | 7525 | 2481 | 5722.7 | 2.0 |
| 1837 | 10.62 | 5.53 | 20.83 | 2877 | 7547 | 2378 | 6087.7 | 1.8 |
| 1838 | 10.68 | 5.66 | 18.96 | 2877 | 7569 | 2275 | 6452.7 | 1.6 |
| 1839 | 10.73 | 5.79 | 17.09 | 2876 | 7591 | 2172 | 19.4 | 1.3 |
| 1840 B . | 10.78 | 5.91 | 15.22 | 2875 | 7613 | 2069 | 385.4 | 2.1 |
| 1841 | 10.84 | 6.04 | 13.35 | 2875 | 7636 | 1966 | 750.4 | 1.8 |
| 1842 | 10.90 | 6.17 | 11.48 | 2874 | 7658 | 1863 | 1115.4 | 1.6 |
| 1843 | 10.95 | 6.30 6.42 | 9.62 7.75 | 2873 2872 | 7680 | 1760 1657 | 1480.4 1846.4 | 1.3 2.1 |
| $1844 B$. | 11.01 | 6.42 |  |  |  |  | 1846.4 | 2.1 |
| 1845 | 11.06 | 6.55 | 5.88 | 2872 | 7724 | 1554 | 2211.4 | 1.9 |
| 1846 | 11.10 | 6.67 | 4.01 | 2871 | 7746 | 1451 | 2576.4 | 1.6 |
| 1847 | 11.14 | 6.80 | 250 45 | 2871 | 7769 | 1348 | 2941.4 | 1.4 |
| $1848 B$. 1849 | $\begin{array}{rr} \\ & 11.18 \\ 89 & 58 \\ 11.22\end{array}$ | $127 \quad \begin{aligned} & \\ & 1\end{aligned}$ | $\begin{array}{rrrr}352 & 45 & 0.28 \\ 352 & 44 & 58.42\end{array}$ | 9.9992870 | 9.9597813 | 1245 9.6181142 | 3307.4 3672.4 | 2.1.9 |

From each of the quantities $K_{\mathrm{x}}, K_{\mathrm{y}}$ and $K_{\mathrm{z}}$, the constant $20{ }^{\prime \prime} .00$ has been subtracted; and from log $k_{\mathrm{y}}$ the constant 0.0000089 , and from $\log k_{z}$ the constant 0.0000560 .

Values, for the beginning of the year, of $K_{x}, \Pi_{y}$, \&-c., and of the Arguments of Nutation, for Washington Mean Noon of Jan. 0 in Common Ycars and Jan. 1 in Bissextile Years.

| Year. | $I_{x}$. | $\Pi_{\mathrm{y}}$. | $K_{z}$. | $\log k_{x}$. | $\log k_{y}$. | $\log k_{z}$. | XV. | XVI. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1850 | 89 58́ 11.127 | 1 i 27 7' 7.18 | $352^{\circ} 44{ }^{\text {c }} 56.55$ | 9.9992869 | 9.9597825 | 9.6181039 | 4037.4 | ${ }^{1.6}$ |
| 1851 | 11.31 | 7.31 | 54.69 | 2869 | 7847 | 0936 | 410:2.4 | 1.4 |
| $185: B$. | 11.35 | 7.43 | 52.83 | 2868 | 7869 | 0833 | 4768.4 | 2.2 |
| 1853 | 11.40 | 7.56 | 50.96 | 2867 | 7891 | 07:29 | 51333.4 | 1.9 |
| 1854 | 11.44 | 7.68 | 49.10 | 2867 | 7914 | 06:6 | 5198.4 | 1.7 |
| 1855 | 11.50 | 7.81 | 47.21 | 2866 | 7936 | 0523 | 5863.4 | 1.4 |
| 1856 B . | 11.56. | 7.93 | 45.38 | 2865 | 7958 | 0420 | $6: 29.4$ | 2.2 |
| 1857 | 11.62 | 8.06 | 43.52 | 2865 | 7980 | 0317 | 6591.4 | 1.9 |
| 1858 | 11.67 | 8.18 | 41.66 | 2861 | 8002 | 0213 | 161.2 | 1.7 |
| 1859 | 11.73 | 8.31 | 39.80 | 2863 | 8024 | 0110 | 526.2 | 1.5 |
| 1860 B. | 11.79 | 8.43 | 37.94 | 2863 | 8046 | 9.6180007 | 892.2 | 2.2 |
| 1861 | 11.81 | 8.56 | 36.08 | 2862 | 8069 | 9.6179904 | 1257.2 | 2.0 |
| 186: | 11.89 | 8.68 | 31.22 | 2861 | 8091 | 9801 | 16:2.2 | 1.7 |
| 1863 | 11.94 | 8.80 | 32.37 | 2861 | 8113 | 9697 | 1987.2 | 1.5 |
| 1861 B. | 11.99 | 8.93 | 30.51 | 2860 | 8135 | 9594 | 2353.2 | 2.2 |
| 1865 | 12.03 | 9.05 | 28.65 | 2859 | 8157 | 9491 | 2718.2 | 2.0 |
| 1866 | 12.07 | 9.18 | 26.79 | 2859 | 8179 | 9388 | 3083.2 | 1.8 |
| 1867 | 12.11 | 9.30 | 21.94 | 2858 | $8: 01$ | 9285 | 3118.2 | 1.5 |
| $1868 B$. | 12.15 | 9.42 | 23.08 | 2858 | 8221 | 9181 | 3814.2 | 2.3 |
| 1869 | 12.19 | 9.55 | 21.23 | 2857 | 8246 | 9078 | 4179.2 | 2.0 |
| 1870 | 12.21 | 9.67 | 19.37 | 2857 | 8268 | 8975 | 4544.2 | 1.8 |
| 1871 | 12.28 | 9.79 | 17.52 | 2856 | 8290 | 887: | 4909.2 | 1.5 |
| $1872 B$. | 12.33 | 9.92 | 15.67 | 2856 | 8312 | 8768 | 5275.2 | 2.3 |
| 1873 | 12.39 | 10.04 | 13.81 | 2855 | 8334 | 8665 | 5640.2 | 2.1 |
| 1874 | 12.44 | 10.16 | 11.96 | 2854 | 8356 | 8561 | 6005.2 | 1.8 |
| 1875 | 12.50 | 10.28 | 10.11 | 2854 | 8378 | 8458 | 6370.2 | 1.6 |
| 1876 B. | 12.56 | 10.40 | 8.26 | 2853 | 8401 | 8355 | 6736.2 | 2.3 |
| 1877 | 12.62 | 10.53 | 6.41 | 2852 | 8123 | 8251 | 302.9 | 2.1 |
| 1878 | 12.67 | 10.65 | 4.56 | 2851 | 8145 | 81.18 | 667.9 | 1.8 |
| 1879 | 12.73 | 10.77 | 2.71 | 2851 | 8167 | 8014 | 1032.9 | 1.6 |
| 1880 B. | 12.78 | 10.89 | $35244 \quad 0.86$ | 2850 | 8489 | 7941 | 1398.9 | 2.4 |
| 1881 | 12.83 | 11.01 | 3524359.01 | 2849 | 8511 | 7838 | 1763.9 | 2.1 |
| 1882 | 12.88 | 11.14 | 57.16 | 2849 | 8533 | 7734 | 2128.9 | 1.9 |
| 1883 | 12.93 | 11.26 | 55.32 | 2848 | 8556 | 7631 | 2493.9 | 1.6 |
| 1881 B. | 12.97 | 11.38 | 53.47 | 2848 | 8578 | 7528 | 2859.9 | 2.4 |
| 1885 | 13.01 | 11.50 | 51.62 | 2847 | 8600 | 7424 | 3221.9 | 2.1 |
| 1886 | 13.05 | 11.62 | 49.77 | 2817 | 8622 | 7321 | 3589.9 | 1.9 |
| 1887 | 13.09 | 11.74 | 47.93 | 28.16 | 86.4 | 7217 | 3951.9 | 1.7 |
| 188813. | 13.13 | 11.86 | 46.08 | 2816 | 8666 | 7114 | 4330.9 | 2.4 |
| 1889 | 13.18 | 11.98 | 44.24 | 2845 | 8688 | 7010 | 4685.9 | 2. 2 |
| 1890 | 13.22 | 12.10 | 42.39 | 2814 | 8711 | 6907 | 5050.9 | 1.9 |
| 1891 | 13.27 | 12.22 | 40.55 | 2844 | 8733 | 6801 | 5415.9 | 1.7 |
| 1892B. | 13.33 | 12.34 | 38.71 | 2813 | 8755 | 6700 | 5781.9 | 2.4 |
| 1893 | 13.39 | 12.46 | 36.86 | 2842 | 8777 | 6597 | 6146.9 | 2.2 |
| 1894 | 13.45 | 12.58 | 35.02 | 2842 | 8799 | 6493 | 6511.9 | 2.0 |
| 1895 | 13.50 | 12.70 | 33.18 | 2841 | 8821 | 6390 | 78.6 | 1.7 |
| 1896 B. | 13.56 | 12.82 | 31.31 | 2810 | 8843 | 6286 | 414.6 | 2.5 |
| 1897 | 13.62 | 12.94 | 29.50 | 2810 | 8866 | 6183 | 809.6 | 2.2 |
| 1898 | 13.67 | 13.06 | 27.66 | 2839 | 8888 | 6079 | 1174.6 | 2.0 |
| 1839 | 895813.73 | 12713.18 | $35213 \quad 25.82$ | 9.999:2838 | 9.9598910 | 9.6175976 | 1539.6 | 1.7 |

[^4] and from $\log _{i g} l_{2}$ the constant $0.0000 \overline{0} 0$

| Year. | $K_{\mathrm{x}}$. | $K_{y}$. | $K_{2}$. | Log $k_{x}$. | Log $k_{y}$. | $\log k_{\mathrm{z}}$. | XV. | XVI. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1900 | $89 \times 5813.78$ |  | $352^{\circ} 43$ 23 ${ }^{\prime \prime} 98$ | 9.9992838 | 9.9598932 | 9.6175872 | 1904.6 | $1.5{ }^{\text {d }}$ |
| 1901 | -13.82 | 13.42 | 22.14 | 2837 | 8954 | 5768 | 2269.6 | 1.3 |
| 1902 | 13.87 | 13.54 | 20.30 | 2837 | 8976 | 5665 | 2634.6 | 1.0 |
| 1903 | 13.91 | 13.65 | 18.47 | 2836 | 8998 | 5561 | 2999.6 | 0.8 |
| $1904 B$. | 13.95 | 13.77 | 16.63 | 2836 | 9021 | 5458 | 3365.6 | 1.5 |
| 1905 | 13.99 | 13.89 | 14.79 | 2835 | 9043 | 5354 | 3730.6 | 1.3 |
| 1906 | 14.03 | 14.01 | 12.95 | 2835 | 9065 | 5250 | 4095.6 | 1.0 |
| 1907 | 14.08 | 14.13 | 11.12 | 2834 | 9087 | 5147 | 4460.6 | 0.8 |
| $1908 B$. | 14.12 | 14.25 | 9.28 | 2833 | 9109 | 5043 | 4826.6 | 1.6 |
| $1909$ | 14.17 | 14.36 | 7.45 | 2833 | 9131 | 4940 | 5191.6 | 1.3 |
| 1910 | 14.22 | 14.48 | 5.61 | 2832 | 9154 | 4836 | 5556.6 | 1.1 |
| 1911 | 14.28 | 14.60 | 3.78 | 2832 | 9176 | 4732 | 5921.6 | 0.8 |
| $1912 B$. | 14.34 | 14.72 | 1.95 | 2831 | 9198 | 4629 | 6287.6 | 1.6 |
| 1913 | 14.40 | 14.83 | 352430.11 | 2830 | 9220 | 4525 | 6652.6 | 1.3 |
| 1914 | 14.45 | 14.95 | 3524258.28 | 2829 | 9242 | 4422 | 219.4 | 1.1 |
| 1915 | 14.50 | 15.07 | 56.45 | 2829 | 9264 | 4318 | 584.4 | 0.9 |
| $1916 B$. | 14.56 | 15.18 | 54.62 | 2828 | 9287 | 4214 | 950.4 | 1.6 |
| 1917 | 14.62 | 15.30 | 52.79 | 2827 | 9309 | 4110 | 1315.4 | 1.4 |
| 1918 | 14.67 | 15.42 | 50.96 | 2827 | 9331 | 4007 | 1680.4 | 1.1 |
| 1919 | 14.72 | 15.53 | 49.13 | 2826 | 9353 | 3903 | 2045.4 | 0.9 |
| 1920 B . | 14.76 | 15.65 | 47.30 | 2826 | 9375 | 3799 | 2411.4 | 1.6 |
| 1921 | 14.80 | 15.76 | 45.47 | 2825 | 9397 | 3695 | 2776.4 | 1.4 |
| 1922 | 14.84 | 15.88 | 43.64 | 2825 | 9420 | 3591 | 3141.4 | 1.2 |
| 1923 | 14.88 | 16.00 | 41.82 | 2824 | 9442 | 3488 | 3506.4 | 0.9 |
| 1924B. | 14.93 | 16.11 | 39.99 | 2824 | 9464 | 3384 | 3872.4 | 1.7 |
| 1925 | 14.97 | 16.23 | 38.16 | 2823 | 9486 | 3280 | 4237.4 | 1.4 |
| 1926 | 15.02 | 16.34 | 36.33 | 2823 | 9508 | 3176 | 4602.4 | 1.2 |
| 1927 | 15.06 | 16.46 | 34.51 | 2822 | 9530 | 3072 | 4967.4 | 0.9 |
| $1928 B$. | 15.11 | 16.57 | 32.68 | 2821 | 9552 | 2969 | 5333.4 | 1.7 |
| 1929 | 15.17 | 16.69 | 30.86 | 2821 | 9575 | 2865 | 5698.4 | 1.5 |
| 1930 | 15.22 | 16.80 | 29.03 | 2820 | 9597 | 2761 | 6063.4 | 1.2 |
| 1931 | 15.28 | 16.92 | 27.21 | 2819 | 9619 | 2657 | 6428.4 | 1.0 |
| 1932B. | 15.34 | 17.03 | 25.38 | 2819 | 9641 | 2553 | 6794.4 | 1.7 |
| 1933 | 15.40 | 17.14 | 23.56 | 2818 | 9663 | 2450 | 361.1 | 1.5 |
| 1934 | 15.46 | 17.26 | 21.73 | 2817 | 9685 | 2346 | 726.1 | 1.3 |
| 1935 | 15.51 | 17.37 | 19.91 | 2817 | 9708 | 2242 | 1091.1 | 1.0 |
| 1936B. | 15.57 | 17.49 | 18.09 | 2816 | 9730 | 2138 | 1457.1 | 1.8 |
| 1937 | 15.62 | 17.60 | 16.27 | 2815 | 9752 | 2034 | 1822.1 | 1.5 |
| 1938 | 15.66 | 17.71 | 14.45 | 2815 | 9774 | 1930 | 2187.1 | 1.3 |
| 1939 | 15.71 | 17.83 | 12.63 | 2814 | 9796 | 1826 | 2552.1 | 1.0 |
| 1940 B . | 15.75 | 17.94 | 10.81 8.99 | 2814 | 9818 | 1722 1618 | 2918.1 | 1.8 |
| 1941 | 15.79 | 18.05 | 8.99 | 2813 | 9841 9863 | 1618 1514 | 3283.1 | 1.6 |
| 1942 1943 | 15.83 15.88 | 18.17 18.28 | 7.17 5.36 | 2813 2812 | $\begin{array}{r}9863 \\ +9885 \\ \hline\end{array}$ | 1514 | 3648.1 4013.1 | 1.3 1.1 |
| 1943 $1944 B$. | 15.88 15.92 | 18.28 18.39 | 5.36 3.54 | 2812 | 9885 9907 | 1306 | 4379.1 | 1.8 |
| 1945 | 15.97 | 18.50 | 352421.72 | 2811 | 9929 | 1202 | 4744.1 | 1.6 |
| 1946 | 16.02 | 18.62 | 3524159.91 | 2811 | 9951 | 1098 | 5109.1 | 1.3 |
| 1947 | 16.07 | 18.73 | 58.09 | 2810 | 9974 | 0994 | 5474.1 | 1.1 |
| $1948 B$. | - 16.12 | ${ }_{1} 18.84$ | 252 56.28 | $\begin{array}{r}2809 \\ \hline 9\end{array}$ | $9.9599996$ | 0890 | 5840.1 | 1.9 |
| 1949 | $\begin{array}{llll}89 & 58 \quad 16.18\end{array}$ | 12718.95 | 3524154.46 | 9.9992809 | 9.9600018 | 9.6170786 | 6205.1 | 1.6 |

From each of the quantities $K_{\mathrm{x}}, K_{\mathrm{y}}$ and $K_{\mathrm{z}}$, the constant $20^{\prime \prime} .00$ has been subtracted ; and from $\log k_{\mathrm{y}}$ the constant 0.0000089 ,

| Corrections of $K_{x}^{-}, K_{x}, \& \cdot c$, due 10 Lumar Nutution, for 1850. Period of Argument XV., Grged. 3. |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Arg. } \\ & \mathrm{XV} . \end{aligned}$ | $\triangle K_{\mathrm{x}}$. | $\Delta K_{y}$. | $\triangle K_{z}$. | $\begin{aligned} & \text { Var. in } \\ & 100 \mathrm{yrs} . \end{aligned}$ | $\Delta \log k_{\text {c }}$ | log. $i_{2}$ | $\begin{aligned} & \text { Arg. } \\ & \mathrm{NV.} \end{aligned}$ | $\triangle K_{x}$. | $\Delta K_{y}^{*}$. | $\triangle K_{z}$. | $\begin{aligned} & \text { Var. in } \\ & 100 \text { yrs. } \end{aligned}$ | $\Delta^{\log / h_{y}}$. | $\Delta \log / i_{i}$. |
| ${ }_{0}^{11}$ | 18.00 | 18.63 | - 20.05 | +0.03 | 1 | 850 | 2100 | 3:2.0: | 81.70 | 28.17 | -0.02 | 148 | 140. |
| 50 | 18.78 | 19.42 | 20.79 | 0.03 |  | 817 | 2450 | 31.53 | 31.18 | 27.89 | 0.02 | 151 | 125 |
| 100 | 19.56 | 20.20 | $21.5 \pm$ | 0.03 | 2 | 844 | 2500 | 31.00 | 30.63 | 27.28 | 0.02 | 154 | 111 |
| 150 | 20.31 | 20.98 | 22.25 | 0.03 | 3 | 840 | 2550 | 30.45 | 30.05 | 26.64 | 0.02 | 157 | 98 |
| 200 | 21.11 | 21.75 | 22.95 | 0.03 | 4 | 835 | 2600 | 39.87 | 29.45 | 25.99 | 0.03 | 160 | 86 |
| 250 | 21.87 | 29.50 | 23.65 | +0.02 | 5 | 829 | 2650 | 29.26 | 28.82 | 25.32 | -0.03 | 162 | 74 |
| 300 | 22.63 | 23.25 | 24.33 | 0.02 | 7 | 822 | 2700 | 28.63 | 28.17 | 24.63 | 0.03 | 161 | 63 |
| 350 | 23.38 | 24.00 | 25.00 | 0.02 | 8 | 814 | 2750 | 27.97 | 27.49 | 23.92 | 0.03 | 166 | 53 |
| 400 | 24.12 | 24.71 | 25.66 | 0.02 | 10 | 806 | 2800 | 27.29 | 26.78 | 23.19 | 0.03 | 168 | 41 |
| 450 | 24.85 | 25.46 | 36.30 | 0.02 | 12 | 797 | 2850 | 26.50 | $\bigcirc 6.06$ | 22.45 | 0.03 | 170 | 36 |
| 500 | 25.57 | 26.17 | 26.93 | +0.02 | 14 | 787 | 2900 | 25.87 | 25.33 | 21.70 | -0.03 | 172 | 28 |
| 550 | 26.27 | 26.86 | 27.53 | 0.02 | 16 | 777 | 2950 | 25.13 | 24.58 | 20.94 | 0.03 | 173 | 21 |
| 600 | 26.94 | 27.52 | 28.10 | 0.02 | 19 | 766 | 3000 | 21.38 | 23.81 | 20.17 | 0.03 | 174 | 16 |
| 650 | 27.60 | 28.17 | 28.65 | 0.02 | 21 | 754 | 3050 | 23.61 | 23.03 | 19.39 | 0.03 | 175 | 11 |
| 700 | 28.25 | 28.80 | 29.19 | 0.02 | 24 | 741 | 3100 | 22.83 | 22.23 | 18.60 | 0.03 | 176 | 7 |
| 750 | 28.87 | 29.41 | 29.69 | +0.02 | 27 | 727 | 3150 | 22.04 | 21.43 | 17.81 | $-0.03$ | 176 |  |
| 800 | 29.47 | 29.99 | 30.17 | 0.02 | 29 | 713 | 3200 | 21.24 | 20.62 | 17.02 | 0.03 | 177 | 2 |
| 850 | 30.05 | 30.55 | 30.62 | 0.01 | 32 | 699 | 3250 | 20.43 | 19.80 | 16.23 | 0.03 | 177 | 1 |
| 900 | 30.60 | 31.09 | 31.05 | 0.01 | 36 | 684 | 3300 | 19.62 | 18.99 | 15.45 | 0.03 | 177 | 0 |
| 950 | 31.13 | 31.60 | 31.45 | 0.01 | 39 | 668 | 3350 | 18.80 | 18.16 | 14.66 | 0.03 | 177 | 1 |
| 1000 | 31.63 | 32.08 | 31.81 | +0.01 | 42 | 652 | 3400 | 17.98 | 17.34 | 13.88 | -0.03 | 177 | 3 |
| 1050 | 32.10 | 32.53 | 32.14 | 0.01 | 46 | 635 | 3450 | 17.16 | 16.51 | 13.10 | 0.03 | 176 | 5 |
| 1100 | 32.55 | 32.95 | 32.45 | 0.01 | 49 | 618 | 3500 | 16.35 | 15.70 | 12.34 | 0.03 | 175 | 9 |
| 1150 | 32.97 | 33.34 | 32.73 | 0.01 | 53 | 600 | 3550 | 15.54 | 14.89 | 11.59 | 0.03 | 174 | 13 |
| 1200 | 33.35 | 33.70 | 32.97 | +0.01 | 57 | 582 | 3600 | 14.73 | 14.09 | 10.84 | 0.03 | 173 | 18 |
| 1250 | 33.70 | 34.03 | 33.18 | 0.00 | 61 | 564 | 3650 | 13.93 | 13.29 | 10.11 | $-0.03$ | 172 | 21 |
| 1300 | 34.02 | 34.32 | 33.35 | 0.00 | 64 | 545 | 3700 | 13.14 | 12.50 | 9.40 | 0.02 | 171 | 31 |
| 1350 | 34.31 | 34.58 | 33.49 | 0.00 | 68 | 526 | 3750 | 12.36 | 11.72 | 8.70 | 0.02 | 169 | 39 |
| 1400 | 31.56 | 34.81 | 33.60 | 0.00 | 72 | 507 | 3800 | 11.59 | 10.96 | 8.02 | 0.02 | 167 | 48 |
| 1450 | 34.78 | 35.00 | 33.67 | 0.00 | 76 | 488 | 3850 | 10.84 | 10.22 | 7.36 | 0.02 | 165 | 58 |
| 1500 | 34.96 | 35.16 | 33.70 | 0.00 | 80 | 469 | 3900 | 10.10 | 9.49 | 6.72 | -0.02 | 163 | 68 |
| 1550 | 35.10 | 35.27 | 33.70 | 0.00 | 84 | 449 | 3950 | 9.38 | 8.78 | 6.11 | 0.02 | 160 | 80 |
| 1600 | 35.21 | 35.35 | 33.66 | 0.00 | 88 | 429 | 4000 | 8.68 | 8.10 | 5.52 | 0.02 | 158 | 92 |
| 1650 | 35.28 | 35.39 | 33.58 | -0.01 | 93 | 410 | 4050 | 8.00 | 7.43 | 4.95 | 0.02 | 155 | 101 |
| 1700 | 35.32 | 35.40 | 33.48 | 0.01 | 97 | 390 | 4100 | 7.35 | 6.79 | 4.42 | 0.02 | 152 | 118 |
| 1750 | 35.32 | 35.37 | 33.34 | -0.01 | 101 | 370 | 4150 | 6.72 | 6.18 | 3.91 | $-0.02$ | 150 | 132 |
| 1800 | 35.29 | 35.31 | 33.17 | 0.01 | 105 | 351 | 4200 | 6.11 | 5.59 | 3.43 | 0.02 | 116 | 116 |
| 1850 | 35.21 | 35.20 | 32.96 | 0.01 | 109 | 332 | 4250 | 5.53 | 5.02 | 2.98 | 0.01 | 143 | $16 \%$ |
| 1900 | 35.10 | 35.06 | 32.71 | 0.01 | 113 | 313 | 4300 | 4.98 | 4.49 | 2.56 | 0.01 | 110 | 178 |
| 1950 | 34.95 | 34.88 | 32.42 | 0.01 | 117 | 294 | 4350 | 4.46 | 3.99 | 2.18 | 0.01 | 137 | 19.1 |
| 2000 | 31.77 | 31.67 | 32.11 | -0.01 | 120 | 275 | 4400 | 3.96 | 3.52 | 1.82 | $-0.01$ | 133 | 211 |
| 2050 | 34.55 | 31.42 | 31.76 | 0.02 | 124 | 257 | 4450 | 3.50 | 3.08 | 1.50 | 0.01 | 129 | 229 |
| 2100 | 34.29 | 34.14 | 31.38 | 0.02 | 128 | 239 | 4500 | 3.07 | 2.67 | 1.21 | 0.01 | 126 | 247 |
| 2150 | 34.00 | 33.82 | 30.97 | 0.02 | 132 | 221 | 4550 | 2.68 | 2.30 | 0.97 | 0.01 | 122 | 265 |
| 2200 | 33.67 | 33.46 | 30.53 | 0.0\% | 135 | 204 | 4600 | 2.32 | 1.97 | 0.75 | -0.01 | 118 | 28.1 |
| 2250 | 33.31 | 33.07 | 30.06 | $-0.02$ | 139 | 187 | 4650 | 1.99 | 1.67 | 0.57 | 0.00 | 114 | 303 |
| 2300 | 32.91 | 32.64 | 29.55 | 0.02 | 14.2 | 171 | 4700 | 1.70 | 1.40 | 0.43 | 0.00 | 110 | $32: 2$ |
| 2350 | 32.48 | 32.18 | 29.0: | 0.03 | 145 | 155 | 4750 | 1.44 | 1.17 | 0.32 | 0.00 | 106 | 311 |
| 2400 | 32.02 | 31.70 | 28.47 | $-0.0 \%$ | 118 | 140 | 4800 | 1.20 | 0.98 | 0.25 | 0.00 | 102 | 360 |

$\triangle \log$ kiy and $\Delta \log _{5} k_{i}$ are in mits of the seventh decinal phace.
The constants added are, $18^{\prime \prime} .00$ to $\triangle K_{x}, 18^{\prime \prime} .00$ to $\triangle K_{y}, 1 \pi^{\prime \prime} .00$ to $\triangle K_{z}, 88$ to $\triangle \log l_{y}$, and 430 to $\triangle \log l_{z}$.

| Corrections of $K_{\mathrm{x}}, K_{\mathrm{y}}$, \&.c., due to Lunur Nutation, for $1-50$ <br>  |  |  |  |  |  |  | Corrections of $\kappa_{\mathrm{x}}, \kappa_{y}$, f.e., due to Solor Autation, for 18.50. Period of Argument XV1, 36ion:24. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Arg. } \\ & \text { Ni. } \end{aligned}$ | $\Delta K_{x}$. | $\Delta K_{y}$ | $\triangle K_{2}$. | Var.in ItOy yrs | $\Delta \log k_{\text {y }}$ | $\triangle \log \mathrm{l}_{2}$ | $\begin{gathered} \text { Arg. } \\ \text { XVi. } \end{gathered}$ | $\Delta K_{x}$ | $\Delta K_{y}$. | $\triangle K_{2}$ | $\begin{aligned} & \text { Vir. in } \\ & 100 \mathrm{yrs} . \end{aligned}$ | $\Delta \log i_{y}$. | $\log ^{1} k_{2}$ | $\begin{aligned} & \text { Solar } \\ & \text { Nimat'n } \end{aligned}$ |
| 4800 | 1.10 | 0.98 | 0.25 | 0.00 | 102 | :360 | 0 | 2.13 | 2"3:3 | 4117 | 0.00 | 6 | 105 | $+0^{\prime \prime} .36$ |
| 48.0) | 1.01 | 0.8:3 | 0.22 | 0.00 | 98 | 380) | 5 | 2.\%\% | 2.51 | 33.36 | 0.00 | 6 | 10.5 | 0.57 |
| 19)0 | (1.8!) | 0.71 | 0.22 | 0.00 | 91 | 100 | 10 | 2.86 | 2.71 | 33.53 | 0.00 | 6 | 106 | 0.76 |
| 4950 | 0.78 | 0.60 | 0.25 | 0.00 | 90 | $1: 0$ | 15 | 2.9\% | 2.91 | 33.68 | 0.00 | 6 | 107 | 0.92 |
| 5000 | 0.71 | 0.58 | 0.33:3 | $+0.01$ | 86 | 439 | 20 | 3.06 | 3.05 | 3.81 | 0.00 | 5 | 109 | 1.06 |
| 50.50 | 0.68 | 0.54 | 0.11 | +0.01 | 81 | 459 | 2.5 | 3.16 | 3.16 | 3.91 | 0.00 | 5 | 111 | +1.16 |
| 5100 | 0.68 | 0.61 | 0.58 | 0.01 | 77 | 479 | 30 | 3.2 | 3.2:3 | 3.98 | 0.00 | 4 | 114 | 1.2: |
| 51.50 | 0.72 | 0.68 | 0.76 | 0.01 | 73 | 498 | 35 | 3.25 | 3.26 | 4.01 | 0.00 | 4 | 117 | 1.25 |
| $5 \because 00$ | 0.79 | 0.78 | 0.97 | 0.01 | 69 | 517 | 40 | 3.25 | 3.26 | 1.01 | +0.01 | 3 | 120 | 1.21 |
| 5250 | 0.90 | 0.92 | 1.20 | 0.01 | 66 | 536 | 45 | 3.20 | 3. 2. | 3.97 | 0.01 | 2 | 12:3 | 1.19 |
| 5:300 | 1.05 | 1.10 | 1.50 | +0.01 | $6:$ | 55 | 50 | 3.11 | 3.14 | 3.89 | +0.01 | 2 | 126 | +1.10 |
| 53350 | 1.23 | 1.31 | 1.81 | 0.01 | 58 | 573 | 55 | 2.99 | 3.02 | 3.75 | 0.01 | 1 | 128 | 0.98 |
| 5100 | 1.45 | 1.56 | 2.15 | 0.01 | 51 | 50\% | (i) | 2.81 | 2.88 | 3.63 | 0.01 | 1 | 131 | 0.83 |
| 5150 | 1.70 | 1.81 | 2.51 | 0.0: | 50 | 609 | 65 | 2.66 | 2.71 | 3.46 | 0.01 | 1 | 133 | 0.65 |
| 5500 | 1.99 | 2.16 | 2.93 | 0.0: | 47 | $6: 7$ | 70 | 2.47 | 2.52 | 3.26 | 0.01 | 0 | 133 | 0.46 |
| 5550 | 2.31 | 2.51 | 3.36 | $+0.02$ | 43 | 614 | 75 | 2.26 | 2.31 | 3.01 | +0.01 | 0 | 133 | +0.25 |
| 5600 | 2.67 | 2.8!) | 3.8i3 | 0.00 | 40 | 660 | 80 | 2.05 | 2.10 | 2.82 | 0.01 | 0 | 133 | +0.01 |
| 56.50 | 3.06 | 3.31 | 4.33 | 0.0.2 | 37 | 676 | 8.5 | 1.83 | 1.88 | 2.59 | 0.01 | 1 | 132 | -0.18 |
| 5700 | 3.47 | 3.75 | 4.81 | 0.02 | 333 | 692 | !0 | 1.62 | 1.67 | 2.35 | 0.01 | 1 | 130 | 0.39 |
| 5750 | 3.91 | 4.2: | 5.37 | 0.0: | 30 | 707 | 95 | 1.42 | 1.47 | 2.12 | 0.01 | 2 | 127 | 0.59 |
| 5800 | 4.39 | 4.7: | 5.93 | +0.02 | 27 | 721 | 100 | 1.24 | 1.29 | 1.91 | $+0.01$ | 2 | 121 | -0.77 |
| 58.0 | 4.89 | 5.21 | 6.52 | 0.0: | 21 | 735 | 105 | 1.09 | 1.13 | 1.72 | 0.01 | 3 | 120 | 0.92 |
| 5900 | 5.42 | 5.80 | 7.13 | 0.02 | 22 | 748 | 110 | 0.97 | 1.00 | 1.85 | 0.01 | 4 | 115 | 1.05 |
| 5950 | 5.98 | 6.38 | 7.76 | . 02 | 19 | 760 | 115 | 0.87 | 0.90 | 3.10 | 0.0:2 | 5 | 110 | 1.15 |
| 6000 | 6.56 | 6.98 | 8.11 | 0.03 | 17 | 77: | 120 | 0.81 | 0.83 | 1:29 | 0.02 |  | 105 | 1.21 |
| 6050 | 7.16 | 7.60 | 9.07 | +0.03 | 14 | 783 | 125 | 0.78 | 0.80 | 1.20 | +0.02 | 8 | 99 | $-1.21$ |
| 6100 | 7.78 | 8.24 | 9.71 | 0.0.3 | 12 | 793 | 130 | 0.78 | 0.80 | 1.15 | 0.0:2 | 3 | 91 | 1.24 |
| 6150 | 8.12 | 8.90 | 10.43 | 0.03 | 10 | 803 | 135 | 0.8\% | $0.8: 3$ | 1.13 | 0.0.2 | 10 | 88 | 1.20 |
| $6: 20$ | 9.09 | 9.59 | 11.14 | 0.03 | 9 | 811 | 140 | 0.89 | 0.90 | 1.14 | 0.02 | 11 | $8: 3$ | 1.13 |
| 6250 | 9.77 | 10.29 | 11.86 | 0.03 | 7 | 819 | 145 | 1.00 | 1.00 | 1.19 | 0.02 | $1:$ | 77 | 1.02 |
| 63300 | 10.47 | 11.01 | 12.59 | +0.03 | 6 | 826 | 150 | 1.1:3 | 1.13 | 1.27 | +0.02 | 13 | 72 | -0.89 |
| (6350 | 11.18 | 11.73 | 13.32 | 0.0:3 | , | 83: | 15.5 | 1.29 | 1.29 | 1.38 | $0.0 \cdot 3$ | 11 | 68 | 0.783 |
| 6100 | 11.91 | 12.47 | 14.07 | 0.03 | 3 | 838 | 160 | 1.17 | 1.47 | 1.51 | 0.02 | 15 | 61 | 0.55 |
| 6150 | 12.65 | 13.23 | 14.8: | 0.03 | 2 | 812 | $1(6)$ | 1.67 | 1.67 | 1.66 | 0.02 | 16 | 60 | 0.35 |
| 6500 | 13.40 | 13.99 | 15.57 | 0.03 | 2 | 8.16 | 170 | 1.87 | 1.87 | 1.82 | 0.02 | 16 | 58 | -0.15 |
| 6550 | 14.16 | 14.76 | 16.33 | +0.03 | 1 | 818 | 175 | 2.08 | 2.08 | 1.99 | +0.02 | 17 | 56 | +0.06 |
| (6600 | 14.9: | 15.53 | 17.08 | 0.03 | 1 | 850 | 180 | 2.28 | 2.28 | 2.16 | 0.02 | 17 | 51 | 0.26 |
| 6650 | 15.69 | 16.31 | 17.83 | 0.03 | 0 | 8.51 | 18\%) | 2.48 | 2.49 | 2.333 | 0.03 | 17 | 51 | 0.46 |
| 6700 | 16.47 | 17.09) | 18.58 | 0.03 | 0 | $85 \%$ | 150 | 2.16 | 2.68 | 2.19 | 0.03 | 17 | 51 | 0.61 |
| 6750 | 17.25 | 17.88 | 19.33 | 0.03 | 1 | 851 | 195 | 2.81 | 2.85 | $\because .64$ | 0.03 | 16 | 55 | 0.81 |
| G800 | 18.03 | 18.66 | 20.08 | +0.03 | 1 | 819 | 200 | 2.99 | 3.01 | 2.78 | +0.033 | 16 | 56 | $+0.96$ |
| 6850 | 18.81 | 19.45 | 20.82 | 0.03 | 1 | 8.17 | 205 | 3.11 | 3.14 | 2.89 | 0.03 | 16 | 57 | 1.08 |
| 6900 | 19.59 | 20.23 | 21.5\% | 0.0:3 | 2 | 814 | 910 | 3.19 | 3.23 | 2.97 | 0.03 | 16 | 60 | 1.16 |
| 6950 | 20.37 | 21.01 | 22:27 | 0.03 | 3 | 810 | 215 | 3.25 | 3.29 | 3.0:3 | 0.03 | 15 | 62 | 1.22 |
| 7000 | 21.14 | 21.78 | 2: 2.98 | 0.03 | 4 | 835 | 220 | 3.27 | 33.32 | 3.06 | 0.0:3 | 15 | 65 | 1.21 |
| 7050 | 21.90 | 22.51 | 23.68 | +0.02 | 5 | 829 | 225 | 3.26 | 3.32 | 3.05 | +0.03 | 11 | 68 | +1.23 |
| 7100 | 22.16 | 233:29 | 21.36 | 0.02 | 7 |  | 230 | 3.22 | 3.29 | 3.02 | 0.03 | 11 | 71 | 1.19 |
| 7150 | 23.41 | \$1.03 | 25.03 | 0.02 | 8 | N14 | 235 | 3.11 | 3.20 | 2.95 | 0.03 | 13 | 73 | 1.11 |
| 7:00 | 23.31 | 21.76 | 25.68 | +0.0: | 10 | 806 | 210 | 3.0:3 | 3.11 | 2.81 | +0.0:3 | 13 | 76 | +1.00 |


| Corrections of $K_{\mathrm{x}}, K_{\mathrm{y}}$, \&.c., duc to Solar Nutation, for 1850 . P'eriod of Argument XVI.. 365d.24. |  |  |  |  |  |  |  | Parallax and Semi-diameler. |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { irg. } \\ & \text { Nvi. } \end{aligned}$ | $\triangle K_{x}$. | $\triangle K_{\mathrm{y}}$ | $\triangle K_{z}$ | $\begin{aligned} & \text { Var. in } \\ & 100 \mathrm{yrs} \end{aligned}$ | $\Delta \log i_{\text {i }}$ | $\triangle \log l_{z z}$ | $\begin{gathered} \text { Solar } \\ \text { Nutat'n } \end{gathered}$ | $\begin{aligned} & \text { log. } \\ & \text { dist.from } \\ & \text { Larth. } \end{aligned}$ | Paraflax | Semidiam. | $\left\|\begin{array}{c} \text { Log. } \\ \text { dist from } \\ \text { Earth. } \end{array}\right\|$ | Parallax | Semidiam. |
| 240 | 3.03 | 3.11 | 2.84 | $+{ }^{1 \prime} 0.03$ | 13 | 76 | +1.00 |  |  |  |  |  |  |
| 215 | 2.89 | 2.97 | 2.71 | 0.03 | 12 | 78 | 0.86 |  | 35.'22 | 31.02 | 9.85 | 12.50 | 12.07 |
| 250 | 2.72 | 2.81 | 2.51 | 0.03 | 12 | 79 | 0.69 | 9.40 9.41 | 39.22 | 31.02 | 9.85 | 12.21 | 11.80 |
| 255 | 2.51 | -2.63 | $\stackrel{2.36}{0.16}$ | 0.03 | 12 | 80 | 0.51 | 9.41 | 31.42 33.61 | 32. 19 | 9.87 | 11.94 | 11.53 |
| 260 | 2.35 | 2.44 | 2.16 | 0.04 | 12 | 81 | 0.31 | 9.42 9.4 | 33.67 | 31.75 | 9.88 | 11.66 | 11.27 |
| 205 | 2.11 | 2.23 | 1.93 | +0.01 | 12 | 81 | +0.10 | 9.41 | 32.13 | 31.03 | 9.89 | 11.40 | 11.01 |
| 270 | 1.9:2 | 2.01 | 1.70 | 0.01 | 12 | 80 | -0.12 |  |  |  |  |  |  |
| 275 | 1.71 | 1.80 | 1.47 | 0.01 | 12 | 78 | 0.33 | 9.45 | 31.39 | 30.32 | 9.90 | 11.14 | 10.76 |
| 280 | 1.51 | 1.60 | 1.24 | 0.01 | 13 | 76 | $0.5: 3$ | 9.46 | 30.68 | 29.63 | 9.91 | 10.89 | 10.51 |
| 285 | 1.82 | 1.41 | 1.02 | 0.04 | 13 | 72 | 0.72 | 9.47 | 29.98 | 28.96 | 9.92 | 10.64 | 10.27 |
| 290 | 1.15 | 1.23 | 0.81 | +0.04 | 14 | 69 | -0.89 | 9.48 | 29.30 | 28.30 | 9.93 | 10.40 | 10.01 |
| 29.5 | 1.00 | 1.08 | 0.62 | 0.04 | 15 | 61 | 1.01 | 9.49 | 28.63 | 27.65 | 9.94 | 10.16 | 9.81 |
| :300 | 0.89 | 0.96 | 0.46 | 0.01 | 16 | 59 | 1.15 | 9.50 | 27.98 | 27.0* | 9.95 | 9.93 | 9.59 |
| 305 | 0.82 | 0.88 | 0.31 | 0.04 | 17 | 54 | 1.22 | 9.51 | 27.31 | 26.40 | 9.96 | 9.70 | 9.87 |
| 310 | 0.78 | 0.84 | 0.25 | 0.04 | 19 | 48 | 1.26 | 9.50 | $26 . \%$ | 25.81 | 9.97 | 9.48 | 9.16 |
| 315 | 0.79 | 0.8 .1 | 0.20 | +0.04 | 20 | 42 | -1.25 | 9.53 | 26.11 | 25.22 | 9.98 | 9.26 | 8.95 |
| $\therefore 2$ | 0.83 | 0.88 | 0.18 | 0.04 | 21 | 36 | 1.21 | 9.51 | 25.5: | 21.65 | 9.99 | 9.05 | 8.74 |
| 325 | 0.21 | 0.6 | 0.20 | 0.04 | 22 | 31 | 1.13 |  |  |  |  |  |  |
| 330 | 1.02 | 1.67 | 0.25 | 0.04 | 23 | 25 | 1.02 | 9.55 | 24.94 | 24.09 | 0.00 | 8.85 | 8.55 |
| 335 | 1.17 | 1:20 | 0.33 | 0.05 | 24 | 20 | 0.88 | 9.56 | 21.37 | 23.54 | 0.01 | 8.65 | 8.35 |
| 310 | 1.33 | 1.36 | 0.44 | +0.05 | 25 | 15 | -0.72 | 9.57 | 23.81 | 23.00 | 0.02 | 8.45 | 8.16 |
| 31.5 | 1.51 | 1.54 | 0.57 | 0.05 | 26 | 11 | 0.54 | 9.58 | 23.27 | 22.48 | 0.03 | 8.26 | 7.198 7.79 |
| 350 | 1.72 | 1.75 | 0.73 | 0.05 | 27 | 8 | 0.33 | 9.59 | 22.71 | 21.97 | 0.04 | 8.07 | 7.79 |
| 35.5 | 1.95 | 1.98 | 0.92 | 0.05 | 27 | 5 | -0.10 | 9.60 | 22.23 | 21.47 | 0.05 | 7.89 | 7.6\% |
| 360 | 2.18 | 2.2: | 1.11 | 0.05 | 28 | 3 | +0.13 | 9.61 | 21.72 | 20.98 | 0.05 0.06 | 7.71 | 7.41 |
| 365 | 2.40 | 2.44 | 1.30 | +0.05 | 28 | 2 | +0.35 | 9.62 | 21.20 | 20.50 | 0.07 | 7.53 | 7.27 |
| 370 | 2.61 | 2.65 | 1.49 | +0.05 | 28 | 2 | +0.56 | 9.63 | 20.74 | 20.03 | 0.08 | 7.36 | 7.11 |
| $\triangle \log l_{i y}$ and $\triangle \operatorname{lng} k_{z}$ are in units of the seventh decimal. Constants added are, $2^{\prime \prime} .00$ to $\Delta K_{x}, 2^{\prime \prime} .00$ to $\triangle K_{y}, 3^{\prime \prime} .00$ to $\triangle K_{z}$, 1 to $\triangle \log k_{\mathrm{k}}$, and 130 to $\triangle \log k_{z}$. |  |  |  |  |  |  |  | 9.61 | 20.27 | 19.58 | 0.09 | 7.19 | 6.95 |
|  |  |  |  |  |  |  |  | 9.65 | 19.81 | 19.13 18.70 | 0.10 0.11 | 7.03 6.87 | 6.79 6.63 |
| TABHEXTHE <br> Factors for abtaining $\triangle x, \Delta y, \Delta z$ from $\triangle \beta$. |  |  |  |  |  |  |  | 9.67 | 18.92 | 18.87 | 0.12 | 6.71 | 6.18 |
|  |  |  |  |  |  |  |  | 9.68 | 18.49 | 17.85 | 0.13 | 6.56 | 6.31 |
|  |  |  |  |  |  |  |  | 9.69 | 18.07 | 17.45 | 0.14 | 6.41 | 6.19 |
| Orbit. Long. |  |  | For $\triangle x$. |  | For $\Delta y$. | For $\triangle z$. |  | 9.70 | 17.65 | 17.05 | 0.15 | 6.26 | 6.05 |
|  |  |  |  |  | 9.71 |  |  | 17.25 | 16.66 | 0.16 | 6.12 | 5.91 |
| 0 |  | $180^{\circ}$ | +0.020 |  |  | $-0.145$ | +0.322 |  | 9.72 | 16.86 | 16.28 | 0.17 | 5.98 | 5.78 |
| 10 |  | 190 | 0.018 |  | -0.148 | $\begin{aligned} & 0.32: 3 \\ & 0.3 \div 4 \end{aligned}$ |  | 9.73 | 16.48 | 15.91 | 0.18 0.19 | 5.85 | 5.65 |
| 20 |  | 200 |  |  | 0.150 |  |  | 9.74 | 16.10 | 15.55 | 0.19 | 5.71 | 5.52 |
| 30 |  | 210 | 0.013 |  | 0.152 | 0.325 |  | 9.75 | 15.73 | 15.20 | 0.20 | 5.58 | 5.39 |
| 40 |  | $2: 0$ |  | . 09 | 0.152 | 0.325 |  | 9.76 | 15.38 | 14.85 | 0.21 | 5.46 | 5.27 |
| 50 |  | 230 | +0.006 |  | -0.151 | +0.325 |  | 9.77 | 15.03 | 14.51 | 0.22 | 5.33 | 5.15 |
| 60 |  | 240 | 0.003 |  | 0.149 | 0.324 |  | 9.78 | 14.68 | 14.18 | 0.23 | 5.21 | 5.03 |
| 70 |  | 250 | 0.001 |  | 0.146 | 0.323 |  | 9.79 | 14.35 | . 13.86 | 0.24 | 5.09 | 4.92 |
| 80 |  | 260 | 0.000 |  | 0.143 | 0.321 |  |  |  |  |  |  |  |
| 90 |  | 270 | 0.000 |  | 0.139 | 0.320 |  | 9.80 | 14.02 | 13.51 | 0.25 | 4.98 | 4.81 |
|  |  |  | +0.002 |  | -0.136 | + 0.319 |  | 9.81 | 13.70 | 13.21 | 0.26 | 4.86 | 4.70 |
| 110 |  | 290 | 0.004 |  | -0.136 | 0.318 |  | 9.82 9.83 | 13.39 13.09 | 12.93 <br> 12.64 <br> 12.35 | 0.27 0.28 | 4.75 4.64 | 4.59 4.48 |
| $1: 0$ |  | 300 | 0.007 |  | 0.132 | 0.317 |  | 9.81 | 12.79 | 12.35 | 0.29 | 4.54 | 4.38 |
| 130 |  | 310 | 0.011 |  | 0.132 | $\begin{aligned} & 0.317 \\ & 0.317 \end{aligned}$ |  | 9.85 | 12.50 | 12.07 | 0.30 | 4.43 | 4.28 |
| 140 |  | 320 |  | . 014 | 0.133 |  |  |  |  |  |  |  |  |
| 150 |  | 330 | +0.017 |  | $-0.135$ | +0.318 |  |  |  |  |  |  |  |
| 160 |  | 310 | 0.019 |  | 0.138 | 0.3190.321 |  |  |  |  |  |  |  |
| 170 |  | 3350 | 0.020+0.020 |  | 0.141 |  |  |  |  |  |  |  |  |
| 180 |  | 360 |  |  | -0.145 | +0.392 |  |  |  |  |  |  |  |

Motion of the Arguments for Centuries.


| TABLE KI.V. <br> Values of the Equation $0^{\prime \prime} .28$ :2 $\sin \left(4 t^{\prime \prime \prime}+3 t^{\prime}-7 l^{\prime \prime}\right.$ $+147^{\circ} .1$.) |  |  | Reduction to the Ecliptic for 1850. <br> Longitude $+\left(360^{\circ}-\delta\right)$, or this angle diminished by $180^{\circ}$. |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Arg. | ${ }^{\prime}$ | $10^{\prime}$ | $20^{\prime}$ | $30^{\prime}$ | 40' | $50^{\prime}$ | $\begin{aligned} & \text { Diff. } \\ & \text { for } 10^{\prime} \end{aligned}$ | $\begin{aligned} & \text { Var. in } \\ & 100 \text { yrs. } \end{aligned}$ |  |
| Year. | Equa. | 1)ifl: for 10 yrs . | \% | $\begin{array}{rr} 1 \prime \prime \\ -0 & 0.00 \\ 0 & 6.31 \end{array}$ | $\begin{aligned} & 11.05 \\ & 1.36 \end{aligned}$ | $\begin{aligned} & \prime \prime \prime \\ & 6.10 \\ & 8.41 \end{aligned}$ |  |  | ${ }^{\prime \prime}{ }^{\prime \prime} .26$ |  |  |  |
|  |  |  |  |  |  |  | 9.46 | 10.51 | 11.56 | 1.05 | 0.00 | 178 |
| 1800 | +0. ${ }^{\prime \prime}$ | $\begin{array}{r} -3 \\ 15 \end{array}$ | 233 | $\begin{array}{ll} 0 & 12.61 \\ 0 & 18.90 \end{array}$ | $\begin{aligned} & 13.66 \\ & 19.94 \end{aligned}$ | $\begin{aligned} & 14.71 \\ & 20.99 \end{aligned}$ | $\begin{array}{r} 15.76 \\ 2.2 .01 \end{array}$ | $\begin{gathered} 16.80 \\ 23.08 \end{gathered}$ | $\begin{aligned} & 17.85 \\ & 24.12 \end{aligned}$ | 1.05 | -0.01 | $177$ |
| 1810 | 0.27\% |  |  |  |  |  |  |  |  | 1.04 | 0.01 |  |
| 18:0 | 0.251 | 27 | 4 | 025.16 | 26.20 | 27.24 | 28.28 | 29.31 | 30.35 |  | 0.02 | 175 |
| 1840 | 0.218 | 3745 | 6 | -0 31.39 | $\begin{aligned} & 32.43 \\ & 38.61 \end{aligned}$ | 33.4639.64 | 31.5040.66 | $\begin{aligned} & 35.53 \\ & 41.69 \end{aligned}$ | $\begin{aligned} & 36.56 \\ & 42.71 \end{aligned}$ | 1.031.02 | $-0.02$ | $\begin{aligned} & 174 \\ & 173 \end{aligned}$ |
|  | 0.176 |  |  | 037.59 |  |  |  |  |  |  | 0.020.03 |  |
|  |  | -51 | 6 | 043.74 | $\begin{aligned} & 44.76 \\ & 50.84 \end{aligned}$ | $\begin{aligned} & 45.77 \\ & 51.85 \end{aligned}$ | $\begin{aligned} & 46.79 \\ & 52.85 \end{aligned}$ | 47.80 | 48.82 | 1.011.01 |  | 172 |
| 1850 1860 | +0.128 0.073 0 |  | 8 | 049.83 |  |  |  | 53.8659.85 | 51.87 |  | 0.03 | 171 |
| 1860 | 0.073 +0.016 | 56 |  | 055.87 | 56.87 | 57.86 | 58.86 |  | 60.85 | 1.00 | 0.03 | 170 |
| 1880 | -0.0.43 | 58 |  | -1 1.84 | 2.83 | 3.82 | 4.80 | 5.78 | 6.76 |  | -0.04 | 169168 |
| 1890 | 0.100 | 54-49 | 10 | 17.73 |  |  |  |  |  |  |  |  |
| 1900 |  |  | 12 | 113.54 | 14.50 | 15.16 | 16.11 | 17.36 | 18.31 | 0.97 0.95 | 0.04 0.05 | $\begin{aligned} & 168 \\ & 167 \end{aligned}$ |
| 1910 | -0.152 | $\begin{aligned} & 42 \\ & 31 \end{aligned}$ | 13 | $\begin{array}{ll} 1 & 19.26 \\ 1 & 24.88 \end{array}$ | $\begin{aligned} & 20.20 \\ & 25.81 \end{aligned}$ | $\begin{aligned} & 21.11 \\ & 26.74 \end{aligned}$ | $\begin{aligned} & 22.08 \\ & 27.66 \end{aligned}$ | 23.0128.58 | $\begin{aligned} & 23.95 \\ & 29.50 \end{aligned}$ | 0.940.92 | 0.050.05 | 166165 |
| 1920 | 0.236 |  |  |  |  |  |  |  |  |  |  |  |
| 1930 | 0.261 | 20 | 15 | -1 30.41 | 21. 22 | 32.23 | 33.13 | $\begin{aligned} & 31.03 \\ & 39.36 \end{aligned}$ | $\begin{aligned} & 34.93 \\ & 40.24 \end{aligned}$ | $\begin{aligned} & 0.90 \\ & 0.88 \end{aligned}$ | -0.06 | 161163 |
| 1940 | 0.277 | -10 | 16 | 135.82 | 36.71 | 37.60 | 38.48 |  |  |  | 0.06 |  |
| 1950 | -0.282 |  | 17 | 141.11 | 41.98 | 42.85 | 43.71 | 44.5749.66 |  |  | 0.06 | 16: |
| 1960 | -0.282 | + ${ }_{14}$ | 18 | 146.28 | 47.13 | 47.98 | 48.82 |  | $50.50$ | $0.84$ | 0.07 | 161160 |
| 1970 | 0.254 | 25 | 19 | 1-51.33 | 52.16 | 52.98 | 53.80 | 54.61 | 55.42 | 0.82 | 0.07 |  |
| 1980 | 0.223 | 36 | $\begin{aligned} & 20 \\ & 21 \end{aligned}$ | -1 50.23 | 57.04 | 57.84 | 58.64 | 59.43 | 60.22 | 0.80-0.07 |  | 159158 |
| 1990 | 0.182 | 44+51 |  | $\begin{array}{ll} 2 & 1.00 \\ 2 & 5.62 \end{array}$ | $\begin{aligned} & 1.78 \\ & 6.37 \end{aligned}$ | $\begin{aligned} & 2.56 \\ & 7.12 \end{aligned}$ | 3.33 | $\begin{aligned} & 4.10 \\ & 8.60 \end{aligned}$ | $\begin{aligned} & 4.86 \\ & 9.31 \end{aligned}$ | 0.77 | 0.08 |  |
| 2000 | -0.131 |  | 22 |  |  |  | 7.86 |  |  | 0.74 | 0.08 | 158 157 |
| 2010 | 0.080 | $\begin{array}{r} +01 \\ 56 \\ 58 \end{array}$ | 23 | $\begin{array}{ll}2 & 10.08 \\ 2 & 14.39\end{array}$ | $\begin{aligned} & 10.81 \\ & 15.09 \end{aligned}$ | $\begin{aligned} & 11.54 \\ & 15.79 \end{aligned}$ | 12.2616.48 | $\begin{aligned} & 12.98 \\ & 17.17 \end{aligned}$ | $\begin{aligned} & 13.69 \\ & 17.86 \end{aligned}$ | $0.72$ $0.69$ | $\begin{aligned} & 0.08 \\ & 0.09 \end{aligned}$ | $\begin{aligned} & 156 \\ & 155 \end{aligned}$ |
| 2020 | -0.023 |  |  |  |  |  |  |  |  | $0.69$ |  |  |
| ${ }^{2} 030$ | +0.036 | $53$ | 2526 | -2 18.54 | 19.22 | 19.89 | 20.56 | 21.22 | 21.87 | 0.66 | -0.09 | 154 |
| 2040 | 0.093 |  |  | 222.51 | 23.16 | 23.80 | 24.44 | 25.07 | 25.70 | 0.63 | 0.09 | 153 |
| 2050 | +0.146 | 50 | 27 | 226.32 | 26.91 | 27.55 | 28.16 | 28.76 | 29.35 | 0.60 | 0.09 | 152 |
| 2060 | +0.193 | 42 | 28 | ${ }^{2} 2929.94$ | 30.52 | 31.10 | 31.67 | 32.24 | 32.81 | 0.57 | 0.10 | 151 |
| 2070 | 0.2:31 | 33 | 29 | 233.38 | 33.94 | 34.49 | 35.01 | 35.58 | 36.11 | 0.54 | 0.10 | 150 |
| 2080 | 0.259 | 23 | 30 | -2 36.64 | 37.16 | 37.68 | 38.19 | 38.70 | 39.20 | 0.51 | $-0.10$ | 149 |
| 2090 | 0.277 | +12 | 31 | ¢ 39.70 | 40.19 | 40.68 | 41.16 | 41.61 | 42.11 | 0.48 | 0.10 | 148 |
| 2100 | +0.282 |  | 32 | 242.57 | 43.03 | 43.48 | 4393 | 41.38 | 41.80 | 0.45 | 0.10 | 147 |
| 2110 | +0.275 | -13 | 33 | 245.25 | 45.68 | 46.10 | 46.52 | 46.93 | 47.33 | 0.41 | 0.10 | 146 |
|  |  |  | 34 | 247.72 | 48.11 | 48.49 | 48.87 | 49.25 | 49.62 | 0.38 | 0.11 | 145 |
|  |  |  | 35 | -2 49.99 | 50.35 | 50.70 | 51.05 | 51.39 | 51.72 | 0.34 | $-0.11$ | 144 |
|  |  |  | 36 | 252.04 | 52.36 | 52.68 | 52.99 | 53.30 | 53.60 | 0.31 | 0.11 | 143 |
| Multi |  | - | 37 | 253.90 | 54.19 | 51.47 | 51.75 | 55.02 | 55.28 | 0.27 | 0.11 | 142 |
|  | uis Equa |  | 38 | 255.51 | 55.79 | 56.01 | 56.28 | $56.5 \pm$ | 56.75 | 0.24 | 0.11 | 141 |
|  |  |  | 39 | 256.96 | 57.18 | 57.39 | 57.60 | 57.80 | 57.99 | 0.20 | 0.11 | 110 |
|  |  |  | 40 | $-258.17$ | 58.35 | 58.52 | 58.69 | 58.85 | 59.01 | 0.17 | -0.11 | 139 |
| 1 |  | 302.4 | 41 | 259.17 | 59.32 | 59.46 | 59.59 | 59.72 | 59.84 | 0.13 | 0.11 | 138 |
| 2 |  | ( 501.8 | 42 | 259.94 | 60.05 | 60.15 | 60.25 | 60.34 | 60.42 | 0.09 | 0.11 | 137 |
| 3 |  | 907.2 | 43 | 330.50 | 0.57 | 0.61 | 0.70 | 0.75 | 0.79 | 0.05 | 0.11 | 136 |
| 4 |  | 209.6 | 44 | -3 0.83 | 0.86 | 0.89 | 0.91 | 0.93 | 0.94 | 0.02 | -0.11 | 135 |
|  |  | 1512.0 |  | $60^{\prime}$ | $50^{\prime}$ | $40^{\prime}$ | $33^{\prime}$ | 20 ${ }^{\prime}$ | $10^{\prime}$ |  |  | Arg. |
| 7 |  | 116.8 |  | -When | curt | tio |  | rcud | the |  |  | able, |
|  |  | 721.6 | the are | ns of minute lected with t | must be sign + | ad from instead of | bott | and the | Reductio | ud it | ecular | iation |


| Argument $=$ Orbit Longitude $+\left(360^{\circ}-8\right)$, or this angle diminished by $180^{\circ}$. |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Arg. | $9^{\prime}$ | $10^{\prime}$ | $20^{\prime}$ | $30^{\prime}$ | $40^{\prime}$ | $59^{\prime}$ | $\begin{aligned} & \text { Diff: } \\ & \text { for } 10^{\prime} . \end{aligned}$ | Var. in 100 yrs. |  |
| 45 | -3 ${ }^{\prime} 0.95$ | 0.95 | 0.94 | ${ }^{\prime \prime} 1$ | 0.91 | 0.88 | ${ }^{\text {\% }} 0.02$ | -0.11 | 134 |
| 46 | $\begin{array}{lll}3 & 0.85\end{array}$ | 0.81 | 0.77 | 0.72 | 0.66 | 0.59 | 0.05 | 0.11 | 133 |
| 47 | $3 \quad 0.52$ | 0.44 | 0.36 | 0.27 | 0.18 | 0.08 | 0.09 | 0.11 | 132 |
| 48 | 259.98 | 59.87 | 59.75 | 59.63 | 59.50 | 59.36 | 0.13 | 0.11 | 131 |
| 49 | 259.21 | 59.06 | 58.90 | 58.74 | 58.57 | 58.40 | 0.16 | 0.11 | 130 |
| 50 | -2 58.23 | 58.05 | 57.86 | 57.66 | 57.46 | 57.25 | 0.20 | -0.11 | 129 |
| 51 | 257.03 | 56.80 | 56.57 | 56.34 | 56.10 | 55.86 | 0.24 | 0.11 | 128 |
| 52 | 255.61 | 55.35 | 55.09 | 54.82 | 54.54 | 54.26 | 0.27 | 0.11 | 127 |
| 53 | 253.98 | 53.69 | 53.39 | 53.09 | 52.78 | 52.46 | 0.31 | 0.11 | 126 |
| 54 | 252.14 | 51.81 | 51.48 | 51.14 | 50.80 | 50.45 | 0.34 | 0.11 | 125 |
| 55 | -2 50.09 | 49.73 | 49.36 | 48.99 | 48.61 | 48.22 | 0.38 | -0.10 | 124 |
| 56 | 247.83 | 47.43 | 47.03 | 46.62 | 46.21 | 45.79 | 0.41 | 0.10 | 123 |
| 57 | 245.37 | 44.94 | 44.51 | 44.07 | 43.62 | 43.16 | 0.44 | 0.10 | 122 |
| $58$ | 242.70 | 42.23 | 41.76 | 41.28 | 40.80 | 40.32 | 0.48 | 0.10 | 121 |
| 59 | 239.84 | 39.35 | 38.85 | 38.35 | 37.84 | 37.32 | 0.51 | 0.10 | 120 |
| 60 | -2 36.78 | 36.25 | 35.72 | 35.18 | 34.64 | 34.09 | 0.54 | $-0.10$ | 119 |
| 61 | 233.53 | 32.97 | 32.41 | 31.84 | 31.27 | 30.69 | 0.57 | 0.09 | 118 |
| 62 | 230.09 | 29.50 | 28.91 | 28.31 | 27.71 | 27.10 | 0.60 | 0.09 | 117 |
| 63 | 226.47 | 25.85 | 25.22 | 24.59 | 23.95 | 23.31 | 0.63 | 0.09 | 116 |
| 64 | 222.67 | 22.02 | 21.37 | 20.71 | 20.05 | 19.38 | 0.66 | 0.09 | 115 |
| 65 | -2 18.69 | 18.01 | 17.33 | 16.64 | 15.95 | 15.25 | 0.69 | -0.08 | 114 |
| 66 | 214.55 | 13.84 | 13.13 | 12.41 | 11.69 | 10.97 | 0.72 | 0.08 | 113 |
| 67 | 210.24 | 9.51 | 8.77 | 8.03 | 7.29 | 6.54 | 0.74 | 0.08 | 112 |
| $68$ | $2 \quad 5.78$ | 5.02 | 4.26 | 3.49 | 2.72 | 1.94 | 0.77 | 0.07 | 111 |
| 69 | 161.16 | 60.38 | 59.59 | 58.80 | 58.01 | 57.21 | 0.79 | 0.07 | 110 |
| 70 | -156.39 | 55.58 | 54.77 | 53.95 | 53.13 | 52.30 | 0.82 | $-0.07$ | 109 |
| 71 | 151.48 | 50.65 | 49.82 | 48.98 | 48.14 | 47.29 | 0.84 | 0.07 | 108 |
| 72 | 146.44 | 45.59 | 44.74 | 43.88 | 43.01 | 42.14 | 0.86 | 0.07 | 107 |
| 73 | 141.26 | 40.39 | 39.51 | 38.63 . | 37.74 | 36.85 | 0.88 | 0.06 | 106 |
| 74 | 135.96 | 35.07 | 34.17 | 33.27 | 32.36 | 31.45 | 0.90 . | 0.06 | 105 |
|  | -1 30.54 | 29.63 | 28.71 | 27.79 | 26.87 | 25.95 | 0.92 | $-0.06$ | 104 |
| $76$ | 125.02 | 24.09 | 23.16 | 22.22 | 21.28 | 20.34 | 0.94 | 0.05 | 103 |
| 77 | 119.39 | 18.44 | 17.49 | 16.54 | 15.58 | 14.62 | 0.95 | 0.05 | 102 |
| 78 | 113.66 | 12.70 | 11.73 | 10.76 | 9.79 | 8.82 | 0.97 | 0.05 | 101 |
| 79 | 17.84 | 6.86 | 5.88 | 4.90 | 3.92 | 2.93 | 0.98 | 0.04 | 100 |
| 80 | -0 61.94 | 60.95 | 59.96 | 58.96 | 57.96 | 56.96 | 1.00 | $-0.04$ | 99 |
| 81 | 055.96 | 54.96 | 53.95 | 52.94 | 51.94 | 50.93 | 1.01 | 0.03 | 98 |
| 82 | 049.92 | 48.91 | 47.90 | 46.88 | 45.86 | 44.84 | 1.02 | 0.03 | 97 |
| 83 | 043.81 | 42.79 | 41.76 | 40.74 | 40.71 | 39.68 | 1.03 | 0.03 | 96 |
| 84 | 037.65 | 36.62 | 35.58 | 34.55 | 33.52 | 32.48 | 1.03 | 0.02 | 95 |
| 85 | -0 31.45 | 30.42 | 29.38 | 28.34 | 27.30 | 26.26 | 1.04 | -0.02 | 94 |
| 86 | 025.21 | 24.17 | 23.13 | 22.08 | 21.03 | 19.98 | 1.05 | 0.02 | 93 |
| 87 | 018.93 | 17.88 | 16.83 | 15.78 | 14.73 | 13.68 | 1.05 | 0.01 | 92 |
| $88$ | 012.63 | 11.58 | 10.53 | 9.48 | 8.42 | 7.37 | 1.05 | $-0.01$ | 91 |
| 89 | -0 6.32 | 5.27 | 4.21 | 3.16 | 2.11 | 1.05 | 1.05 | 0.00 | 90 |
|  | $60^{\prime}$ | $50^{\prime}$ | $40^{\prime}$ | $30^{\prime}$ | $20^{\prime}$ | $10^{\prime}$ |  |  | Arg. |

Note.-When the degrees of the Argument are read from the right hand side of the Table, the tens of minutes must be read from the bottom; and the Reduction and its Secular Variation are affected with the sign + instead of - .
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[^0]:    * Tables du Soleil, exécutées d'après les ordres de la Société Royale des Sciences de Copenhague, par MM. P. A. Hansen et C. F. R. Olufsen. Copenhague. 1853.
    $\dagger$ The Pulkowa constant of aberration $20^{\prime \prime} .4451$ should however be employed instead of $20^{\prime \prime} 255$.
    $\ddagger$ Peters' Numerus Constans Nutationis, p. 71.
    § Tables du Soleil, p. 21.

[^1]:    *This is the value of the longitade of the perilielion at the epoch 1850.0 , which was employed in computing the tables of the perturbations to double entry.

    + Ligoronsly, the Argument which should be employed as the horizontal Argument of the tables of perturbations to double entry, has this expression,

    $$
    71 d .65641+d-924.200801109 \mathrm{~m},
    $$

    

[^2]:    "The single term in the perturbations of the latitude, duc to the action of Saturn, has not been tabulated. It seemed super. fluous to take account of it, when the corresponding term in the latitude of the Larth, producing, at maximum, an effeet in the geocentric position of Venus, nearly three times greater, is neglected by Hansen and Olufsen in their "Tables du Solcil."

[^3]:    * Der Venus-durehgang von 1769, p. 107.

[^4]:    

